Porous Microstructure Analysis (PuMA)

Presenter: Federico Semeraro

AMA at Thermal Protection Materials Branch (ARC-TSM)

***Lead Developers**:* J.C. Ferguson and F. Semeraro

***Other Contributors**:* J. Thornton, F. Panerai, A. Borner, N.N. Mansour, S. Fraile Izquierdo, J.B.E. Meurisse

June 16th, 2022

ANALYTICAL MECHANICS ASSOCIATES

Predictive Material Modeling (PMM) group

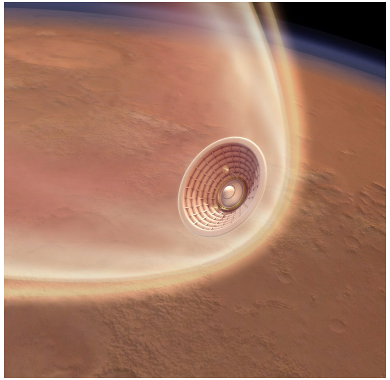
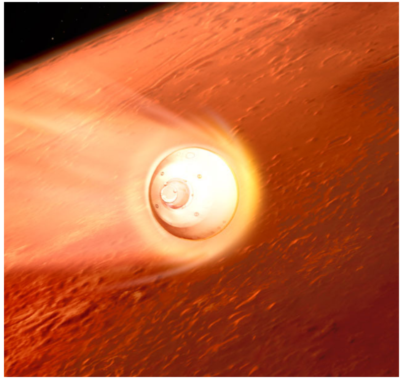
Entry System Modeling (ESM) project

Content

- Motivation and objectives
- Overview of PuMA
  - Open-source release
  - Material properties computation
  - Artificial geometry generation
- Effective properties for anisotropic porous media
  - Fiber orientation
  - Conductivity
  - Elasticity
  - Permeability

Thermal Protection Systems (TPS)

