



Flutter Control



UNIVERSITY OF
MICHIGAN



Part 1: Control of Flexible Aircraft

Fuel Efficient Aircraft Design

- Breguet Range Equation

$$\text{Range} = V I_{sp} \frac{L}{D} \ln \left(\frac{m_{\text{takeoff}}}{m_{\text{landing}}} \right)$$

- Improve fuel efficiency by
 - Improving engine efficiency
 - Reducing drag with longer, more slender wings (high aspect ratio)
 - Reducing structural mass

Fuel Efficient Aircraft Design

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 - Improving engine efficiency
 - Reducing drag with longer, more slender wings (high aspect ratio)
 - Reducing structural mass
- Adverse effects
 - Increased coupling of structural dynamics and rigid body motion
 - Increased coupling of aerodynamic loads and structural deformation
 - Reduced flutter margins

Flutter



Source: NASA Dryden Flight Research

Flight Demonstrators

Lockheed Martin/AFRL: Body Freedom Flutter (BFF)

Ref: Burnett, et al. AIAA 2010;
Holm-Hansen, et al. AUVSI 2010.



Flutter Free FLight Envelope eXpansion for ecOnomical Performance improvement
Ref: <https://flexop.eu/>, PI: B. Vanek



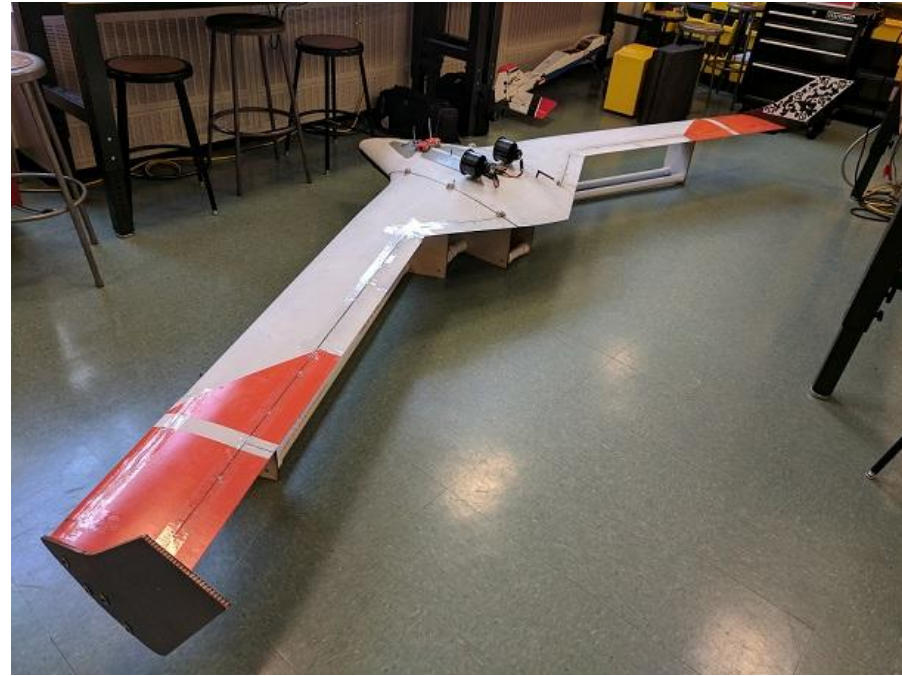
NASA/Lockheed Martin: X-56A
Multi-Utility Tech. Testbed (MUTT)
Ref: Schaefer, ACGSC 2018.

Performance Adaptive Aeroelastic Wing (PAAW)

- **Goal:** Suppress flutter, control wing shape and alter shape to optimize performance
 - Funding: NASA NRA with Dr. Jeffrey Ouellette as Tech. Monitor
 - Team: UMN, VT, STI, CMSOft, Aurora, Schmidt & Assoc.

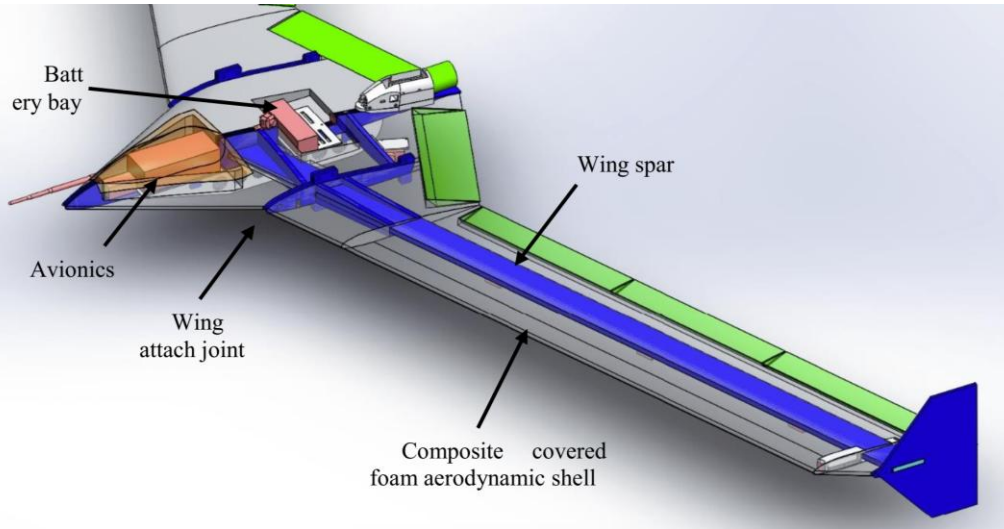


mAEWing1: BFF Replica
10ft wingspan, 14lbs



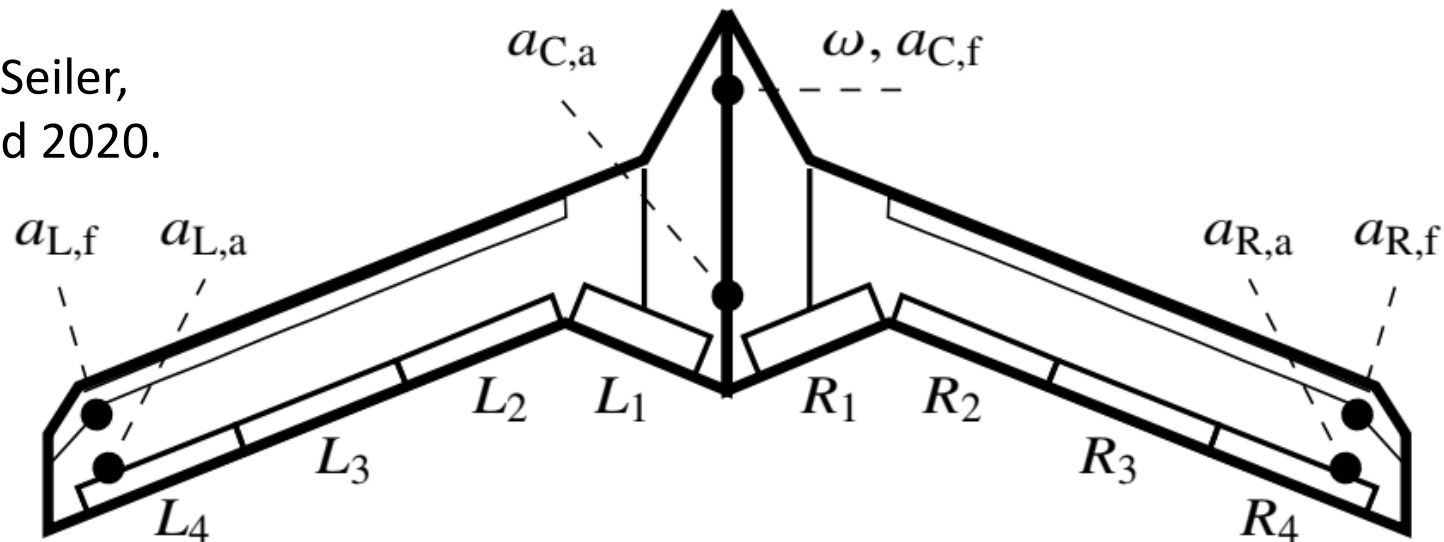
mAEWing2: Half-scale X-56A
14ft wingspan, 42lbs

mAEWing1 Sensor/Actuator Configuration

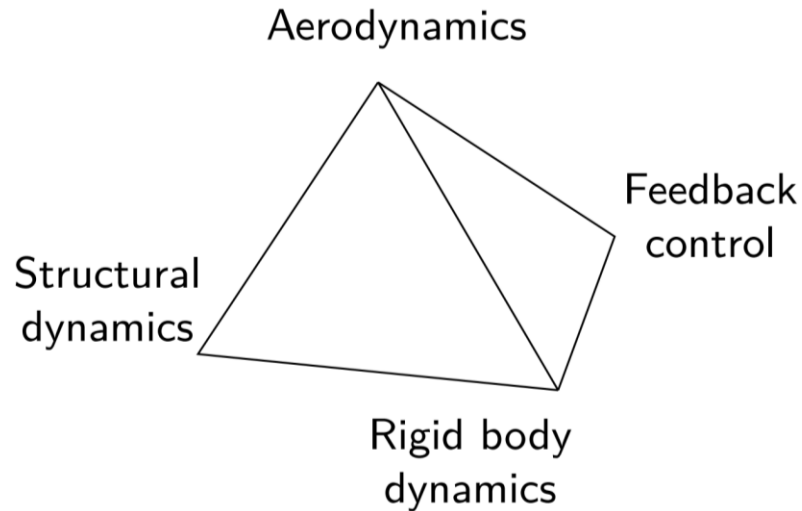


Ref: Regan & Taylor,
AIAA 2016-1747

Ref: Theis, Pfifer, & Seiler,
AIAA JGCD, accepted 2020.



