



2nd AIAA Aeroelastic Prediction Workshop – Loci/CHEM Results

Eric Blades
Azariah Cornish

Prepared for:

Second Aeroelastic Prediction Workshop

Date:


January 2-3, 2016

13290 Evening Creek Drive, Suite 250, San Diego CA 92128

 (858) 480-2000

 www.ata-e.com

 [ata-engineering](https://www.linkedin.com/company/ata-engineering)

 [@ATAEngineering](https://twitter.com/ATAEngineering)

Agenda

- Methodology and Tools
 - CFD solver
 - CSD solver
 - Wetted surface transfer
 - Mesh deformation
- Coupling Approach
- Case 1 Results (3 mesh levels)
- Case 2 Results (3 mesh levels)

FSI Methodology

- Domain-decomposition or partitioned approach
 - Each solver is optimized for the numerics of each domain
 - Fluid domain: Loci/CHEM finite volume solver
 - Developed at Mississippi State University (Prof. Ed Luke)
 - Open source
 - Production solver at NASA/MSFC
 - Structural domain: FEM solver
 - **Linear: Native CSD solver module for CHEM**
 - Non-linear: Couple to Abaqus NLCSD solver
- Each domain suitably discretized for domain-specific analysis
 - Wetted surface will likely be discretized differently

CFD Flow Solver: Loci/CHEM

Key Features

- Unsteady Reynolds-Averaged Navier-Stokes solver
 - Cell-centered
 - Supports unstructured mesh topologies including polyhedral meshes
- Parallel, highly scalable
- Finite-rate chemically reacting flows
- Implicit and explicit time integration methods
- Multiple turbulence models and hybrid RANS-LES
- Moving meshes (ALE, GCL)
 - Mesh deformation
 - Overset mesh capability

CFD Flow Solver: Loci/CHEM

Important Parameters

- Unsteady Reynolds-Averaged Navier-Stokes solver
 - Case 1: Used SA and SST turbulence models (SA for unsteady)
 - Case 2: SST turbulence model
- Inviscid flux construction: Roe scheme
 - Spatially second-order accurate
 - Venkatakrisnan flux limiter used
- Temporal evolution: Newton-relaxation
- Temporal discretization
 - 3-pt backward Euler
 - 2nd order accurate
- Used provided unstructured meshes

Linear CSD Solver

- Developed as module for CHEM
- Import mass/stiffness matrices or modal model from Nastran and Abaqus
 - Allows use of existing structural models
- Utilizes PETSc parallel linear algebra library
- Newmark-beta time integration scheme
 - Implicit, 2nd order, backwards finite difference
 - Hilbur-Hughes-Taylor similar, adds numerical damping
- No structural damping used
- Initial *rotational velocity* applied to perturb structure

Wetted Surface Information Transfer

- Algorithm ensures *global* conservation of loads and displacements
 - Principal of virtual work and is used to transform the aerodynamic forces to the finite element nodal forces
→ *Conserves forces/moments*
 - Structural displacements at the FE nodes are transformed back to the CFD wetted surface grid points through the reciprocal theorem → *Ensures conservation of work*
- Requires wetted surface definition for CFD and CSD domains
- Robust
 - Allows for gaps between CFD and FEM wetted surfaces
 - Allows disjoint wetted surfaces

Wetted Surface Algorithm

- For each CFD wetted surface node
 - Find nearest FEM node
 - Find host FEM element
 - Search performed using element neighbor search
 - Only performed once
- Project all CFD forces to FEM wetted surface
 - Distribute force to nodes of host element using isoparametric shape functions