Need for Thermal Protection Systems

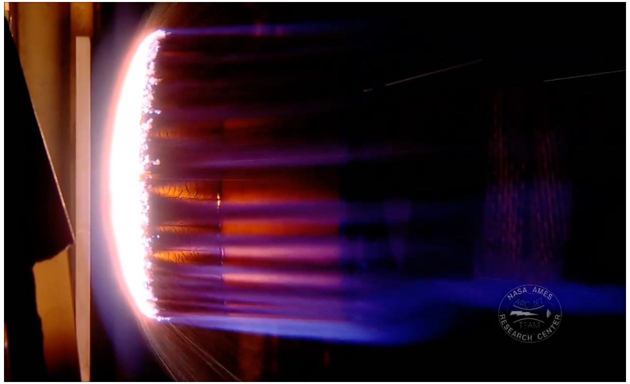



Ground-based Testing

P. Agrawal et. al. 2016.

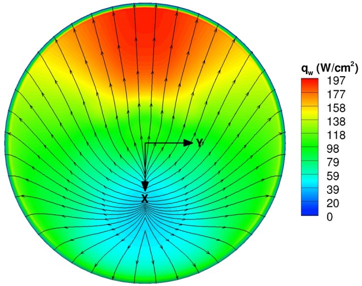
Virgin PICA Sample

Charred PICA Sample

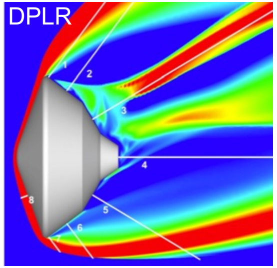


Arcjet Testing of TPS

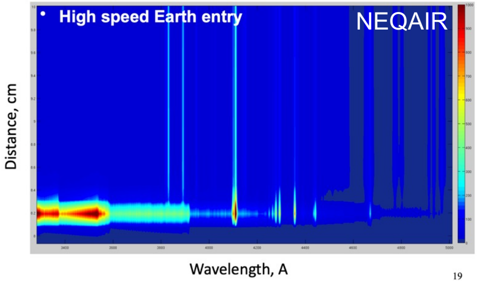
Computational Modeling



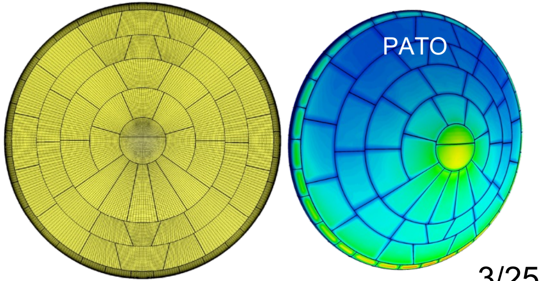
Hypersonic CFD



Radiation Analysis

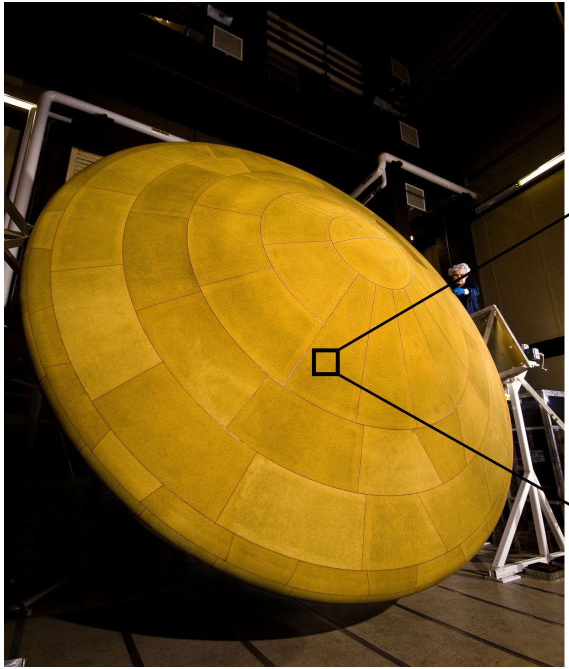


Material Response

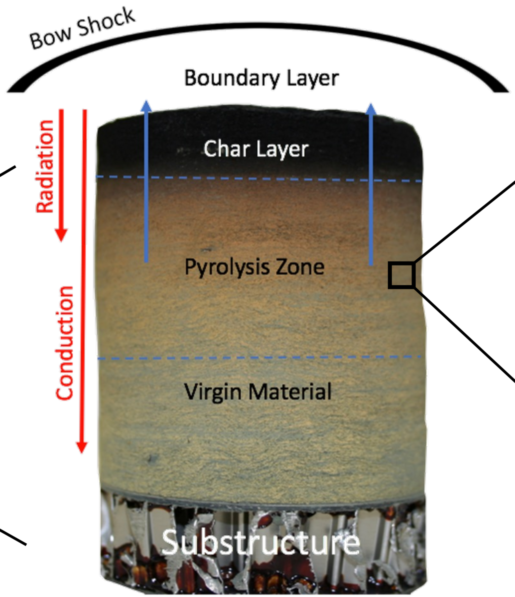


Modeling TPS

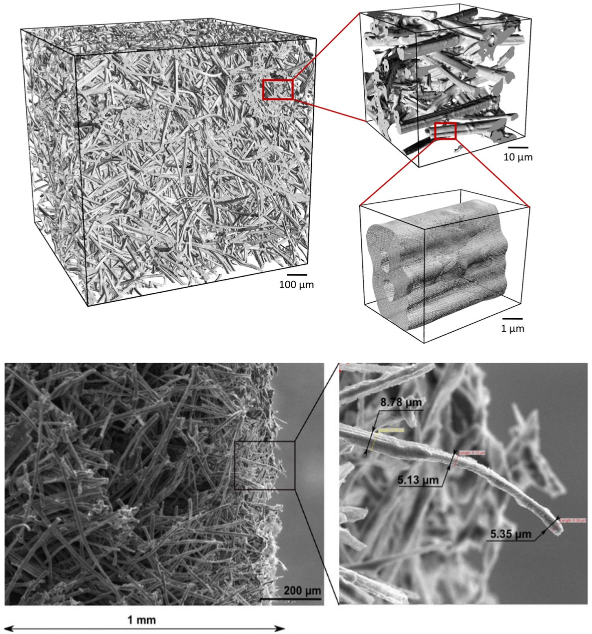
Full scale



Mars Science Laboratory (MSL) heat shield



Microscale

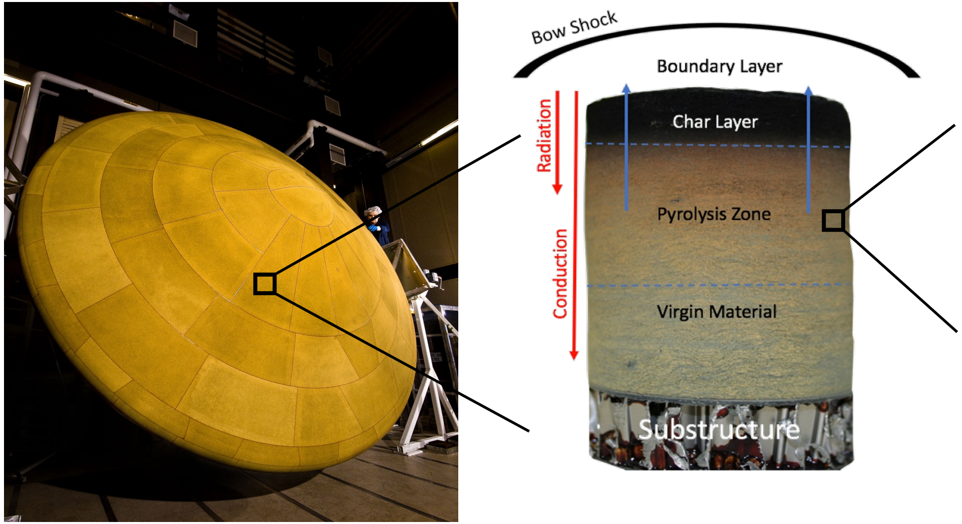


Carbon-fiber microstructure

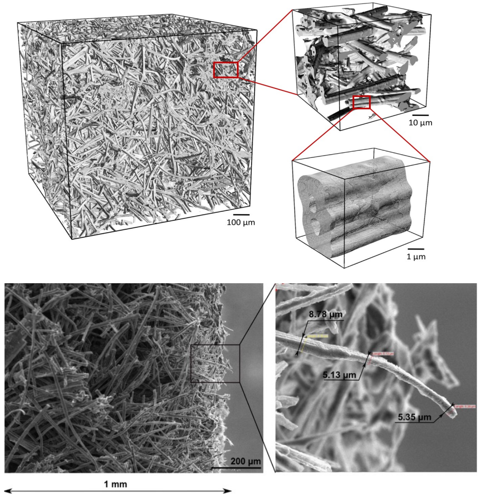
NASA Modeling Capabilities

FIAT | CHAR | Icarus | PATO → **Full scale**

PuMA → **Microscale**



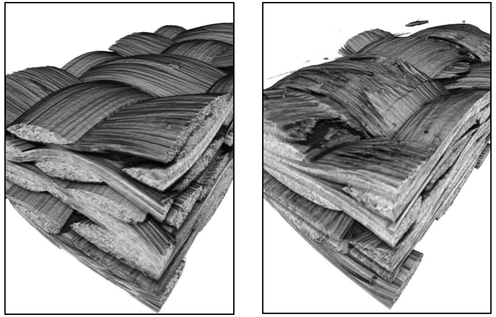
Mars Science Laboratory (MSL) heat shield



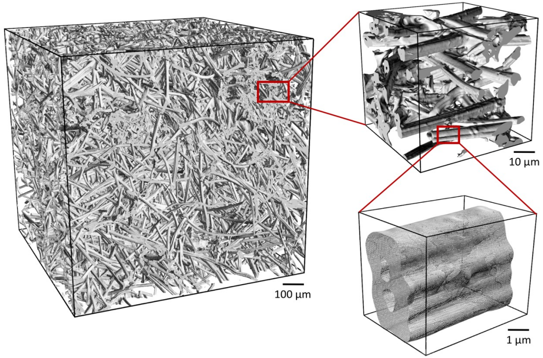
Carbon-fiber microstructure

Heat Shield Microstructures

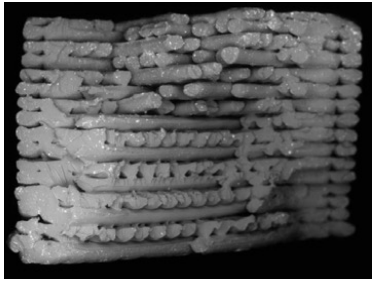
3D carbon fabric prior to (left) and after (right) Arcjet exposure