Modeling for Aeroservoelastic Systems



[Cooper & Wright 2015; Collar 1946]

A variety of models are required at different levels of fidelity for flutter analysis, control design, etc.

Lower
Fidelity

Higher
Fidelity



Flight
Dynamics
(Schmidt)

Control-oriented
Panel Code
(UMN/Gupta)

IO Reduced-
Order Model
(STI/CMSOft)

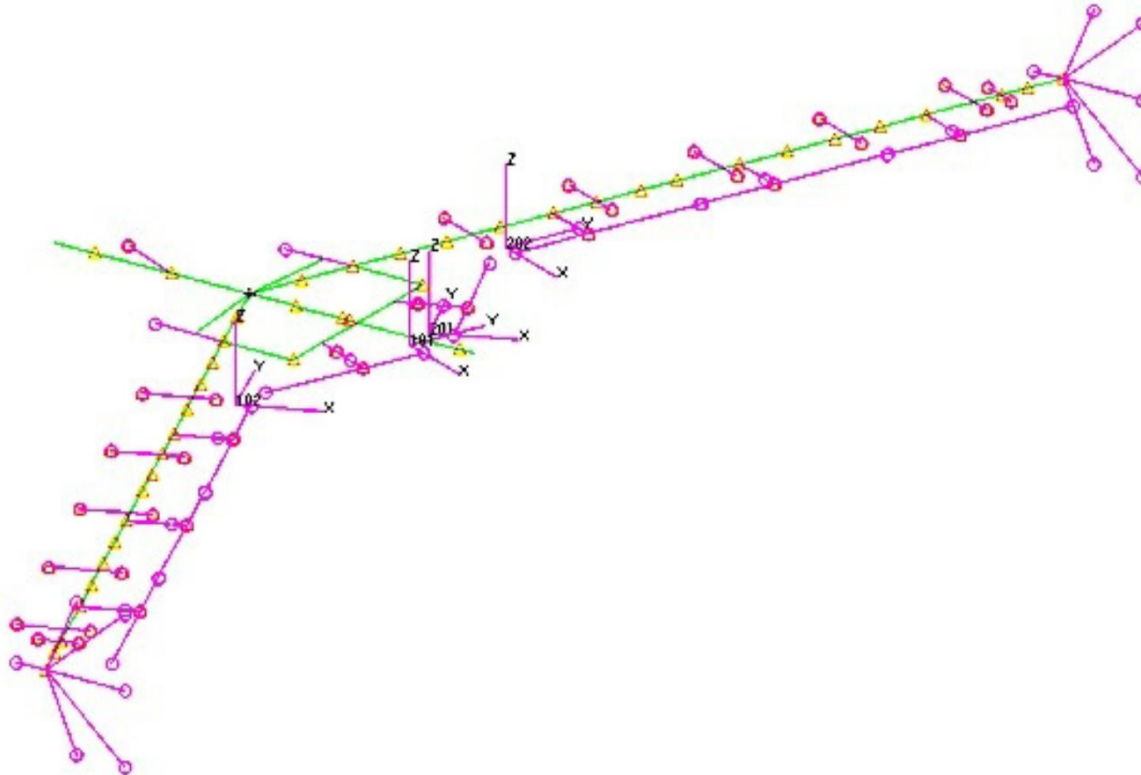
NASTRAN
(VT)

CFD/CSD
(CMSOft)

Control-Oriented Modeling

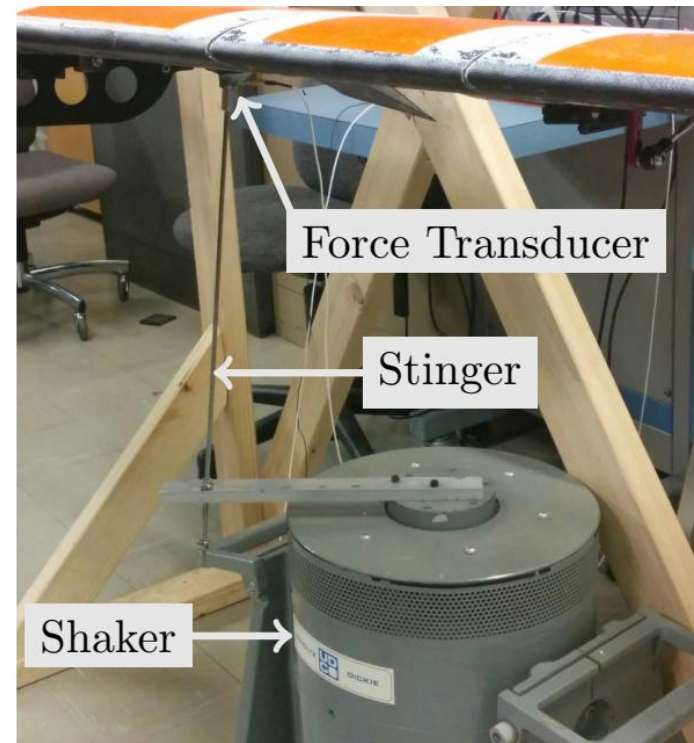
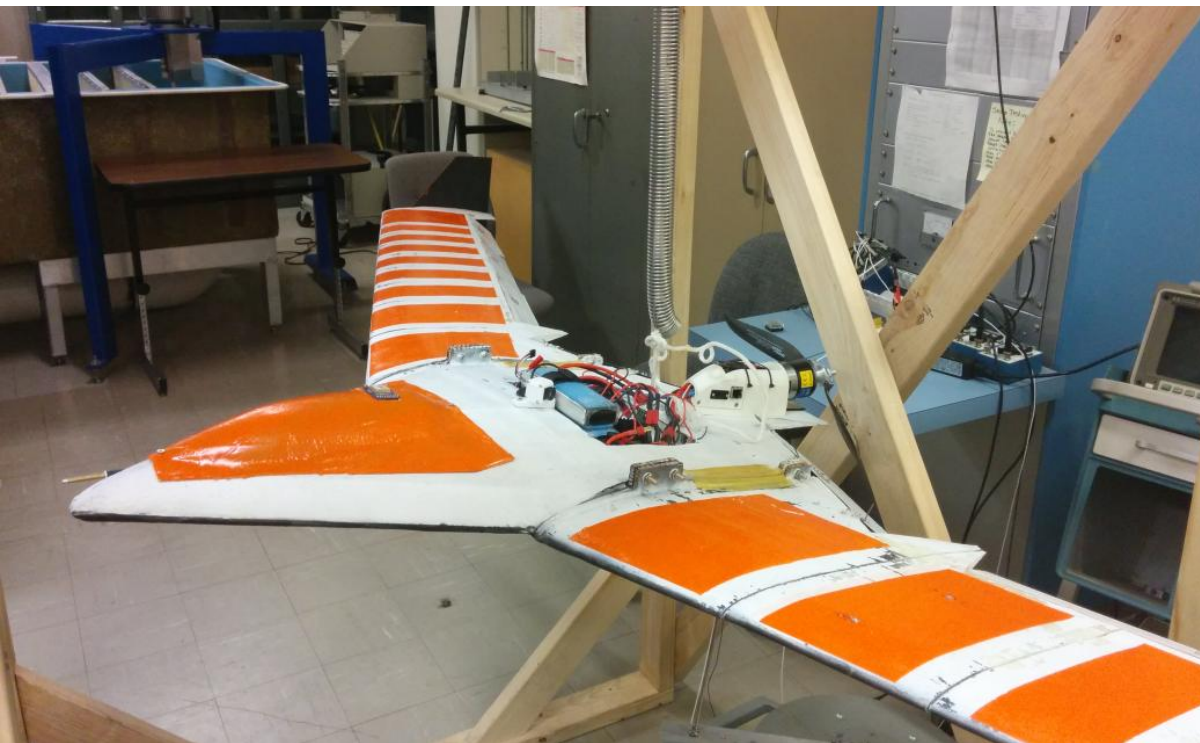
1. VT: Construct MSC NASTRAN model