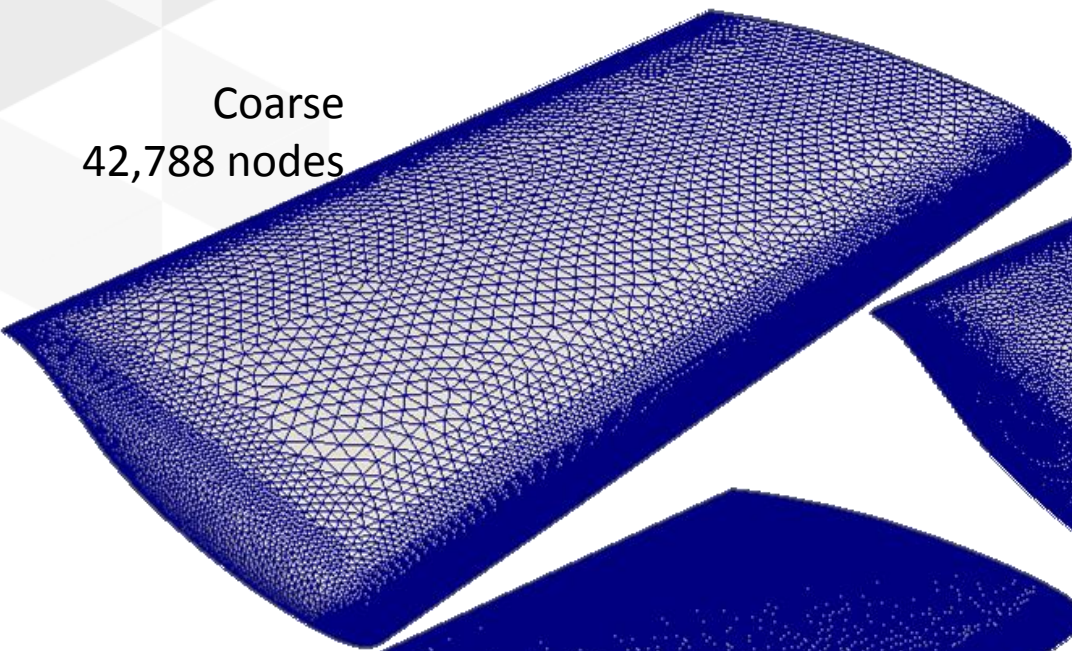
$$F_i^{CSD} = \sum_{j=1}^m \varphi_j f_i^{CFD} \quad M_i^{CSD} = \sum_{j=1}^m \varphi_j \left(\vec{f}^{CFD} \times \vec{d} \right)$$

- Use of same shape functions for displacement transfer ensure conservation of work

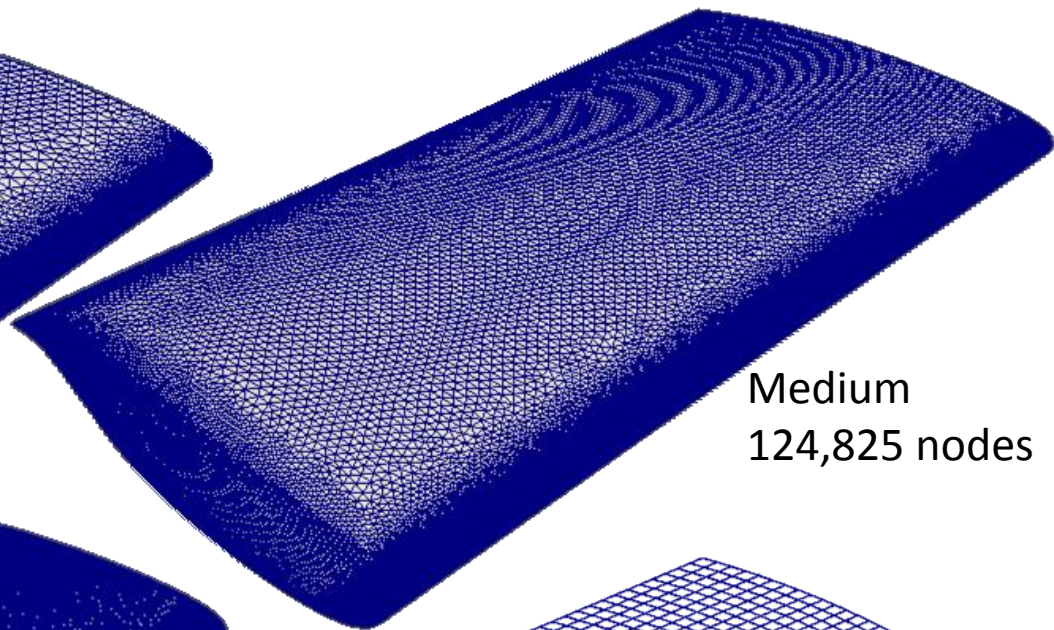
$$\delta_i^{CFD} = \sum_{j=1}^m \varphi_j \left(\delta_i^{CSD} + \vec{d} \times \vec{\delta}^{CSD} \right)$$