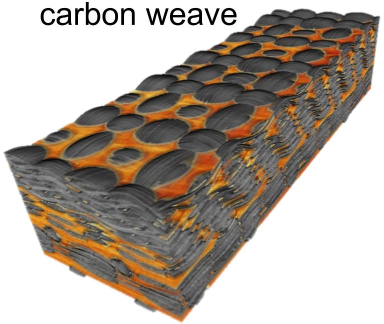
Fibrous architectures



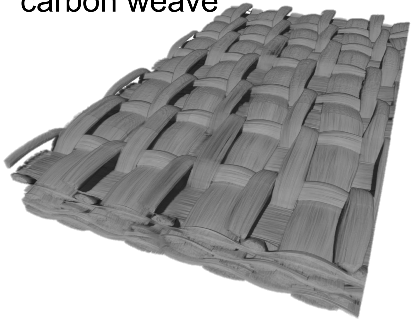
3D printed material



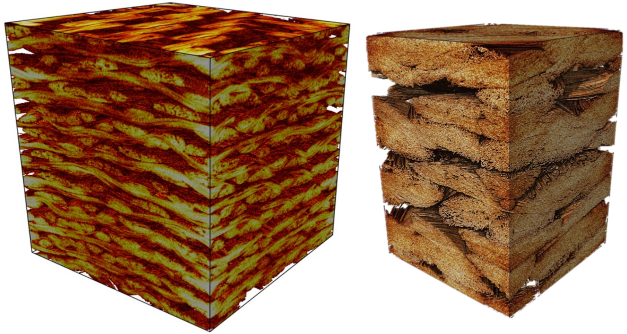
12-ply infused carbon weave



6-ply dry carbon weave

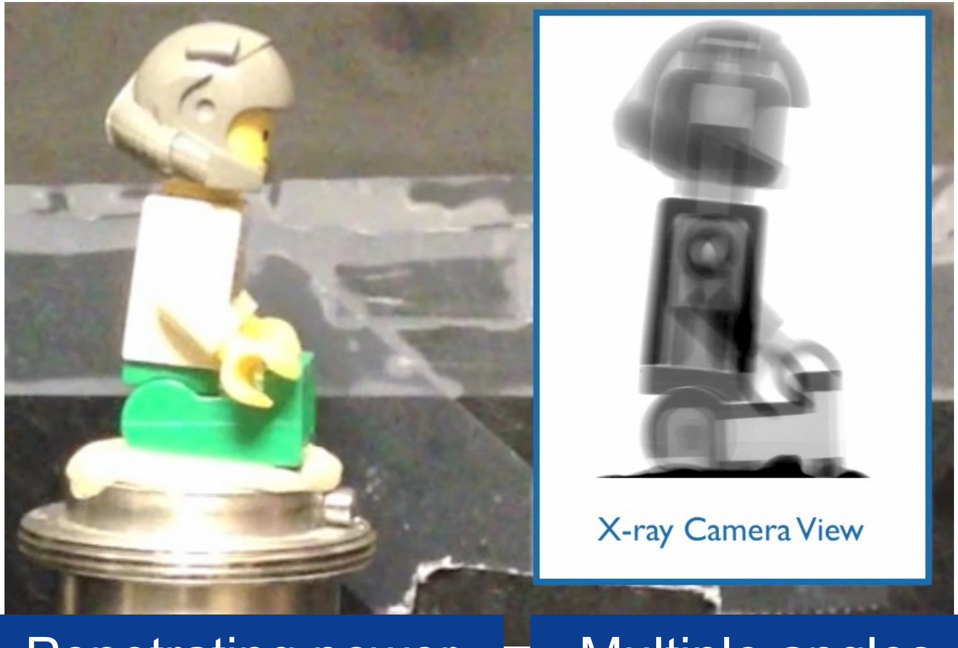


Multiscale imaging of silica weave



X-ray Microtomography

Collect X-ray images of the sample as you rotate it through 180°



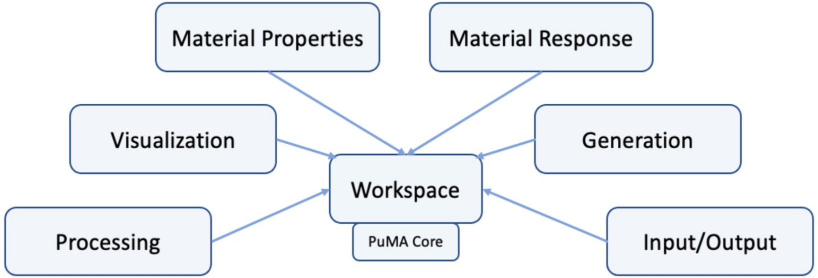
Penetrating power

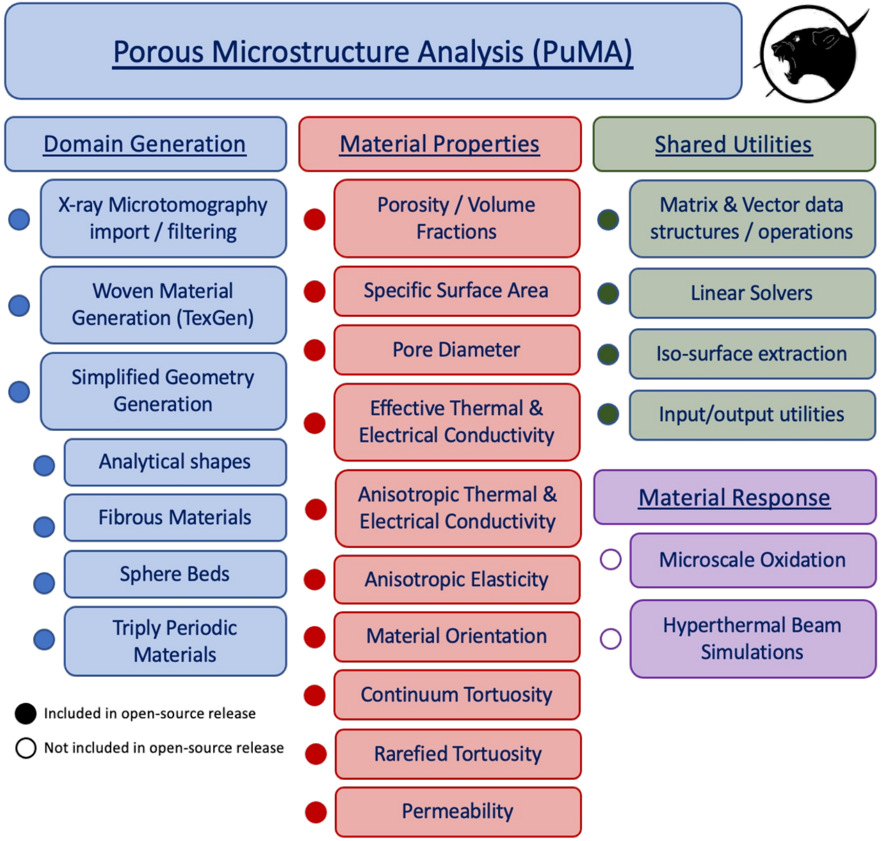
Multiple angles

Use this series of images to “reconstruct” the 3D object

Courtesy of D. Parkinson (ALS)

PuMA Behind the Scenes





Porous Microstructure Analysis (PuMA) v3 release

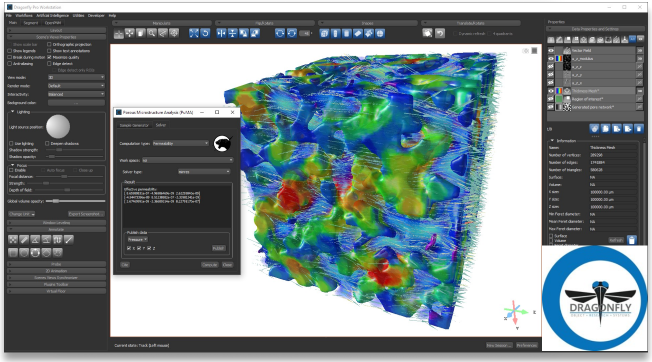
Installation: conda install -c conda-forge puma

Open-source repository: https://github.com/nasa/puma

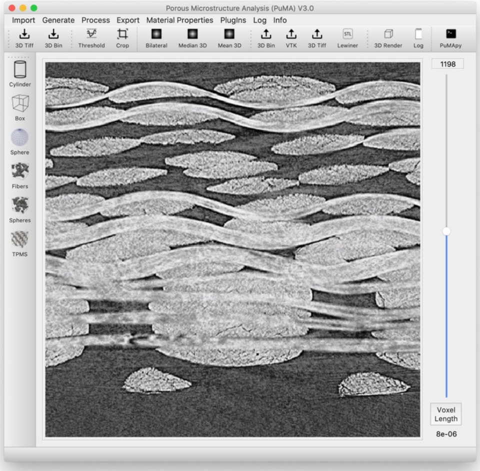
Documentation: https://puma-nasa.readthedocs.io

Community chat: https://gitter.im/puma-nasa/community

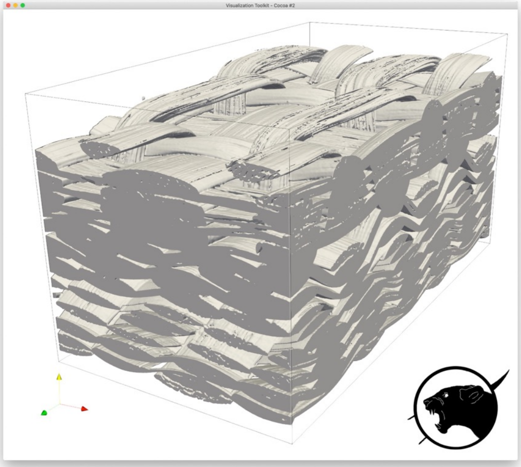
Tutorials: PuMA YouTube channel and online Colab notebook



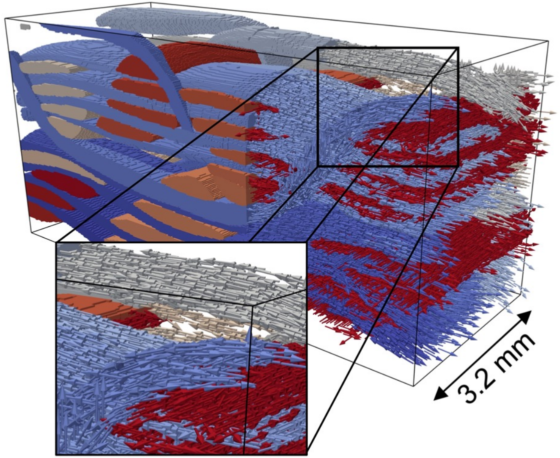
a)



b)



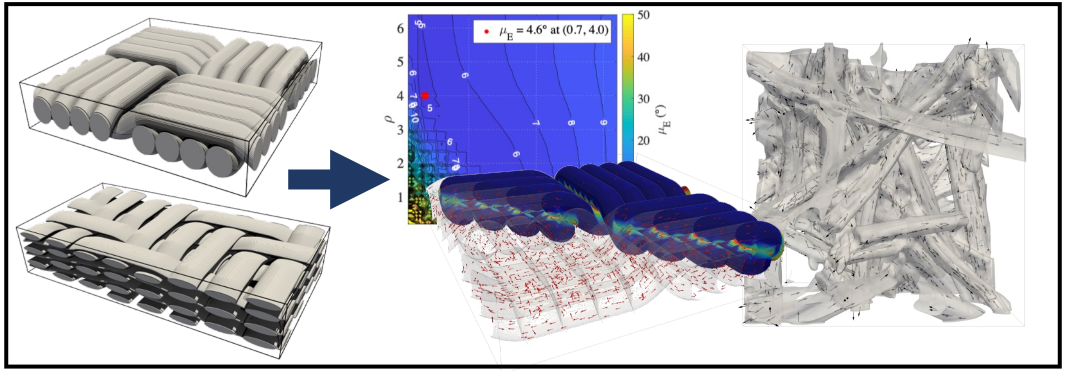
c)



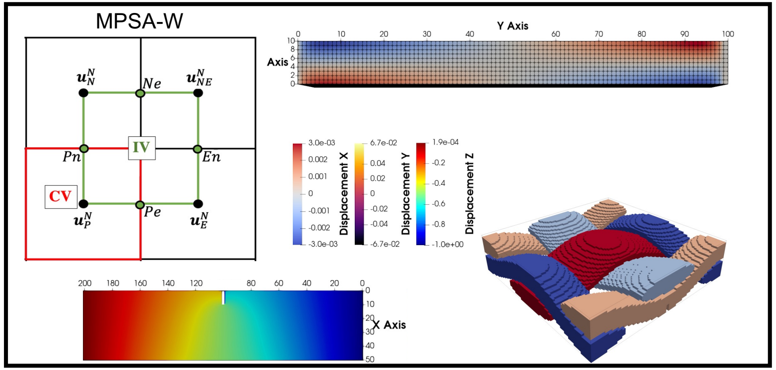
Ferguson, J.C., Semeraro, F., Thornton, J.M., Panerai, F., Borner, A., Mansour, N.N., 2021. Update 3.0 to “PuMA: The Porous Microstructure Analysis software”, *SoftwareX*