- Ref: Schmidt, Zhao, Kapania, AIAA 2016-1748
- Finite-element model with rod / beam elements & unsteady aerodynamic model with double lattice.
- Initial model from CAD and simple static test data from UMN



Control-Oriented Modeling

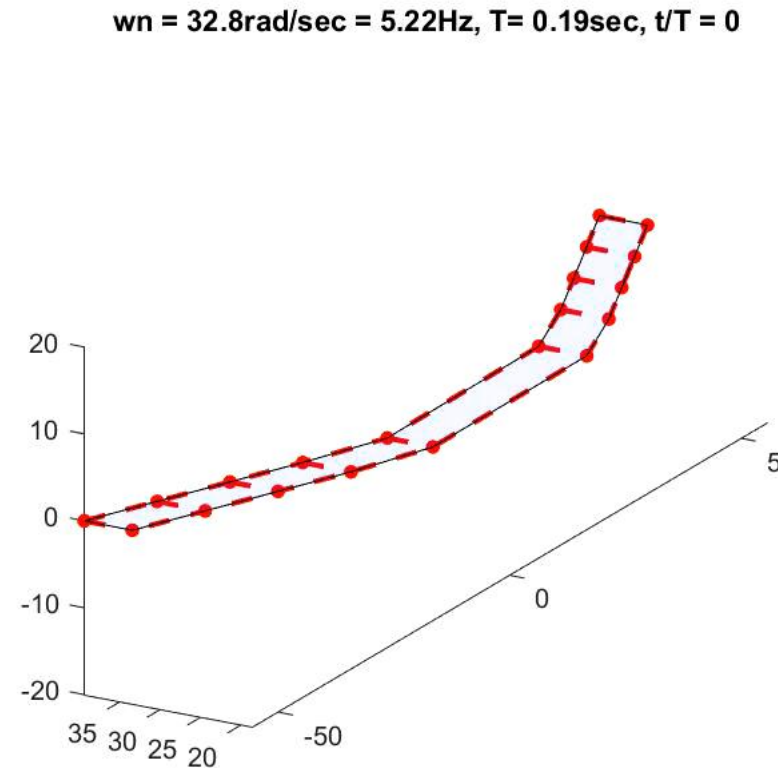
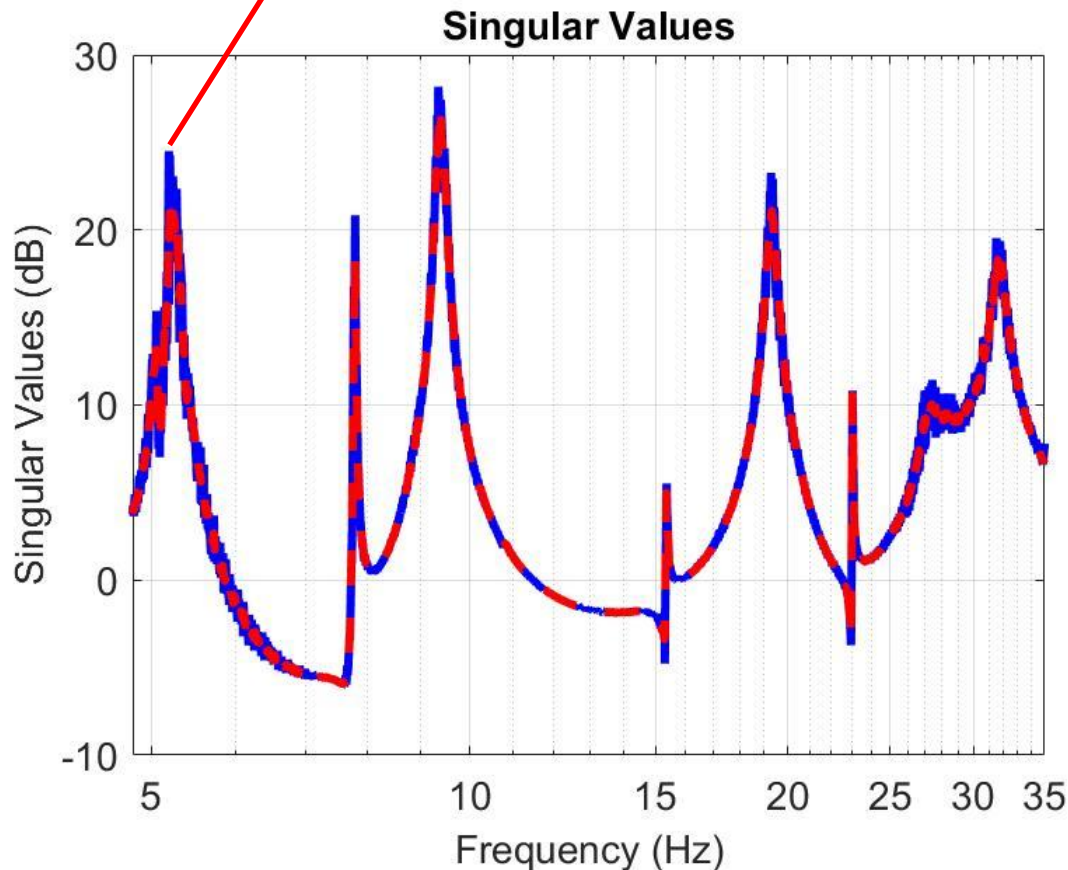
1. VT: Construct MSC NASTRAN model
2. VT/UMN: Update NASTRAN FEM with ground test data
 - Ref: Gupta, Seiler, Danowsky, AIAA 2016-1753
 - Matlab Demo: “Modal Analysis of a Flexible Flying Wing Aircraft”, Demonstrates frequency domain fitting in System ID Toolbox



Control-Oriented Modeling

1. VT: Construct MSC NASTRAN model
2. VT/UMN: Update NASTRAN FEM with ground test data

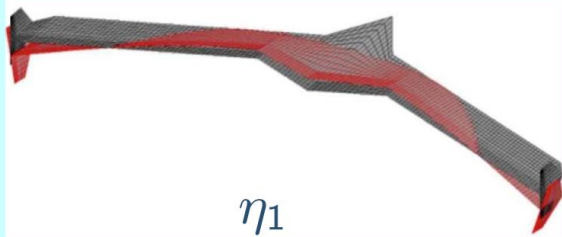
First structural mode at $33.6\text{rad/sec} \approx 5.4\text{Hz}$



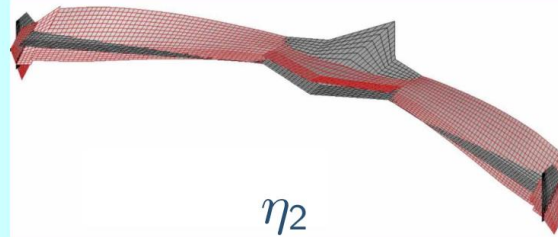
Control-Oriented Modeling

1. VT: Construct MSC NASTRAN model
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3. VT: Obtain mode shapes & frequencies from NASTRAN
 - Ref: Schmidt, Zhao, Kapania, AIAA 2016-1748

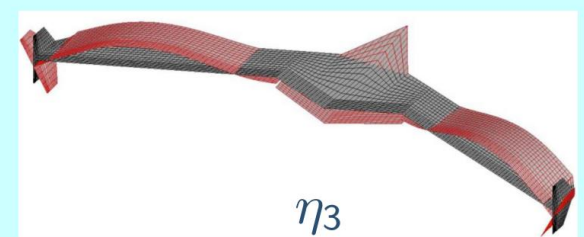
Structural modes [Schmidt et al 2016 AIAA]



*Symmetric 1st
Bending ~5-6Hz*



*Symmetric 1st
Torsion ~12Hz*



*Symmetric 2nd
Bending ~19.5Hz*

Control-Oriented Modeling

1. VT: Construct MSC NASTRAN model
2. VT/UMN: Update NASTRAN FEM with ground test data
3. VT: Obtain mode shapes & frequencies from NASTRAN
4. Schmidt: Construct low-order flight dynamics model
 - Ref: Schmidt, Zhao, Kapania, AIAA 2016-1748
 - Ref: Schmidt, Journal of Aircraft, 2016.
 - Parameter-varying model constructed using mean-axes

