



# Aircraft System Identification



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# Outline



- **Overview of Aircraft System Identification**
- **Procedure and Results**
- **Applications**
- **Demonstration Using SIDPAC Software**
- **Concluding Remarks**
- **References for Further Study**



# Aircraft System Identification

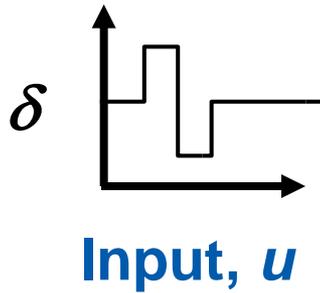


***System Identification*** is the process of building mathematical models for physical systems based on imperfect observations or measurements

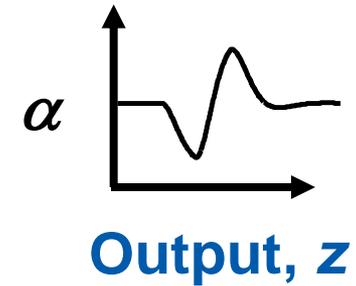


If the physical system is an aircraft, then this activity is called ***aircraft system identification***

# Problems In Dynamics



System,  $S$



***Simulation:*** Given  $S$  and  $u$ , find  $z$

***Control:*** Given  $S$  and  $z$ , find  $u$

***Identification:*** Given  $u$  and  $z$ , find  $S$



# Aircraft System Identification

$$m\dot{V} + \omega \times mV = F_{Aero} + F_{Thrust} + F_{Gravity} \quad \left[ \frac{d}{dt}(mV) = \sum F \right]$$
$$I\dot{\omega} + \omega \times I\omega = M_{Aero} + M_{Thrust} \quad \left[ \frac{d}{dt}(I\omega) = \sum M \right]$$

**Typical aircraft system identification problem:**

From measurements of the inputs and outputs, determine mathematical model forms for  $F_{Aero}$  and  $M_{Aero}$ , then estimate the unknown parameters in those models

*System Identification is used to model what is not known, based on measured data*



# How Does It Work?

$$\text{Pitching moment equation: } M = I_y \dot{q} + (I_x - I_z) pr + I_{xz} (p^2 - r^2)$$

## Equation-Error

$$M = I_y \dot{q} + (I_x - I_z) pr + I_{xz} (p^2 - r^2)$$

Postulated model:

$$J = \frac{1}{2} (M - \hat{M})^T (M - \hat{M})$$

Solve with one-shot linear algebra

## Output-Error

$$\dot{q} = \frac{1}{I_y} [M - (I_x - I_z) pr - I_{xz} (p^2 - r^2)]$$

Unknowns

$$\hat{M} = M_o + M_\alpha \alpha + M_q q + M_\delta \delta$$

Integrate  $\longrightarrow \hat{q}$

$$J = \frac{1}{2} (q - \hat{q})^T (q - \hat{q})$$

Solve with iterative nonlinear optimization



# What Are the Results?

Pitching moment model:  $\hat{M} = M_o + M_\alpha \alpha + M_q q + M_\delta \delta$

$M_o$  = pitching moment bias

$M_\alpha$  = static stability

$M_q$  = dynamic stability or damping

$M_\delta$  = pitch control authority

Results include estimated numerical values for all unknown parameters, as well as statistical uncertainties (error bounds).