Advanced Material Property Computation

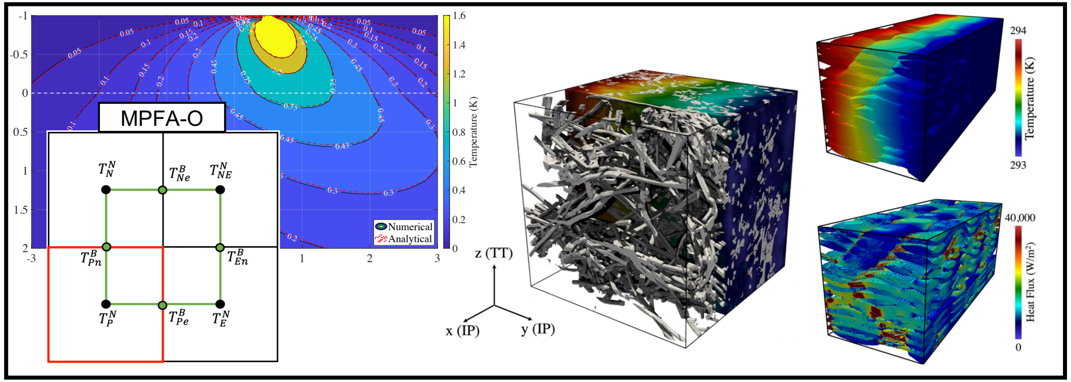
Local orientation. *Computational Materials Science* (2020)



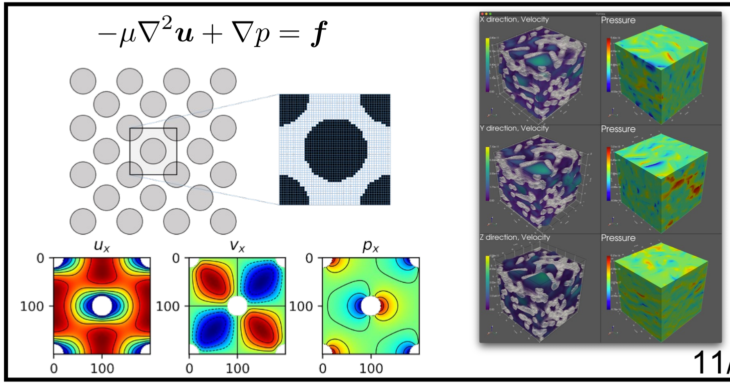
Effective elasticity. *AIAA Scitech Forum* (2022, 2023)



Effective conductivity. *Computational Materials Science* (2021)



Effective permeability. *npj Computational Materials* (2022)

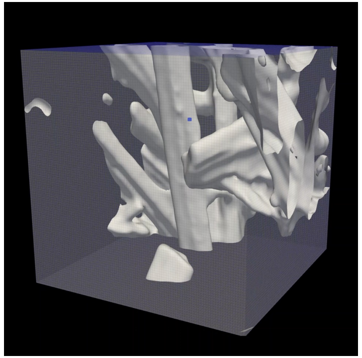


Particle Methods in PuMA

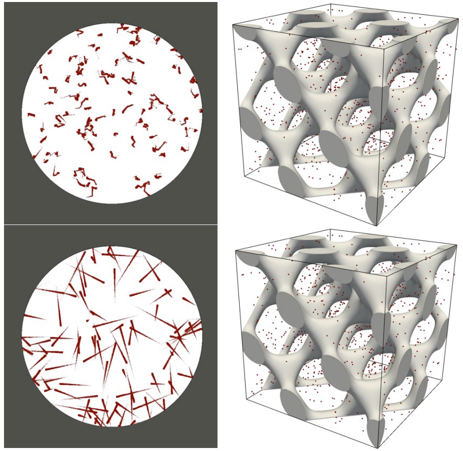
Oxidation

4D tomography

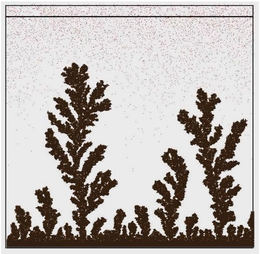
Radiative Conductivity



Tortuosity

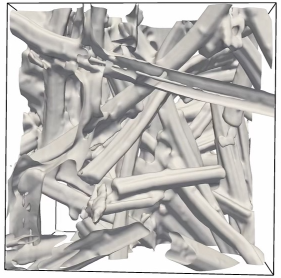


Dendrites in Batteries



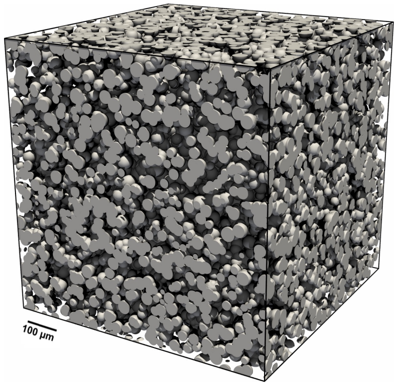
Dendrite growth in lithium metal batteries. Wood et al. ACS Central Science. (2016)

Material Orientation

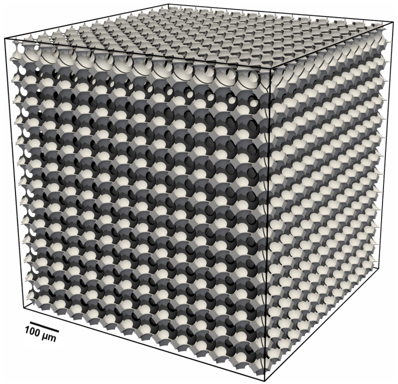


Artificial Domain Generation

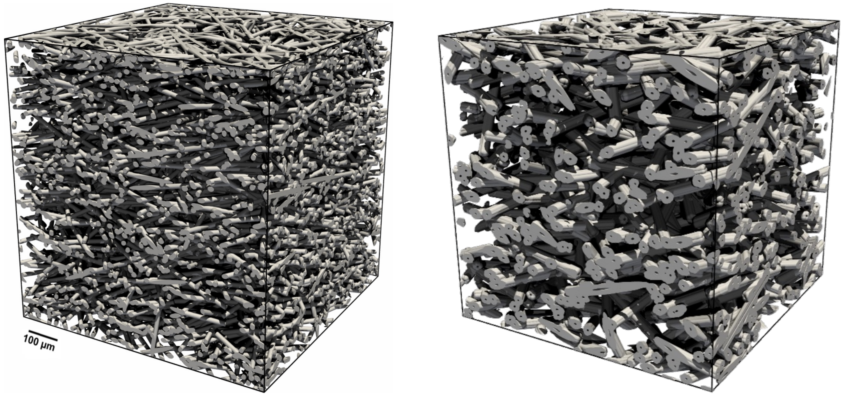
Packed Sphere Beds



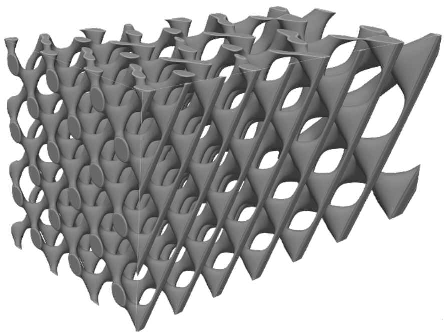
Periodic Foams



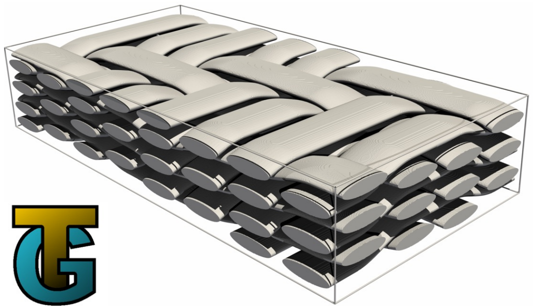
Fiber Structures



Triply Periodic Minimal Surface (TPMS)