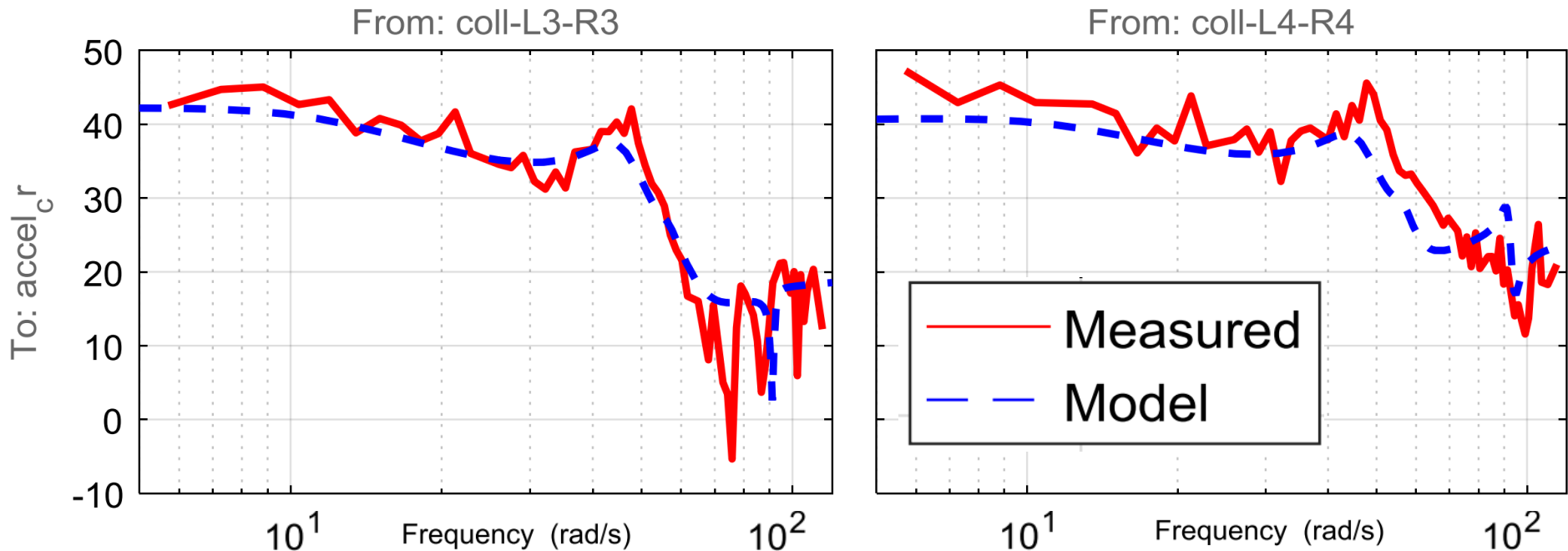
Model has longitudinal rigid body dyn. & three elastic modes

$$\begin{aligned}\dot{x} &= A(V_\infty)x + B(V_\infty)u \\ y &= C(V_\infty)x + D(V_\infty)u\end{aligned}$$

where $x = [u \ \alpha \ \theta \ q \mid \eta_1 \ \dot{\eta}_1 \ \eta_2 \ \dot{\eta}_2 \ \eta_3 \ \dot{\eta}_3]^T$

Control-Oriented Modeling

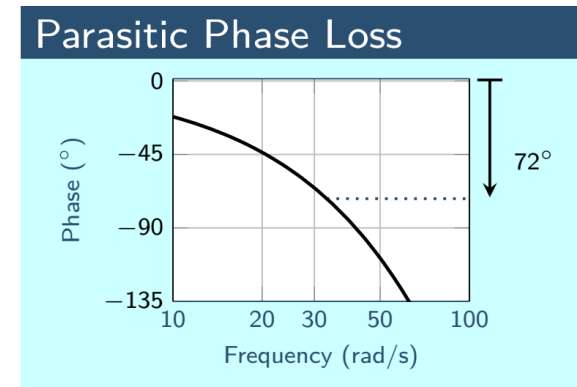
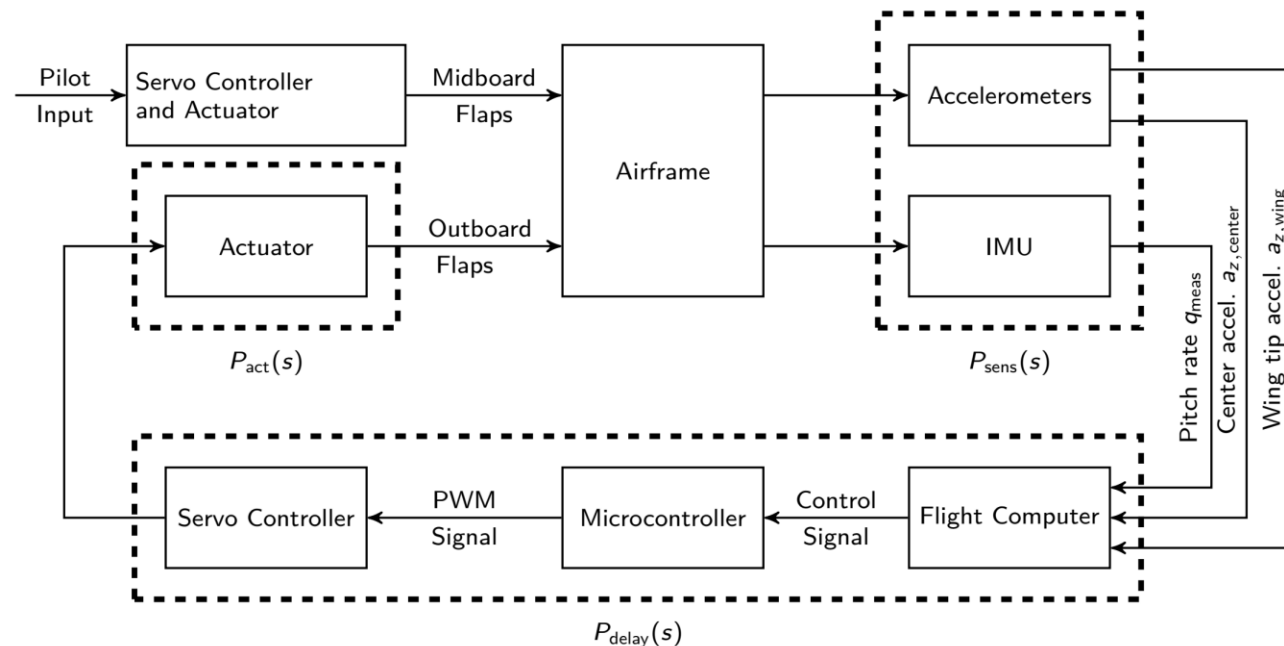
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3. VT: Obtain mode shapes & frequencies from NASTRAN
4. Schmidt: Construct low-order flight dynamics model
5. STI/UMN/Schmidt: Grey-box ID from flight tests
 - Ref: Danowsky, Schmidt, Pfifer, AIAA 2017-1394



Bode mag (dB) from symmetric L3/R3 and L4/R4 to center body accel

Control-Oriented Modeling

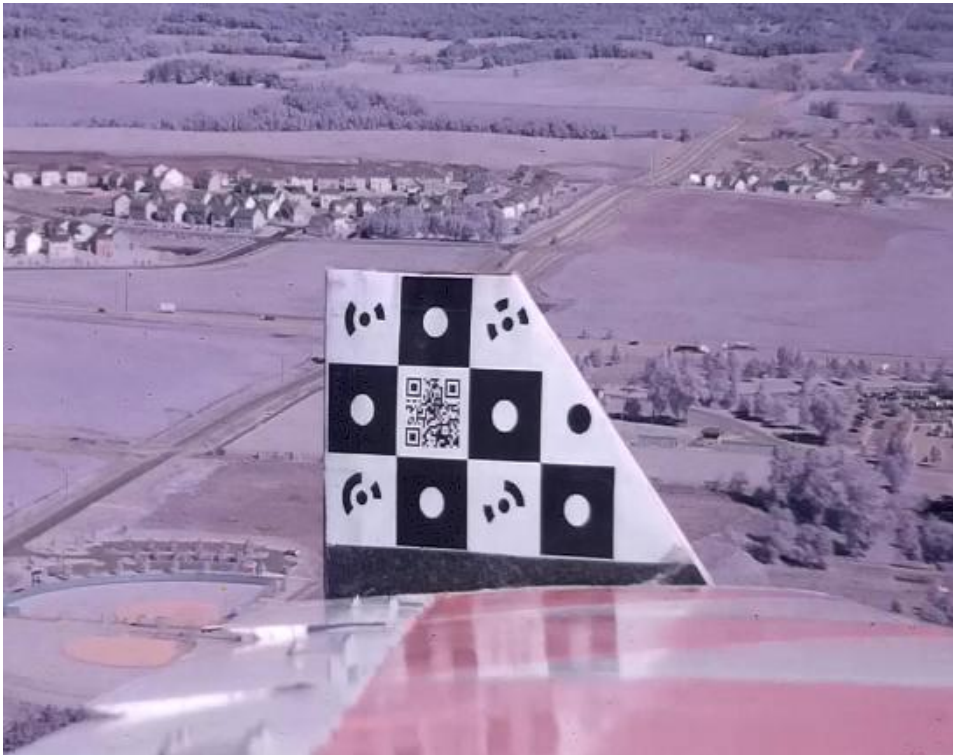
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4. Schmidt: Construct low-order flight dynamics model
5. STI/UMN/Schmidt: Grey-box ID from flight tests
6. UMN: Component Modeling
 - Ref: Theis, Pfifer, Seiler, AIAA 2016-1751