Wetted Surface Comparison

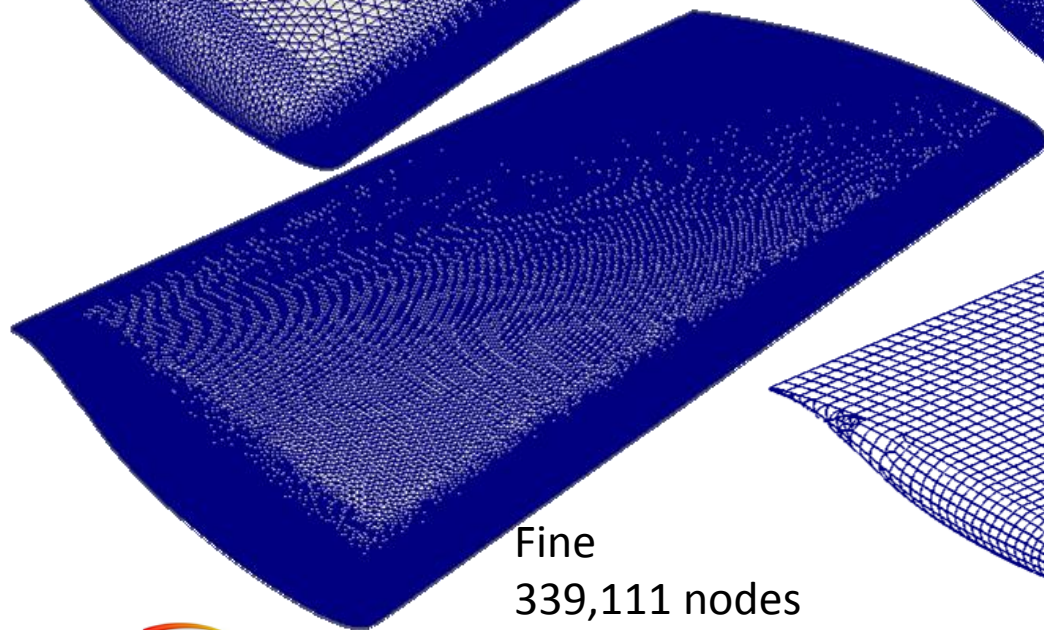
Coarse
42,788 nodes



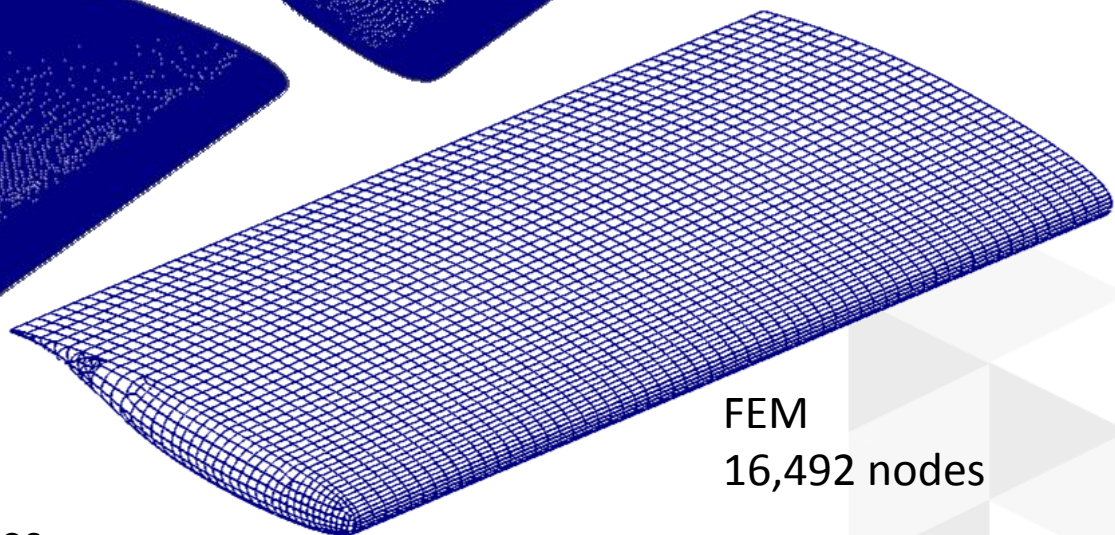
Medium