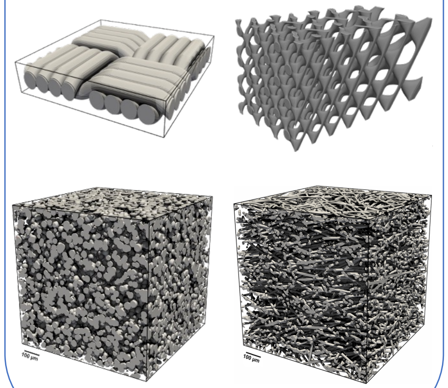
Woven geometries



Material Optimization

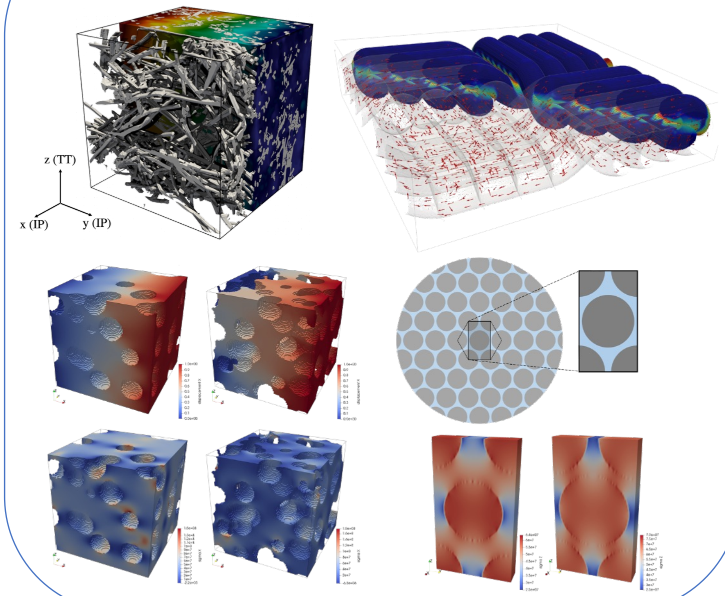
Compute Properties

Material Generation



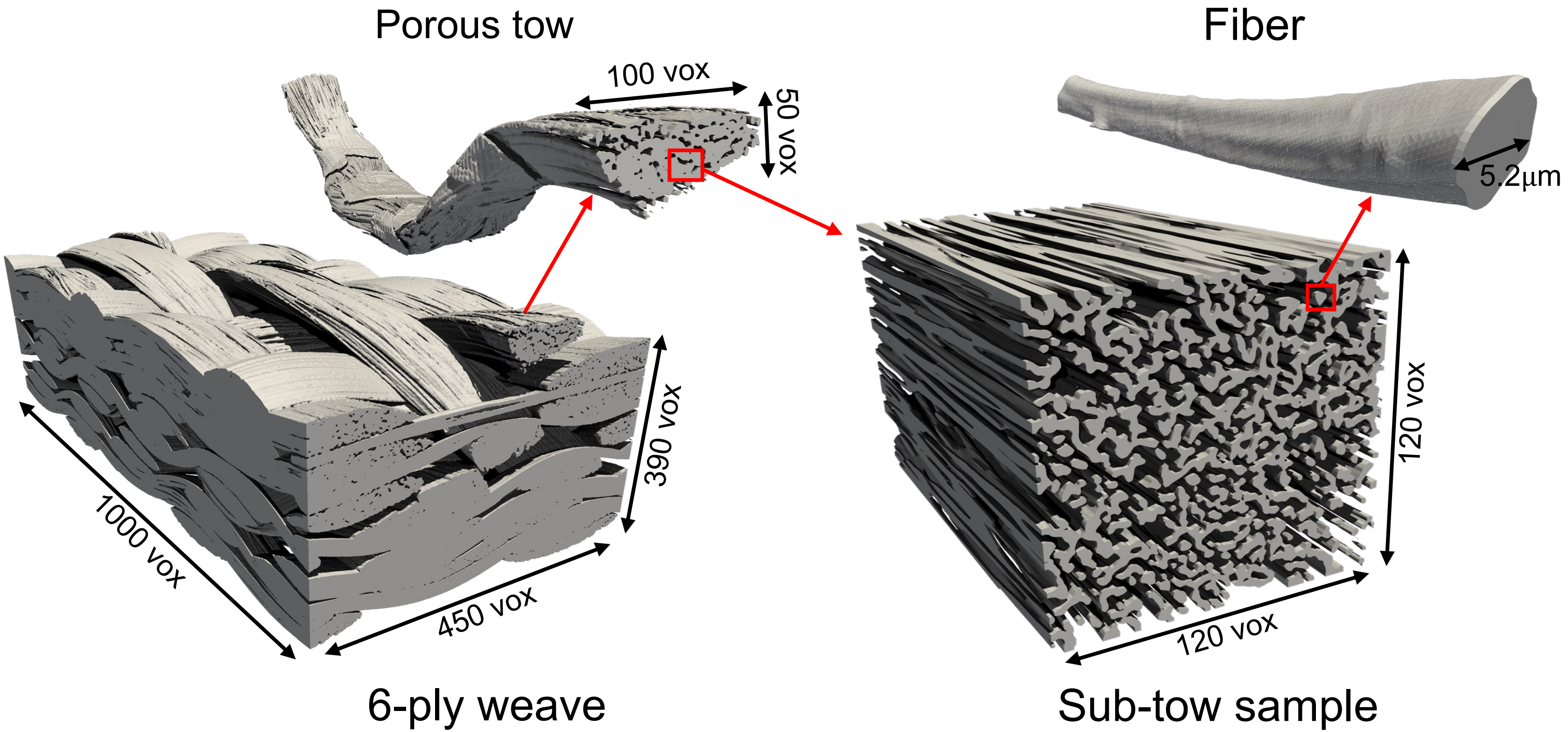
Optimization Toolbox

Material Properties



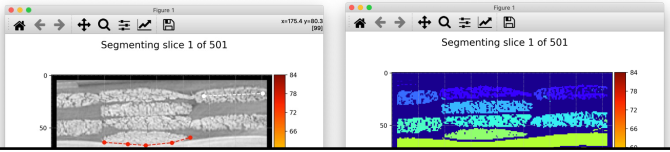
Update Geometry

Micro-CT Weaves: Anisotropic at Multiple Scales

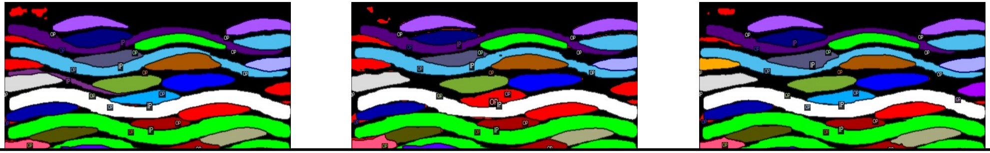


Weave Segmentation and Tow Tracking

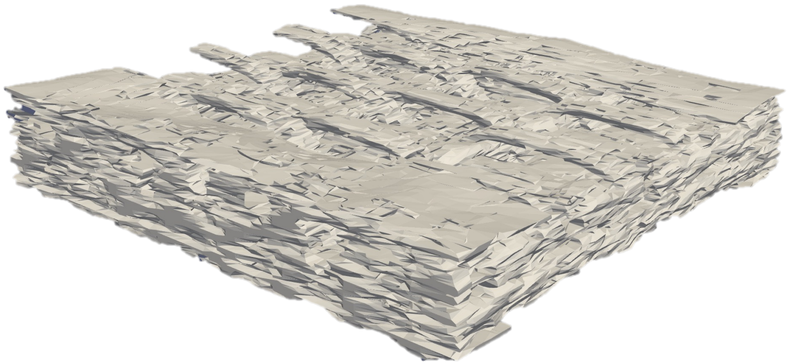
Manual labeling



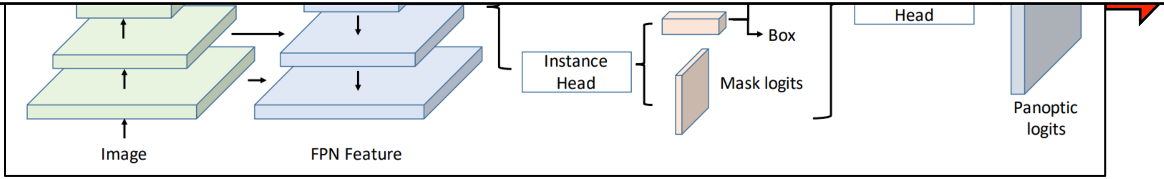
Tracking by IoU

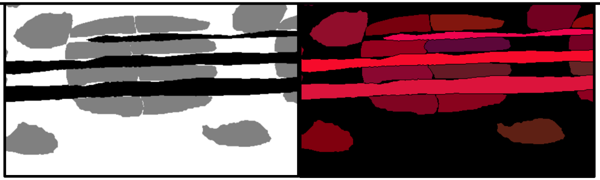


Naïve threshold of original Micro-CT weave



Fully segmented weave





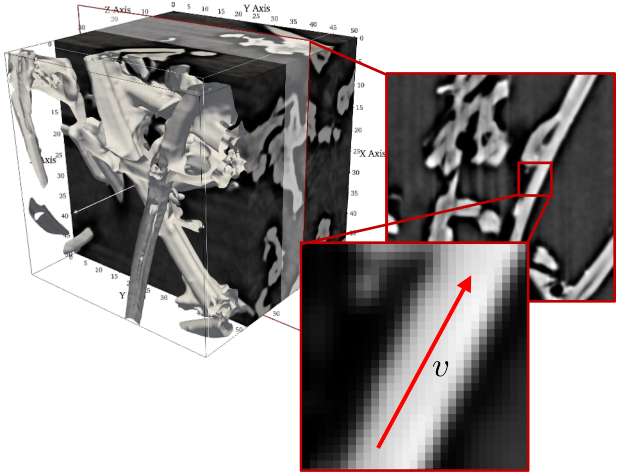
Semantic Classes

Instances

Allred, A., Abbott, L.J., Doostan, A., Maute, K. Automated processing of x-ray computed tomography images via panoptic segmentation for modeling woven composite textiles, *Composite Structures*