Open-Loop Flutter at $\sim 30\text{m/s}$

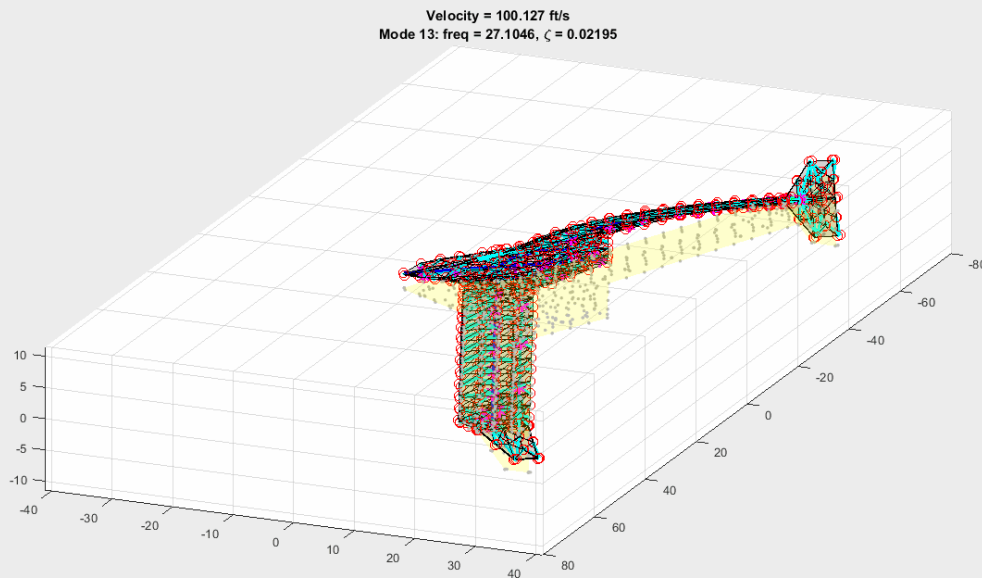
Model Predictions:

- Flight Dynamics (Schmidt): 29.1 m/s
- NASTRAN (VT): 29.5 m/s
- CFD/CSD (CMSOft): 30.8 m/s
- Input/Output Reduced Order Model (STI/CMSOft): 31.7m/s



Open-Loop Flutter at $\sim 30\text{m/s}$

Mode Shape: Coupling of rigid body short period and 1st symmetric wing bending.



Mode shape from IOROM

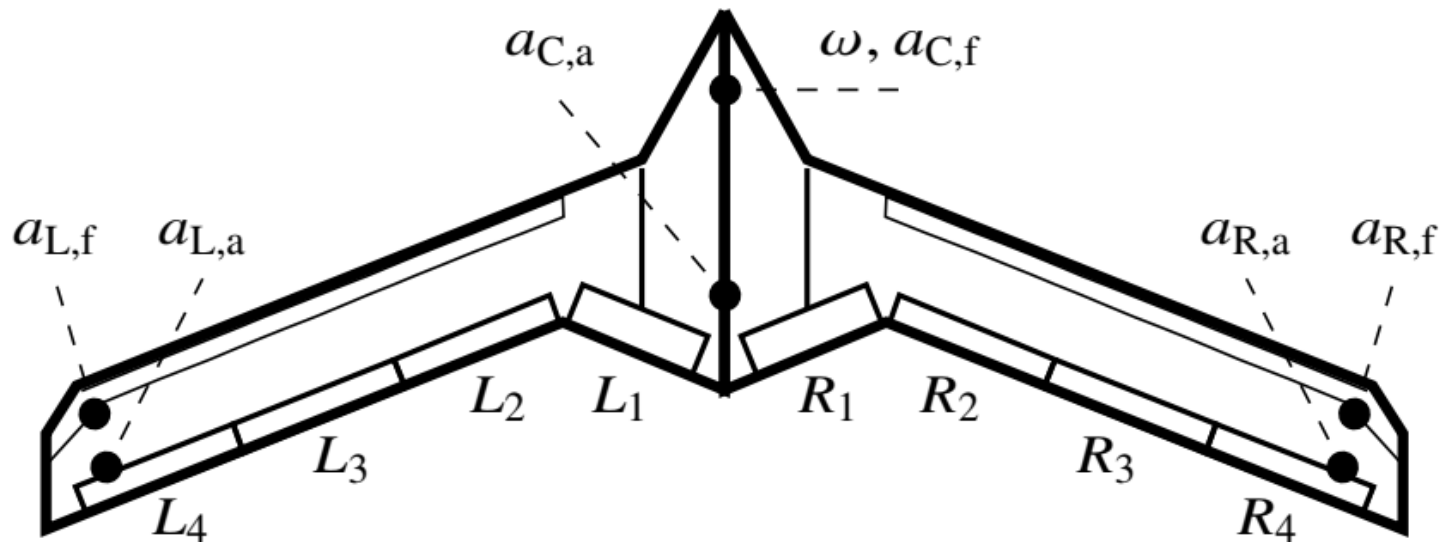


Active Flutter Suppression

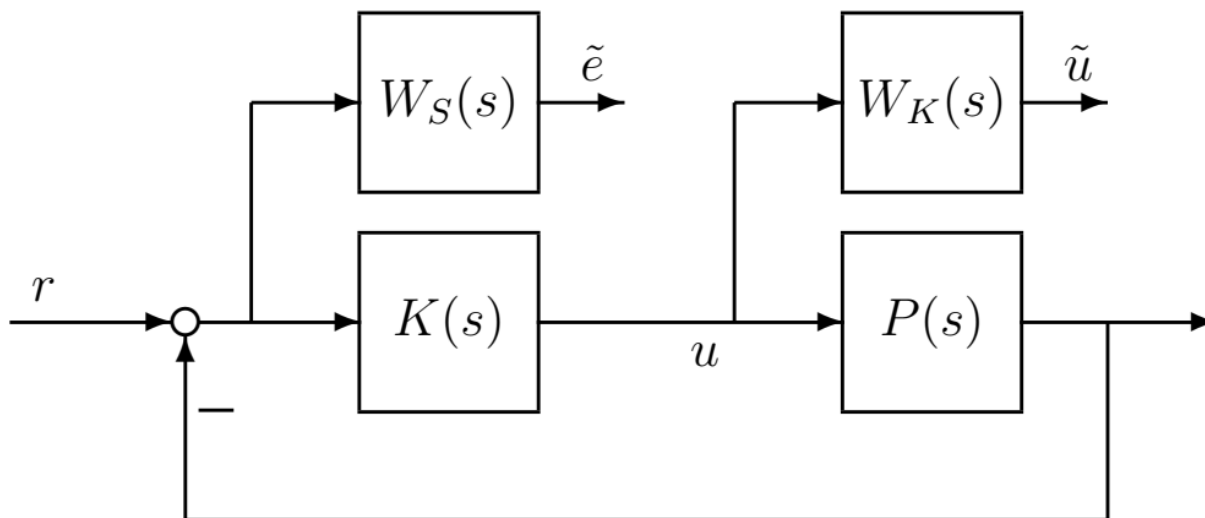
Design Objectives:

1. Maximize damping (or 1' closed-loop flutter speed.)
2. Remain within actuator position/rate limits
3. Minimal interference with rigid-body autopilot
4. Robustness to model uncertainties

Approach: H_∞ Optimal Control with L1/R1/L4/R4 surfaces.