124,825 nodes



Fine
339,111 nodes

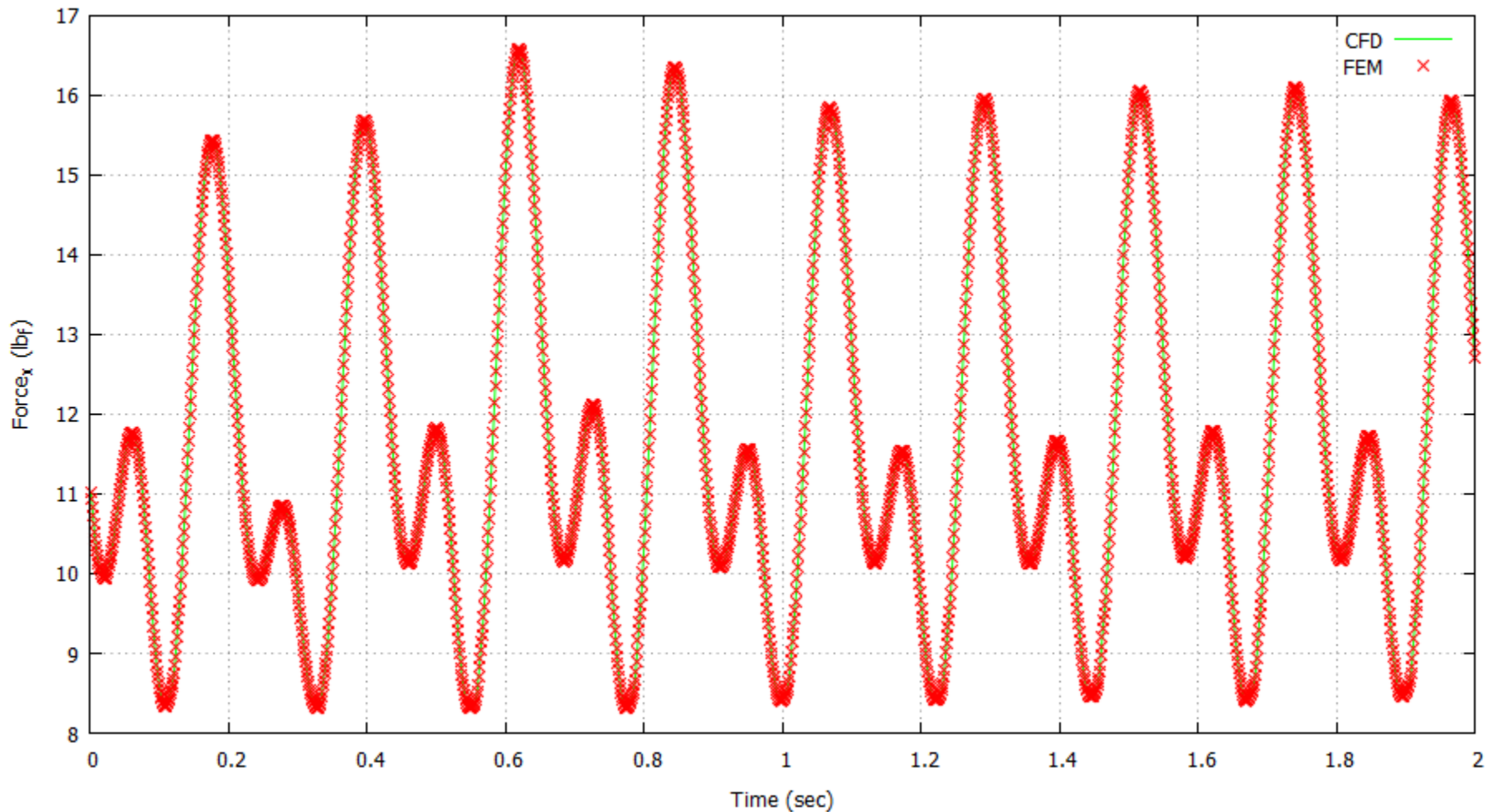


FEM
16,492 nodes



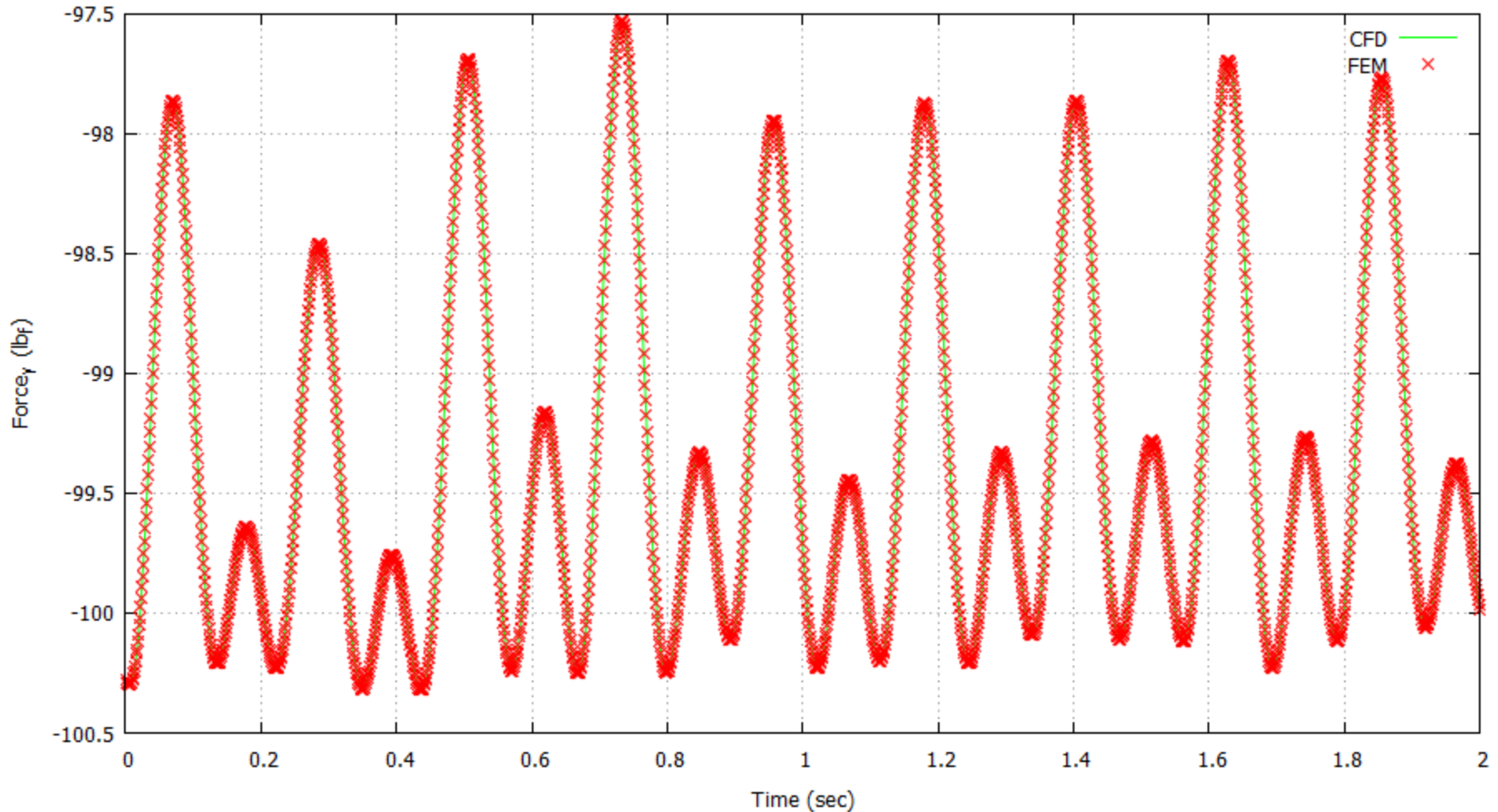
Wetted Surface Force Comparison: Fx

Medium CFD grid at the predicted flutter condition
Differences to within machine precision