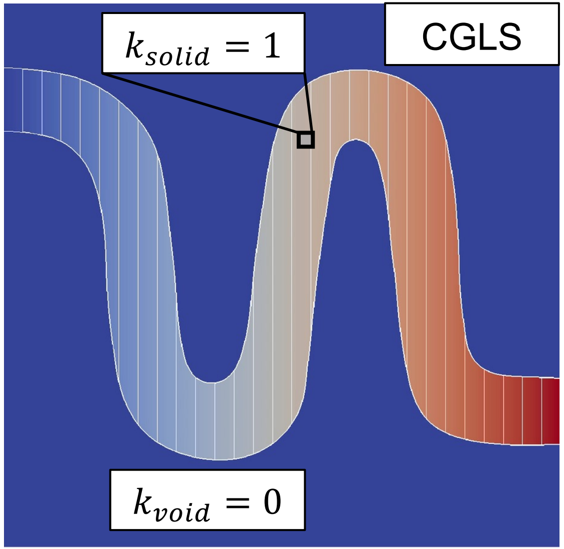
Orientation Methods

Structure tensor

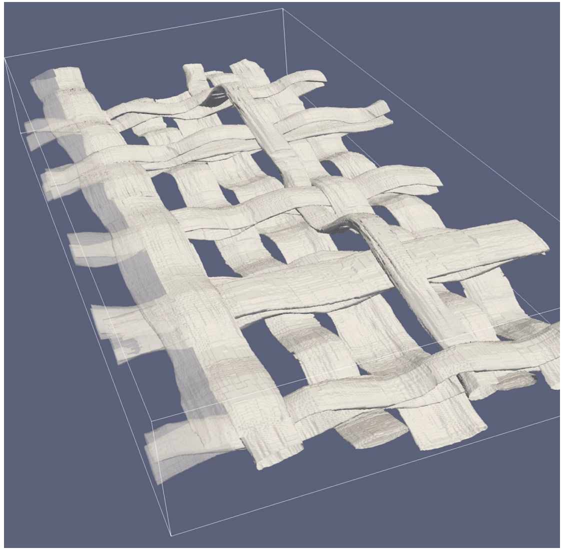


$$(I(x+v) - I(x))^2 \approx 0$$

Artificial flux



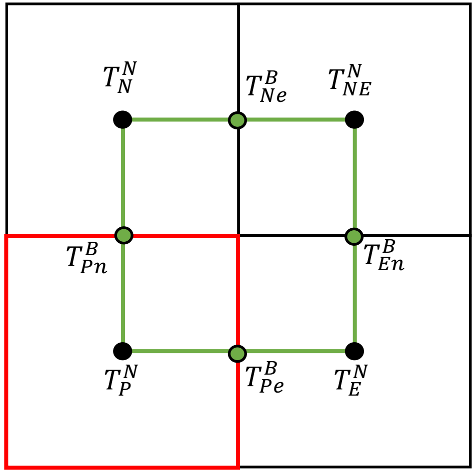
Ray casting



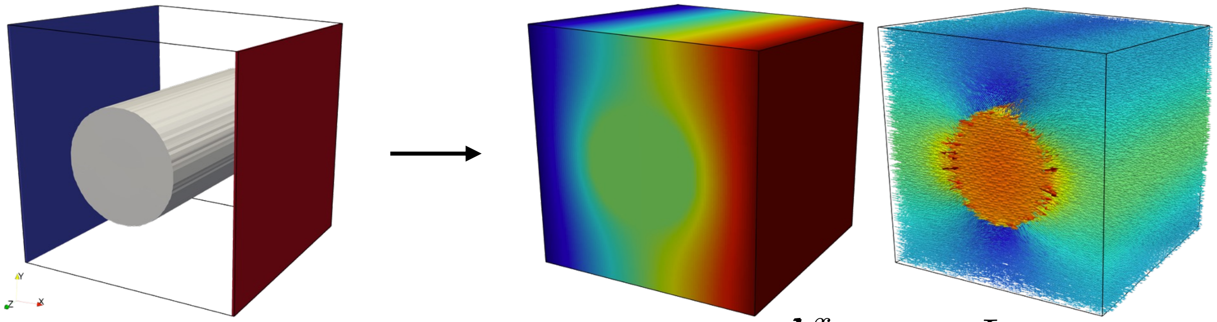
Semeraro, F., Ferguson, J.C., Panerai, F., King, R.J. and Mansour, N.N., 2020. Anisotropic analysis of fibrous and woven materials part 1: Estimation of local orientation. *Computational Materials Science*, *178*, p.109631.

Conductivity Solver

$$\nabla \cdot \boldsymbol{q} = 0 \quad \text{where} \quad \boldsymbol{q} = -\boldsymbol{k}\nabla T = -\begin{bmatrix} k^{xx} & k^{xy} & k^{xz} \\ k^{xy} & k^{yy} & k^{yz} \\ k^{xz} & k^{yz} & k^{zz} \end{bmatrix} \begin{pmatrix} \partial T/\partial x \\ \partial T/\partial y \\ \partial T/\partial z \end{pmatrix}$$



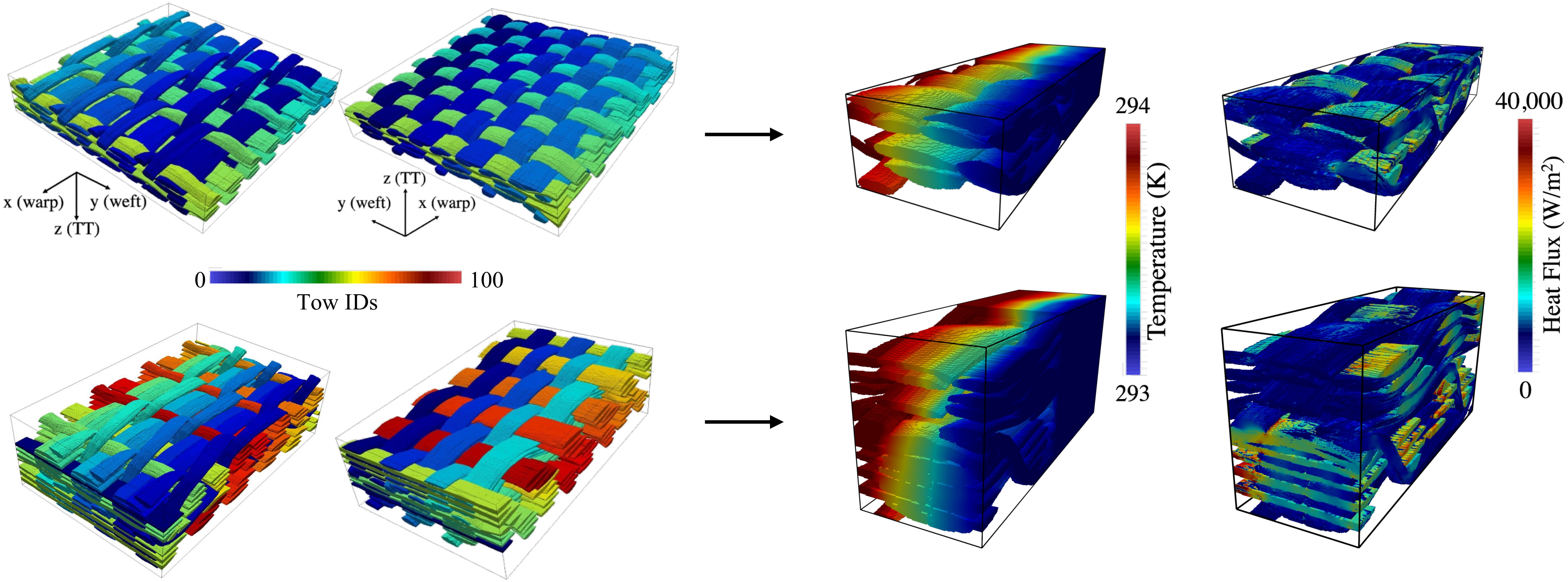
Multi-Point Flux Approximation (MPFA-O)*: $\boldsymbol{q} = \boldsymbol{E}\boldsymbol{T}^N$



$$\boldsymbol{k}^x = -\boldsymbol{q} \cdot L_x$$

*Ivar Aavatsmark. Multipoint flux approximation methods for quadrilateral grids. *9th International forum on reservoir simulation 2007*, *Abu Dhabi*, pages 9–13.