Modeling results characterize the stability and control of the aircraft

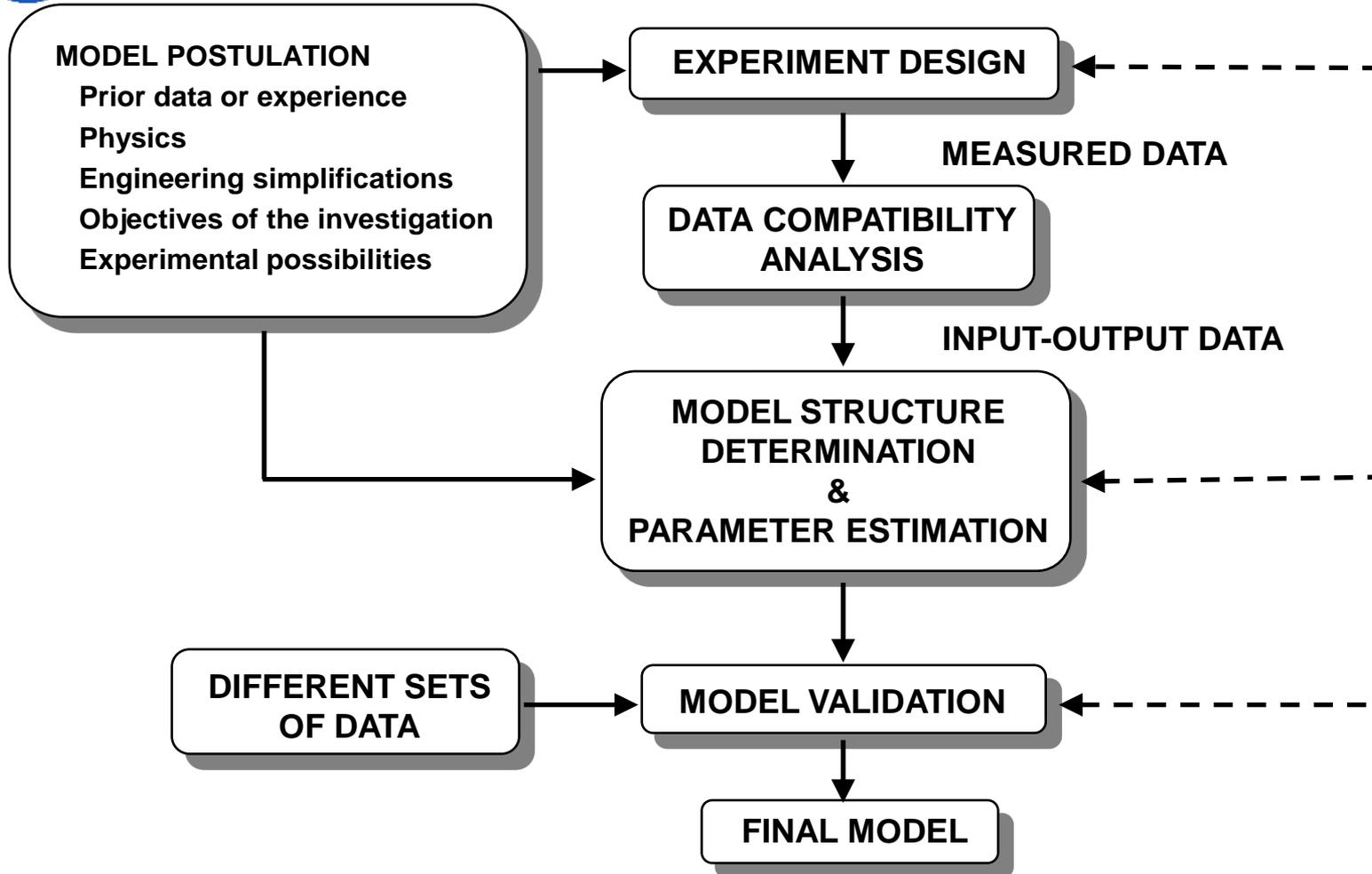


# It's Not Easy

- 1) **Aircraft are multiple-input, multiple-output, nonlinear dynamical systems with complicated, nonlinear, time-varying aerodynamics**
- 2) **For an aircraft in flight, applied forces and moments must be inferred from measured responses**
- 3) **Large amounts of data must be processed**
- 4) **Aircraft measurements are noisy and sensors have practical limitations**
- 5) **Physical quantities cannot be varied independently for an aircraft in flight**