Brief Summary of H_∞ Optimal Control

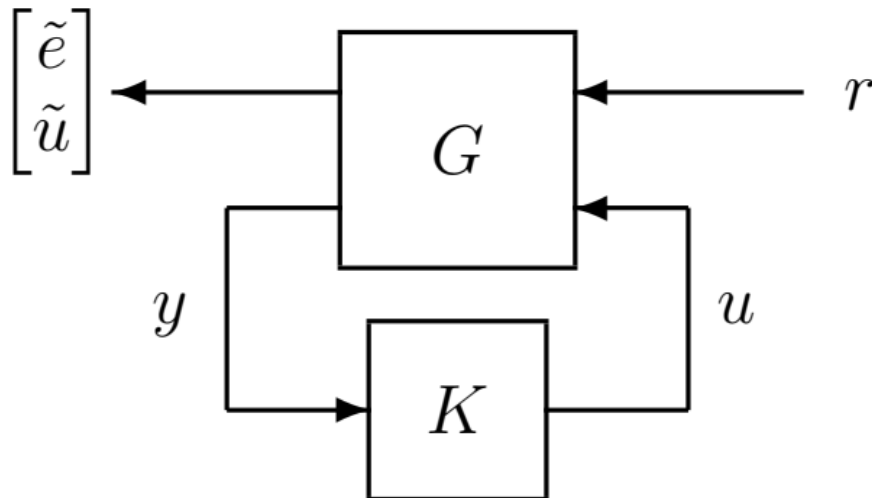
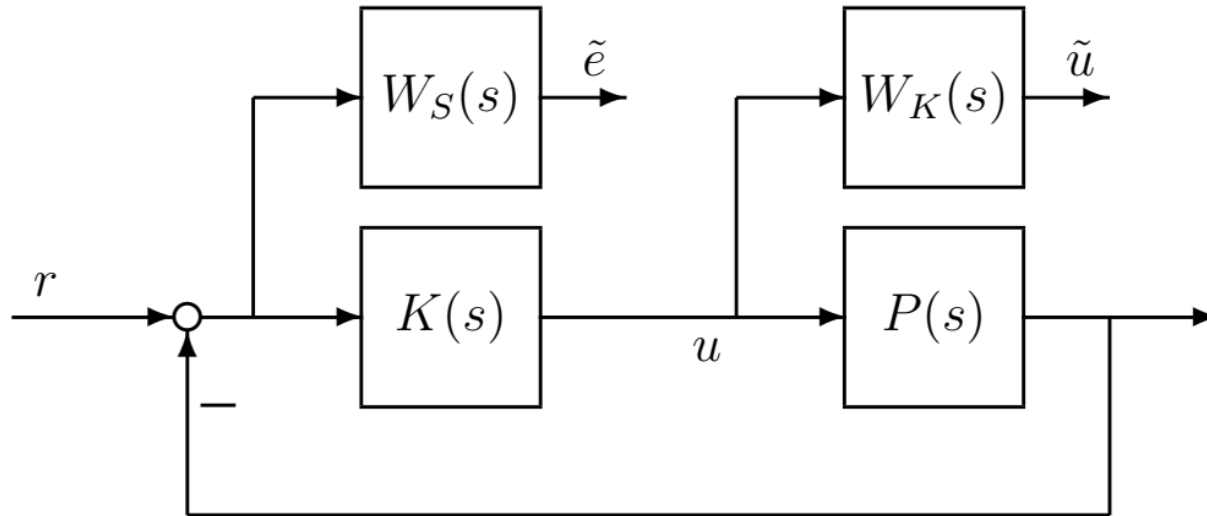


Goal (SISO): Find K to stabilize P and minimize

$$\sup_{\omega} |W_S(j\omega)S(j\omega)|^2 + |W_K(j\omega)K(j\omega)S(j\omega)|^2$$

Weights W_S and W_K selected to specify frequency-dependent tradeoffs.

Brief Summary of H_∞ Optimal Control

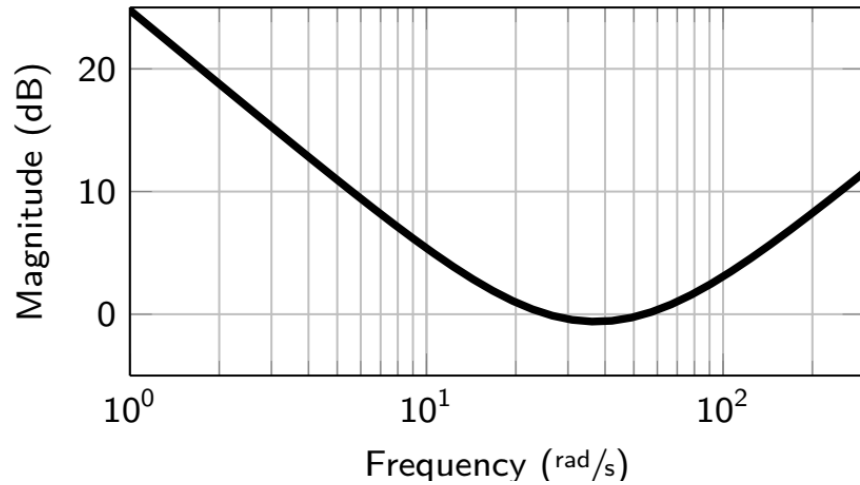


Goal: This is posed more generally as:

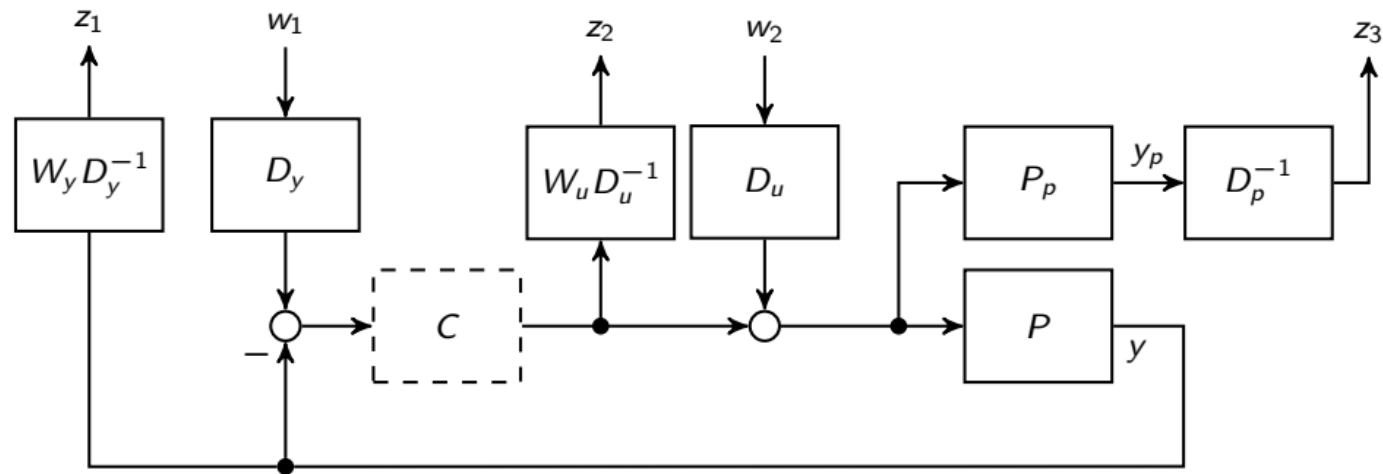
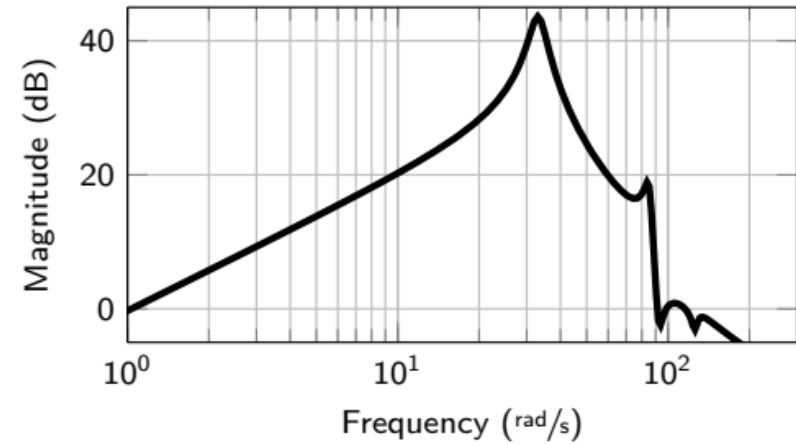
$$\inf_{K \text{ stabilizing}} \|F_L(G, K)\|_\infty$$