Conductivity Solver Validation: ADEPT

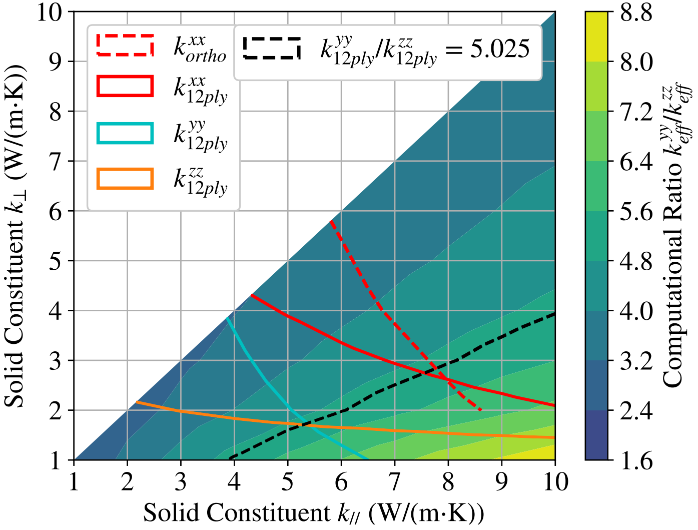


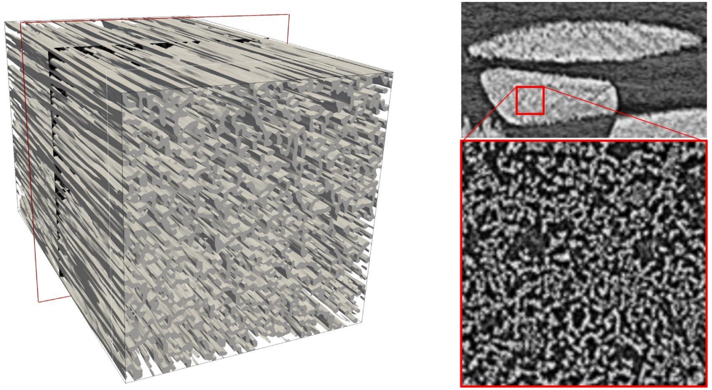
Semeraro, F., Ferguson, J.C., Acin, M., Panerai, F. and Mansour, N.N., 2021. Anisotropic analysis of fibrous and woven materials part 2: Computation of effective conductivity. Computational Materials Science, 186, p.109956.

Single Fiber Conductivity Estimation

Experimental value at room temperature:

$$\boldsymbol{k}_{exp}^{12ply} = \begin{bmatrix} 2.184 & - & - \\ - & 1.980 & - \\ - & - & 0.394 \end{bmatrix}$$





Single fiber thermal conductivity

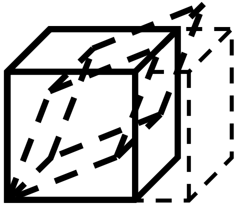
$$[k_{//}, k_{\perp}] = [9.7, 5.5]\frac{\text{W}}{\text{mK}}$$

$$\boldsymbol{k}_{num}^{12ply} = \begin{bmatrix} 2.310 & -0.414 & 0.000 \\ -0.524 & 2.030 & 0.071 \\ 0.007 & 0.050 & 0.504 \end{bmatrix}$$

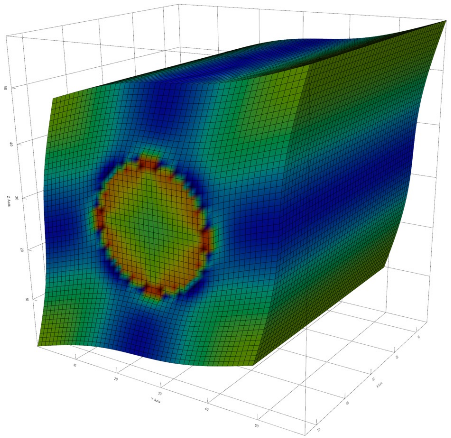
Elasticity Solver

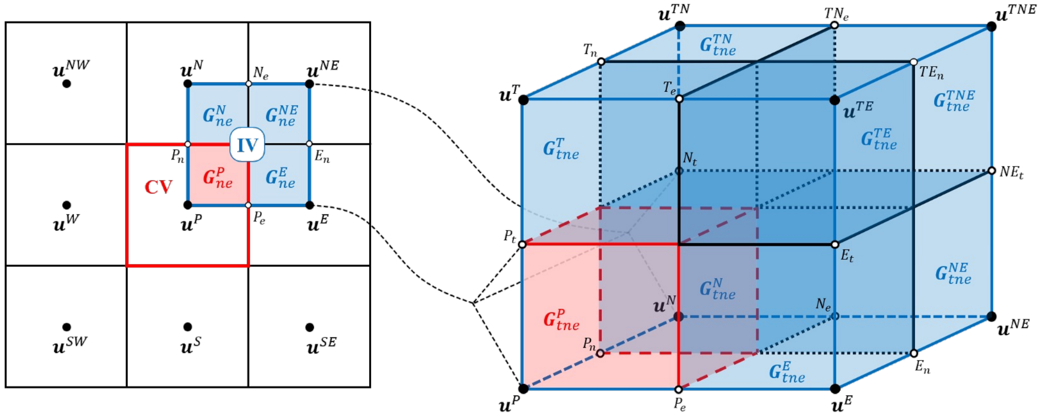
$$\nabla \cdot \boldsymbol{\sigma} = 0 \quad \text{where} \quad \boldsymbol{\sigma} = \boldsymbol{C\varepsilon} = \begin{bmatrix} C^{11} & C^{12} & C^{13} & C^{14} & C^{15} & C^{16} \\ C^{12} & C^{22} & C^{23} & C^{24} & C^{25} & C^{26} \\ C^{13} & C^{23} & C^{33} & C^{34} & C^{35} & C^{36} \\ C^{14} & C^{24} & C^{34} & C^{44} & C^{45} & C^{46} \\ C^{15} & C^{25} & C^{35} & C^{45} & C^{55} & C^{56} \\ C^{16} & C^{26} & C^{36} & C^{46} & C^{56} & C^{66} \end{bmatrix} \frac{\nabla \boldsymbol{u} + (\nabla \boldsymbol{u})^T}{2}$$

Multi-Point Stress Approximation (MPSA-W)*: $\boldsymbol{\sigma} = \boldsymbol{E}\,\boldsymbol{u}^N$



$$C^4 = \frac{2L_xL_y}{L_x + L_y}\boldsymbol{\sigma}$$



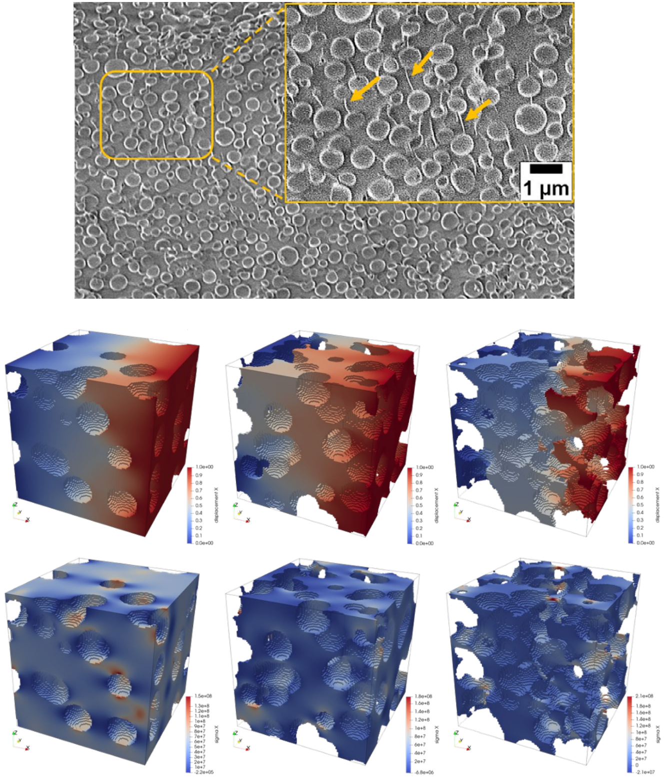


*Keilegavlen, E. and Nordbotten, J.M., 2017. Finite volume methods for elasticity with weak symmetry. Int. Journal for Numerical Methods in Engineering, 112(8), pp.939-962.