# Aircraft System Identification



***Note that information embodied in a model is either assumed or derived from measurements***



# Physics and System Identification



***Scientific theories are not discoveries of the laws of nature but rather inventions of the human mind.***

**-- Dr. Athanasios Papoulis**

***All models are wrong; some are useful.***

**-- Dr. George Box**



# Applications

## *Flight Research, Envelope Expansion*



## *Validate and Improve Predictions*



## *Flight Simulation*



## *Accident Investigation*



## *Evaluate New or Modified Aircraft*

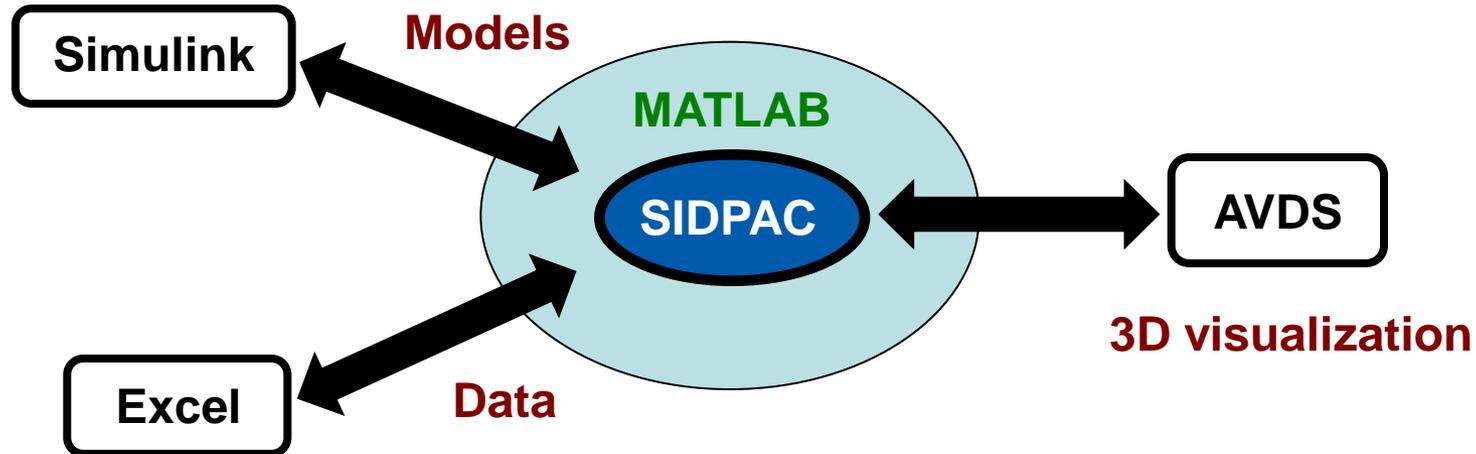


## *Flight Control, Flying Qualities*





# System Identification Programs for AirCRAFT (SIDPAC)



- **SIDPAC is a collection of over 350 programs that implement a wide variety of state-of-the-art methods for aircraft system identification**
- **SIDPAC programs are implemented as MATLAB® M-files, and have been thoroughly tested and successfully applied to real data**
- **SIDPAC is used at more than 80 organization worldwide to solve aircraft system identification problems**
- **SIDPAC documentation is the AIAA textbook *Aircraft System Identification – Theory and Practice*, by V. Klein and E.A. Morelli**



# What Does SIDPAC Do?



## *SIDPAC tools help an analyst to:*

- **Design experiments**
- **Define instrumentation requirements**
- **Filter, smooth, transform, and visualize the data**
- **Identify math models that mimic the real system**
- **Check model accuracy and predictive capability**
- **Organize, report, and use the results**