H_∞ for Active Flutter Suppression

Weight W_u for control effort



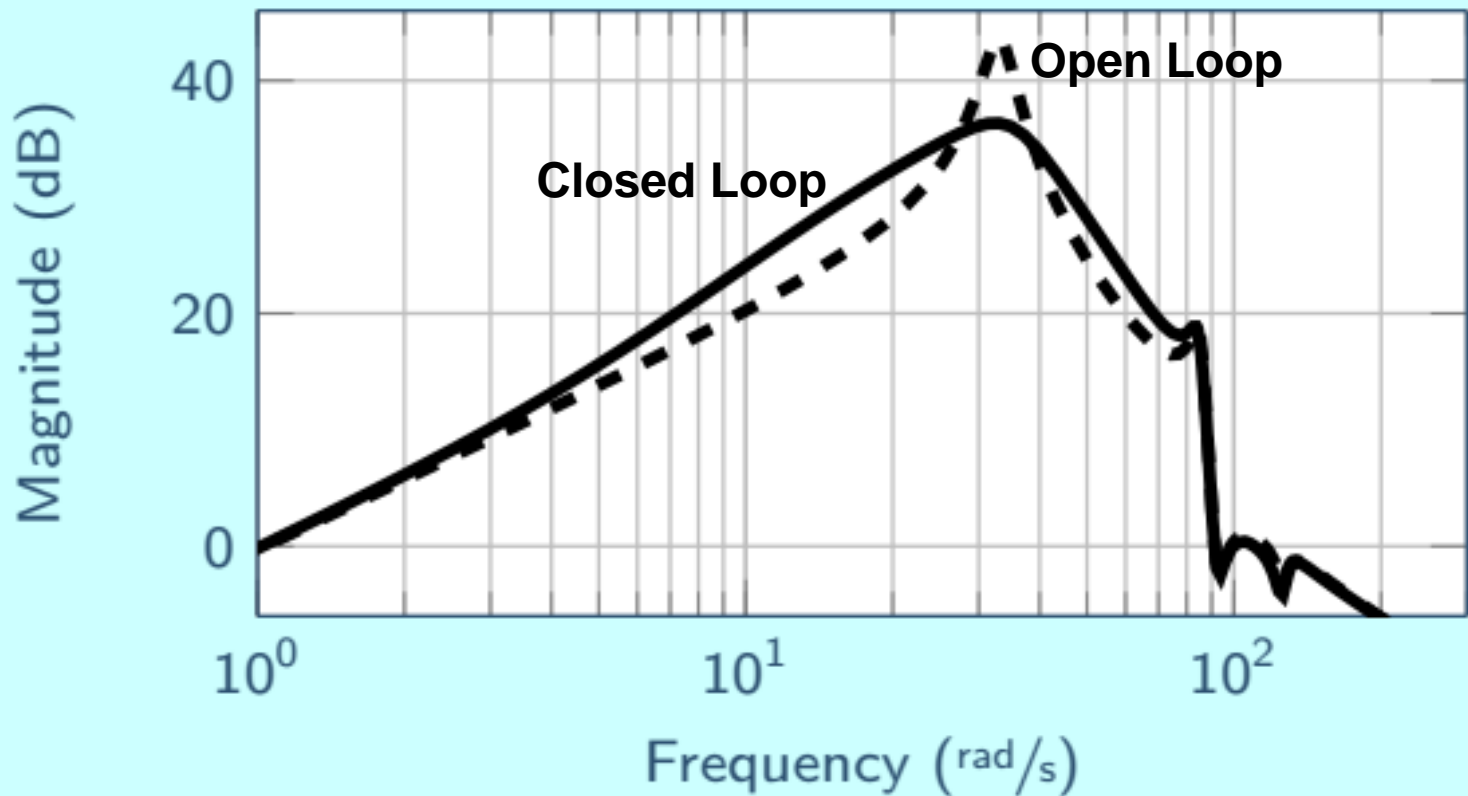
Model P_p for structural mode $\dot{\eta}_1$



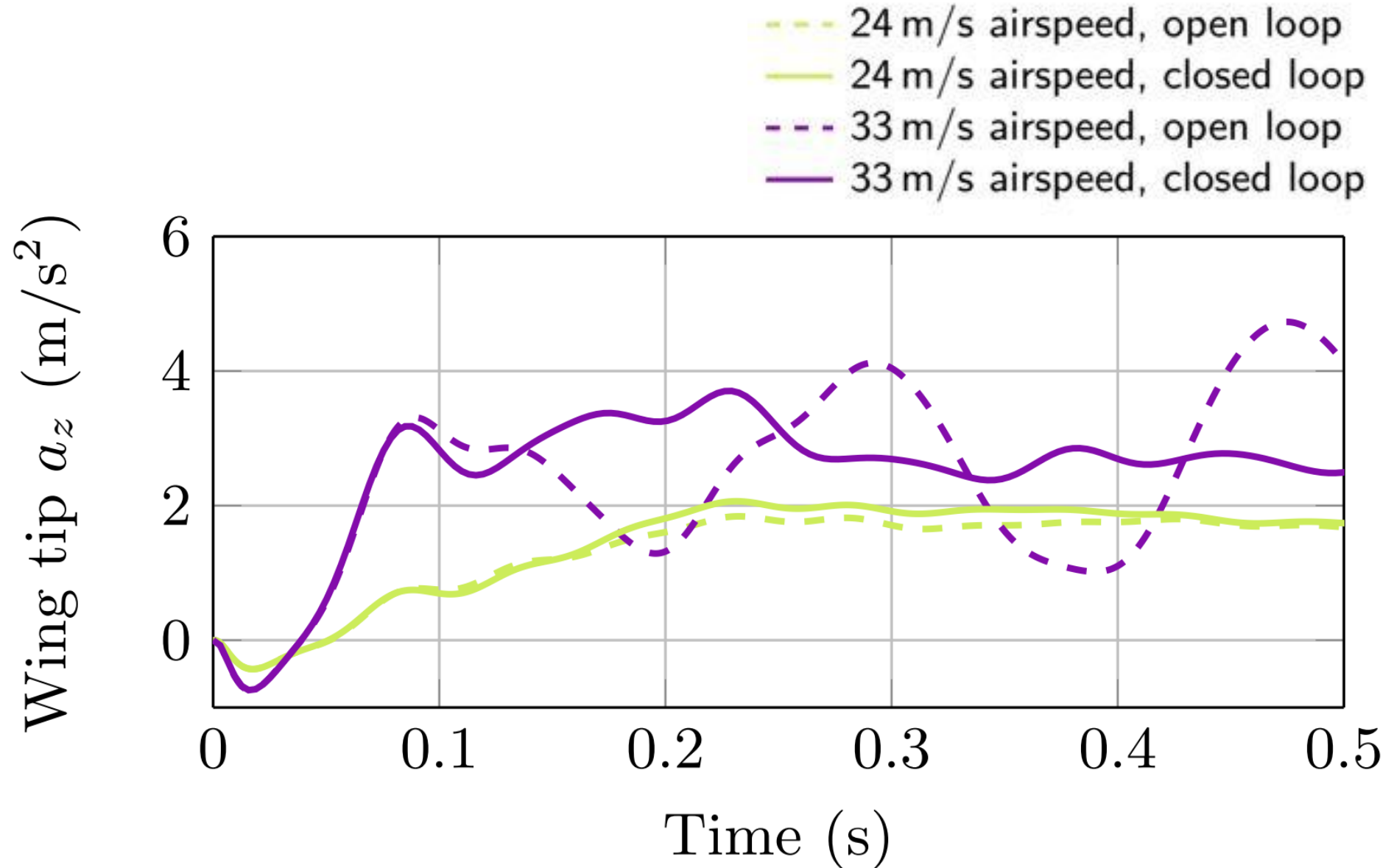
Refs: Theis, PhD 2018 & Theis, Pfifer, Seiler ('16 AIAA SciTech & JGCD)

Closed-Loop Performance

Structural Sensitivity ($P_p S_i$)