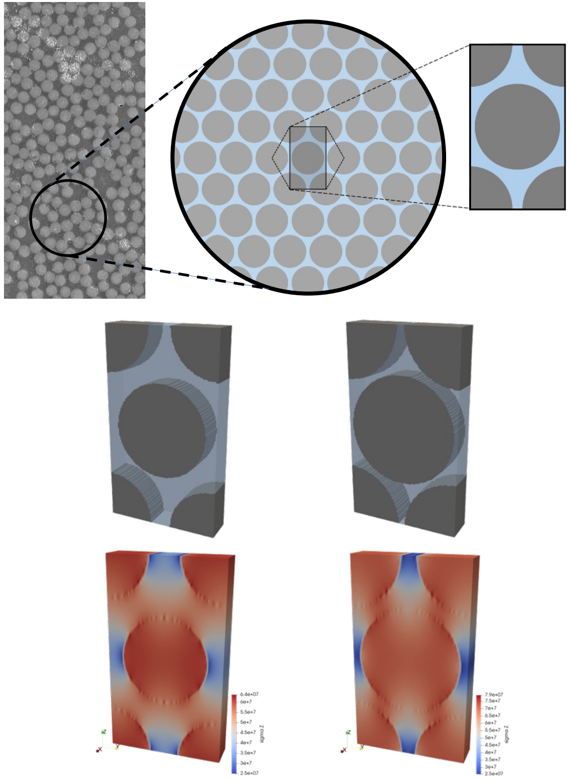
Elasticity Solver Validation: Woven Composite

Fraile Izquierdo, S., Semeraro, F., Acin, M., 2022. Multi-Scale Analysis of Effective Mechanical Properties of Porous 3D Woven Composite Materials. *AIAA Scitech Forum*

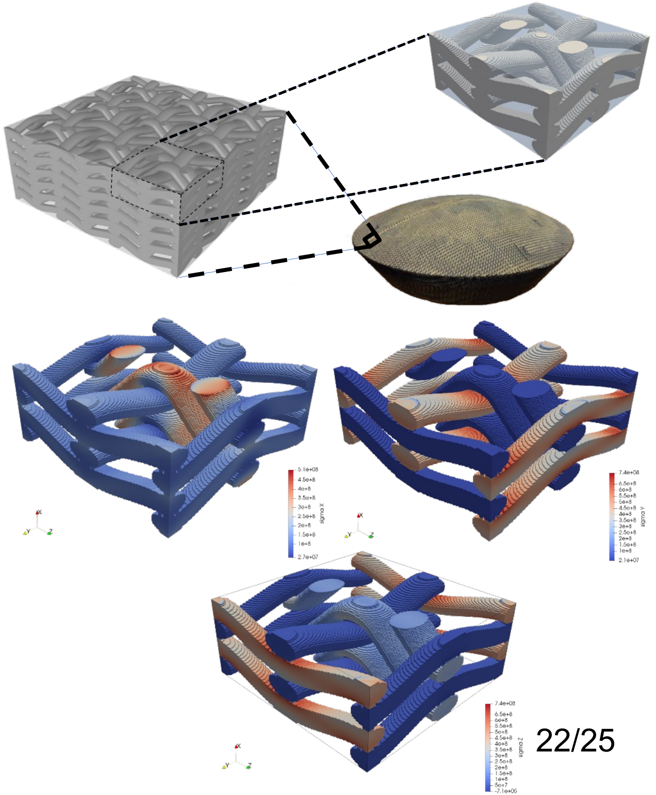
Matrix: porous phenolic resin



Intra-tow fiber packing

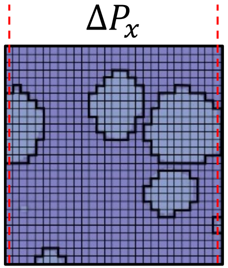


Woven unit cell

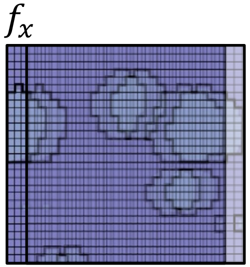


Permeability Solver

- Governing equation for Stokes flow (valid for slow creeping regimes, $Re \approx 0$):



$$-\mu \nabla^2 \boldsymbol{u} + \nabla p = \boldsymbol{f}$$

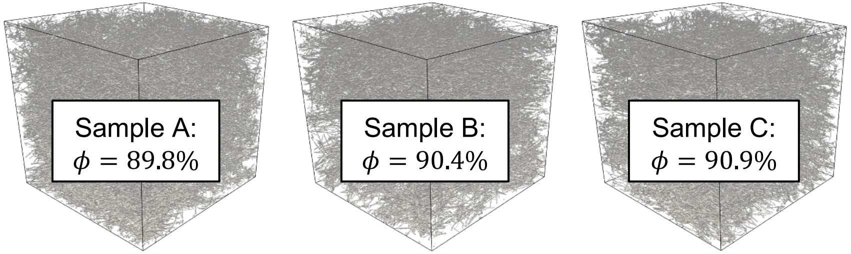


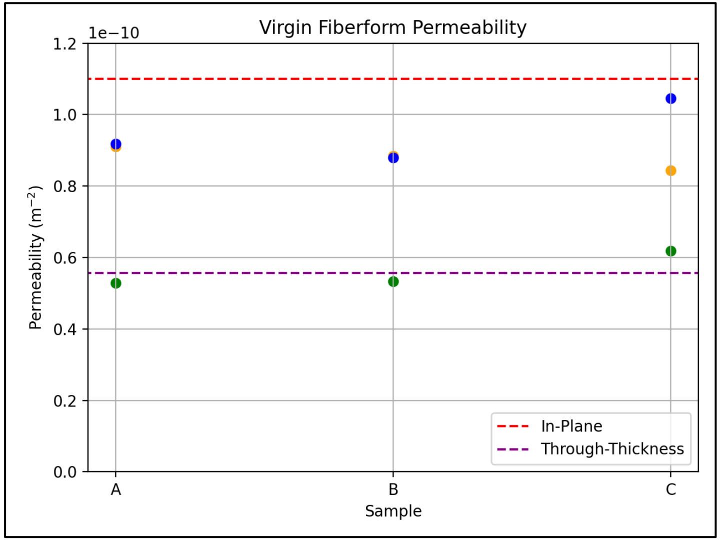
- Solved with Finite Element (FE) scheme with Q1-Q1 discretization in velocity and pressure (plus pressure stabilization) using Element-By-Element (EBE) technique
- By imposing a unit body force f_i in the three Cartesian directions, the permeability is homogenized as:

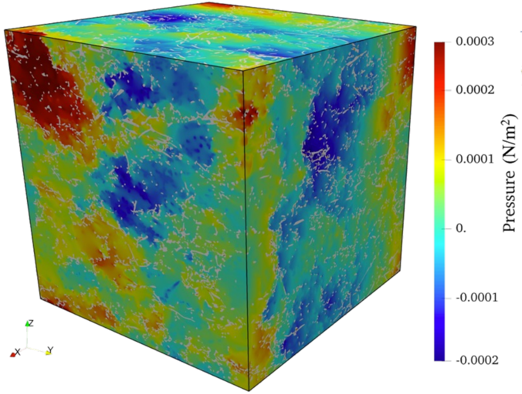
$$\begin{bmatrix} k^{xx} & k^{xy} & k^{xz} \\ k^{xy} & k^{yy} & k^{yz} \\ k^{xz} & k^{yz} & k^{zz} \end{bmatrix} = \frac{l^3}{|V|} \int^{V} u^i \, dV$$

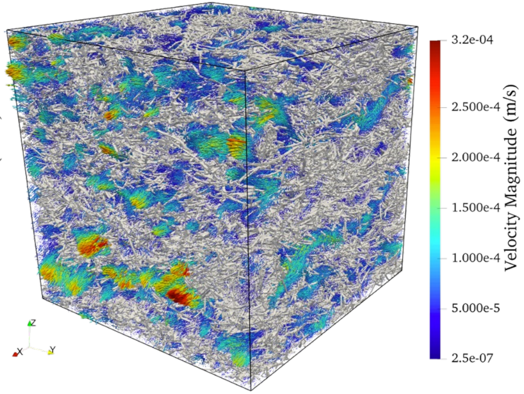
Permeability Validation: Fiberform

- Three 500^3 samples with voxel size = 2.6μm
- Run on NVIDIA V100 GPUs with matrix-free PCG









*Pedro C. F. Lopes, Rafael S. Vianna, Victor W. Sapucaia, Federico Semeraro, Ricardo Leiderman, and Andre M. B. Pereira. Simulation Toolkit for Digital Material Characterization of Large Image-based Microstructures. *npj Computational Materials* (under review)

Questions?