# SIDPAC Demonstration



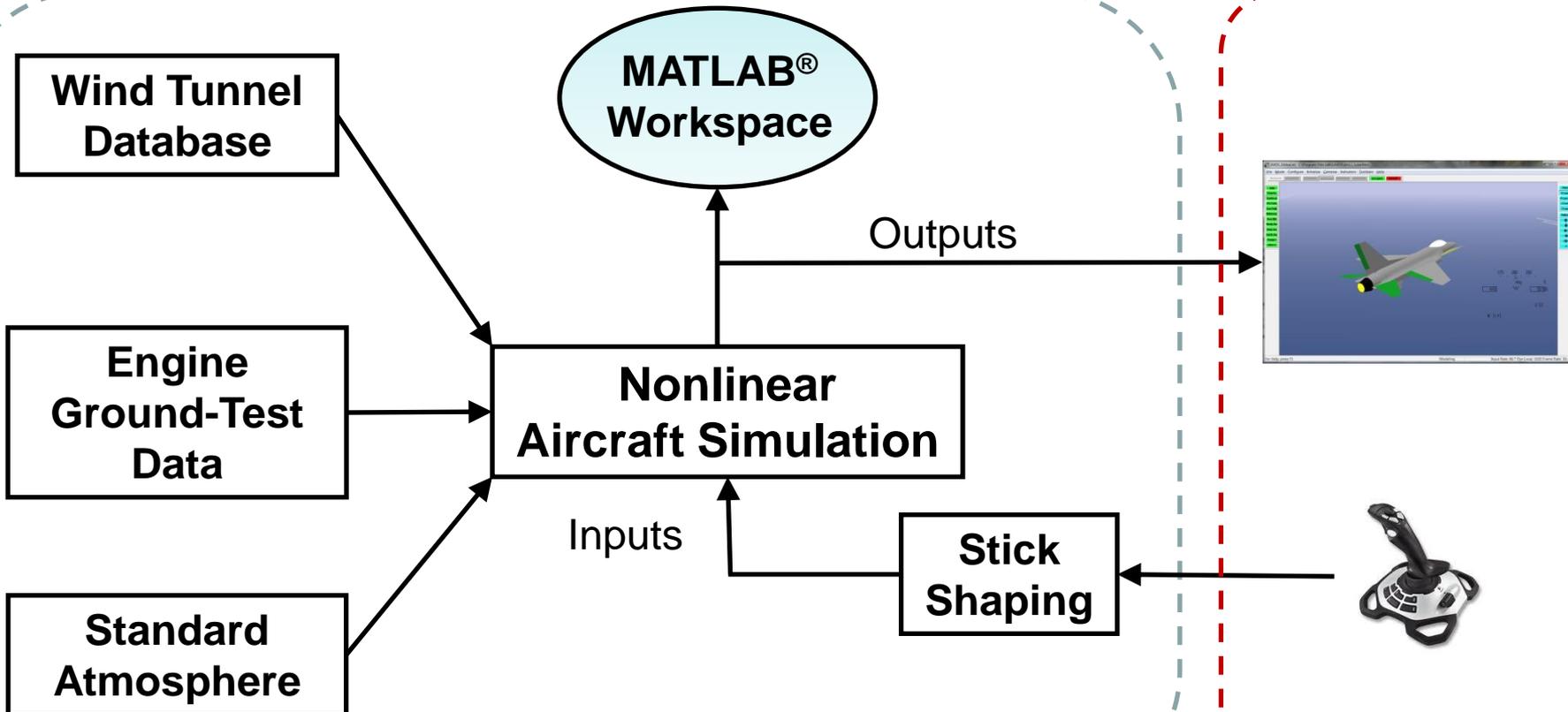
## *F-16 Fighting Falcon*



# F-16 Nonlinear Simulation

MATLAB®

AVDS





# Applications



*Twin Otter*



*X-43A (Hyper-X)*



*Sub-scale Transport Aircraft*



*ARES I-X Launch Vehicle*



*X-29A*



*Tu-144LL Supersonic Transport*



*1903 Wright Flyer Replica*



*Global Hawk*



***There are many others ...***



# Concluding Remarks

- **System Identification can be applied to any system; Gauss, Newton, and Einstein were all outstanding practitioners of System Identification.**
- **For modern Aircraft System Identification, experiment design, instrumentation system design, understanding data analysis and modeling methods, and the ability to use System Identification software are important for success.**
- **System Identification is a critical technology for aerospace vehicles throughout their lifetime, from preliminary design, through testing and operations.**
- **System Identification is a tool for understanding and interacting with the physical world.**



# References For Further Study



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- P3)** Hamel, P.G. and Jategaonkar, R. (1996) “Evolution of Flight Vehicle System Identification,” *Journal of Aircraft*, Vol. 33, No. 1, pp. 9-28.
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