Closed-Loop Performance



Closed-Loop Flight Tests

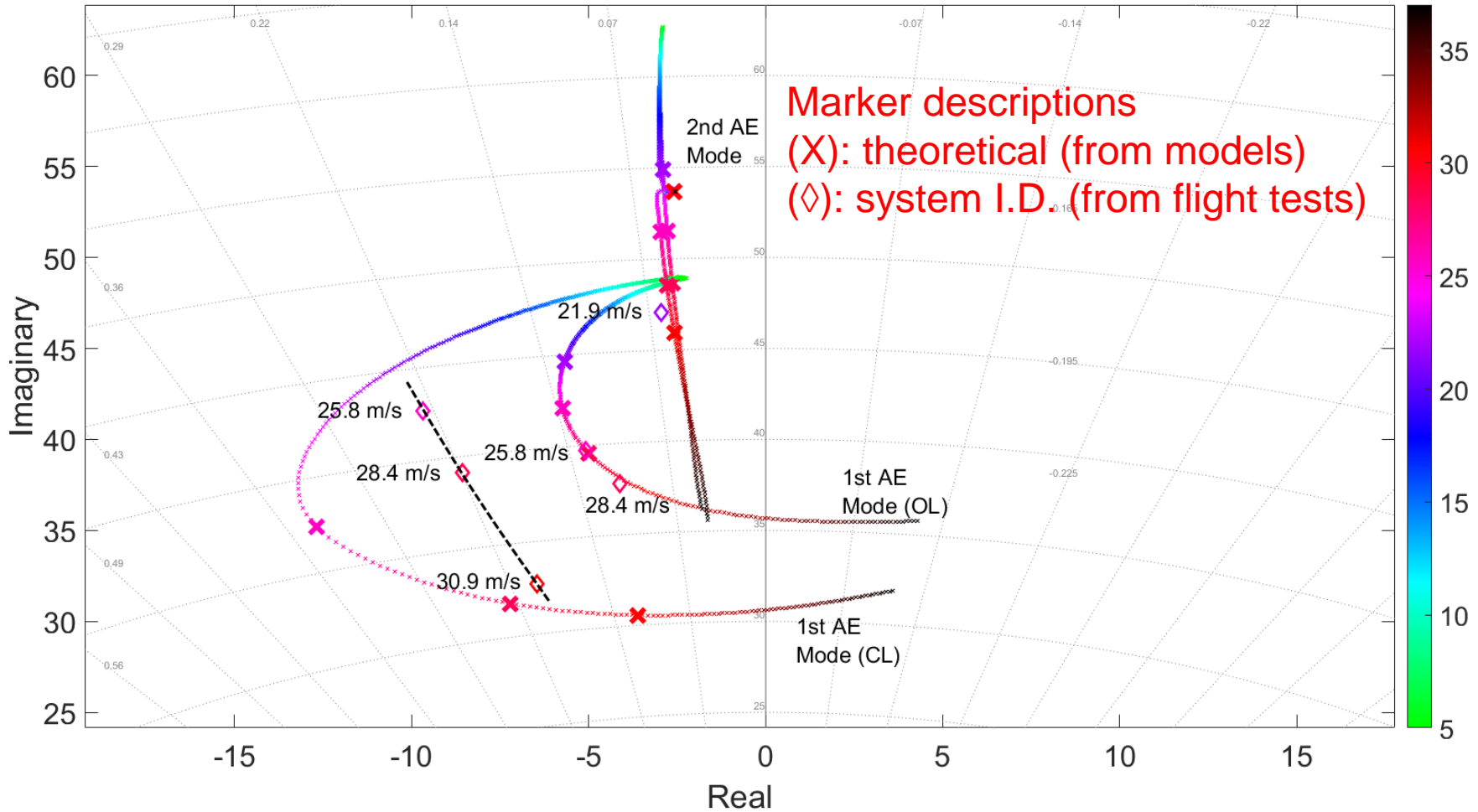
- Three controllers designed to increase damping to BFF mode at 23m/s.
 - Hinf Controller (Retuned): Kotikalpudi, et al, AIAA 2018-3426
 - MIDAAS: Danowsky (STI), 2017-4353
 - Classical Controller: Schmidt, Journal of GCD, 2016.

Closed-Loop Flight Tests

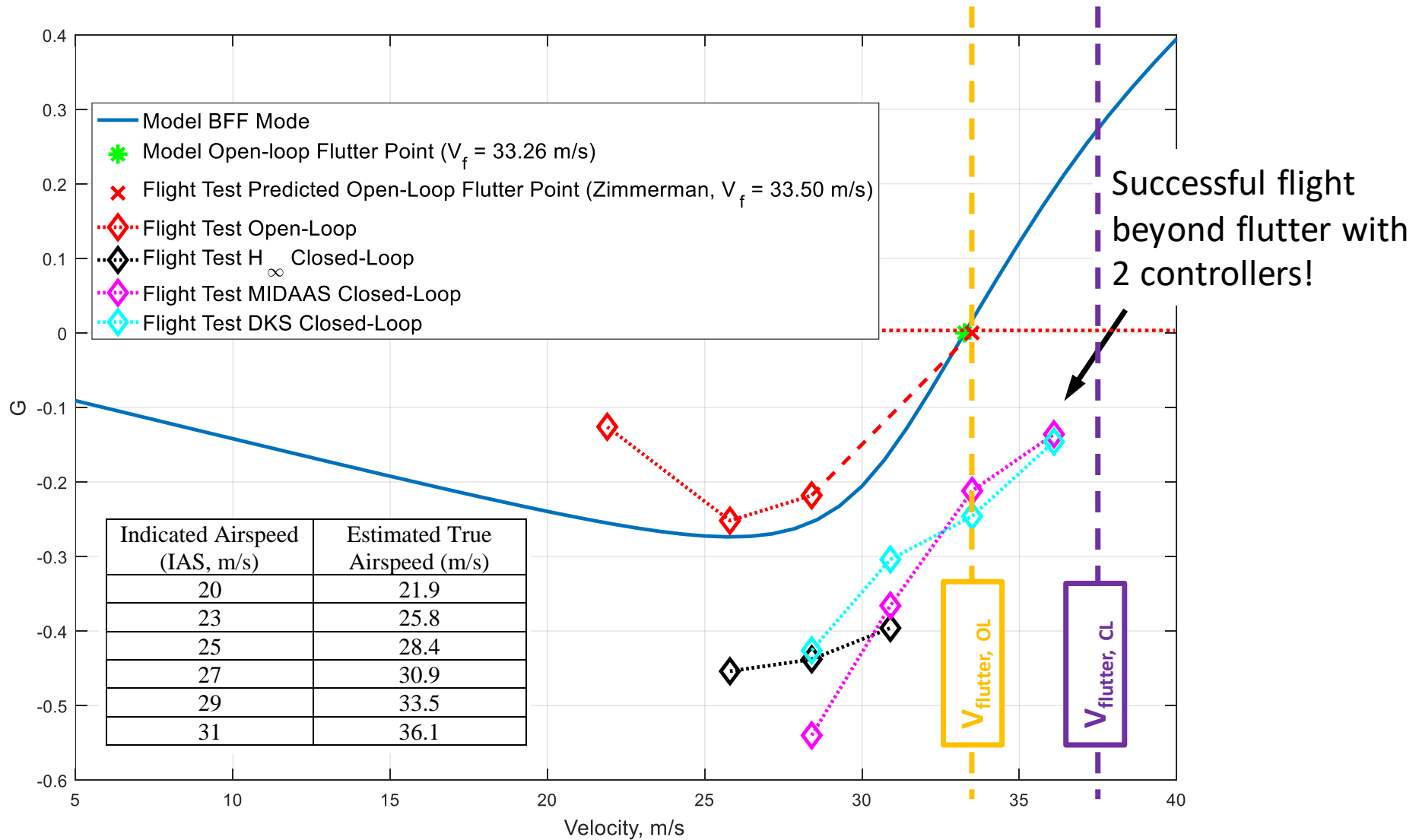
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 - MIDAAS: Danowsky (STI), 2017-4353
 - Classical Controller: Schmidt, Journal of GCD, 2016.
- Flight Tests
 - Ref: Danowsky, Kotikalpudi, Schmidt, Regan, Seiler, AIAA 2018-3427
 - Controllers tested at and above the designed airspeed.
 - All controllers added damping at the designed speed.
 - MIDAAS & classical designs flown above open-loop flutter speed.
 - Hinf controller did not increase flutter speed but this was an artifact of our design objective and flight test plan.

Pole Map for Retuned H_∞ Controller

Map of Poles and Zeros



Flight Test Summary



Next Steps

- **Robust Flutter Speed (RFS):** Airspeeds where active flutter control has 6dB/45deg margins on all inputs & outputs
 - Metric for safe flight envelope with active flutter suppression
 - Current: Restrict envelope to 20% below (open-loop) flutter speed

Next Steps

- **Robust Flutter Speed (RFS):** Airspeeds where active flutter control has 6dB/45deg margins on all inputs & outputs
 - Metric for safe flight envelope with active flutter suppression
 - Current: Restrict envelope to 20% below (open-loop) flutter speed
- Redesigned 3 controllers to maximize robust flutter speed
 - Design complicated by second bending mode at higher speeds
- **Preliminary Results:**
 - H_∞ control achieves robust/absolute flutter speeds of 43/41 m/s
 - Similar but slightly lower speeds for MIDAAS & classical designs
 - Tested in sims (linear parameter varying model with actuator limits & nonlinear panel-based model)