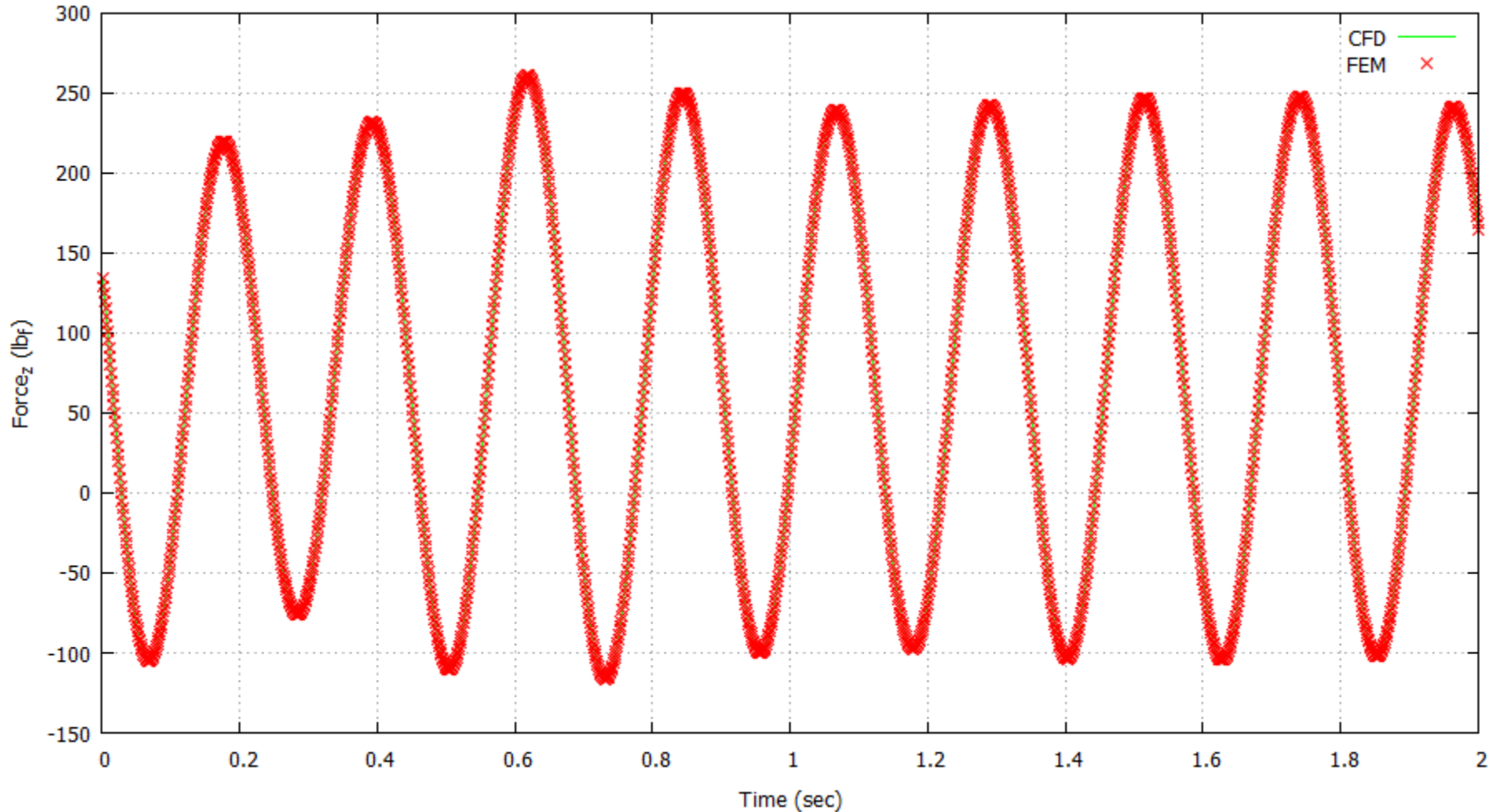
Wetted Surface Force Comparison: F_y

Medium CFD grid at the predicted flutter condition



Wetted Surface Force Comparison: F_z

Medium CFD grid at the predicted flutter condition

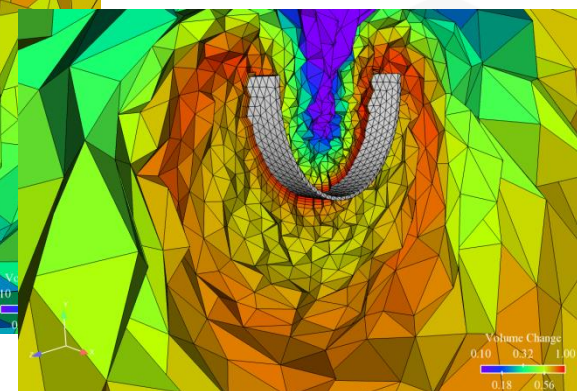
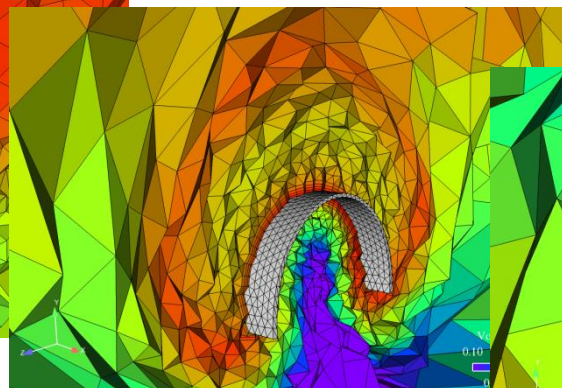
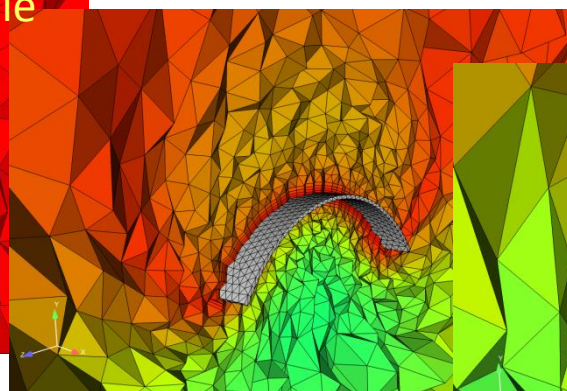
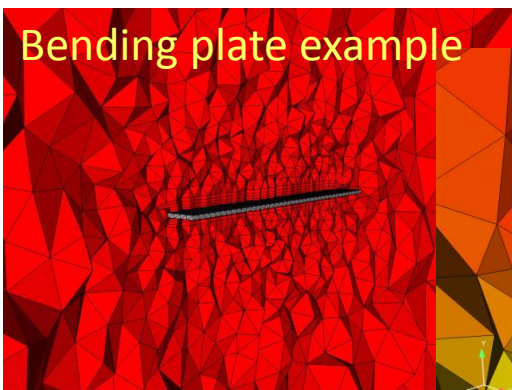
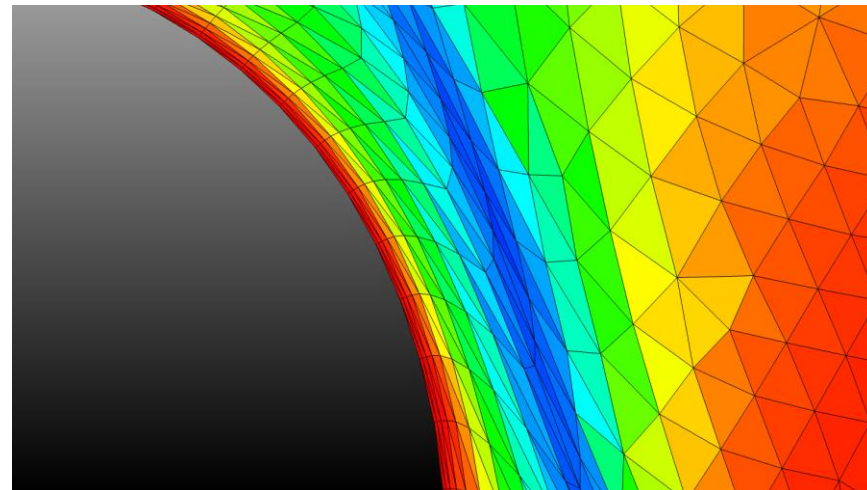
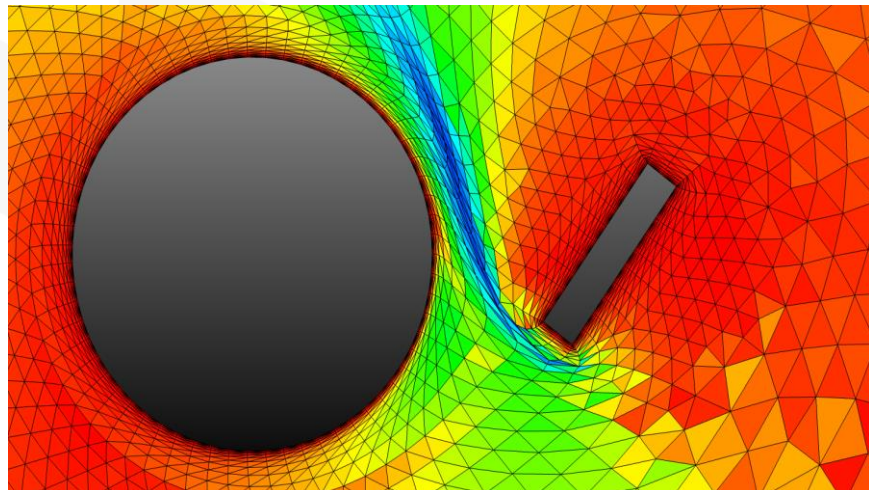


- Interpolation based approach[†]
 - Uses reciprocal distance-weighted averages of rotation and displacements of surface nodes
 - Local deformation field is modeled as a rigid body transformation involving both a rotation and a translation
 - Rotations of the surface about local nodes are computed using a nonlinear least squares method to find the closest rotation about the node that best matches the displacements of all edges and normals from surface facets that reference the given node

[†]E. Luke , E. Collins, and E. Blades, "A fast mesh deformation method using explicit interpolation," Journal of Computational Physics:231(2), pp. 586-601

- Utilize a two-exponent form of the weighting function
 - Preserve near-boundary deformations while providing a smooth transition in the interpolation from a near-body region of strong boundary influence into the bulk of the volume mesh
 - Works well on arbitrary mesh types including viscous BL meshes and hanging node adapted meshes
- Deformation applied in single step so mesh quality doesn't degrade for periodic motions

Mesh Deformation Examples

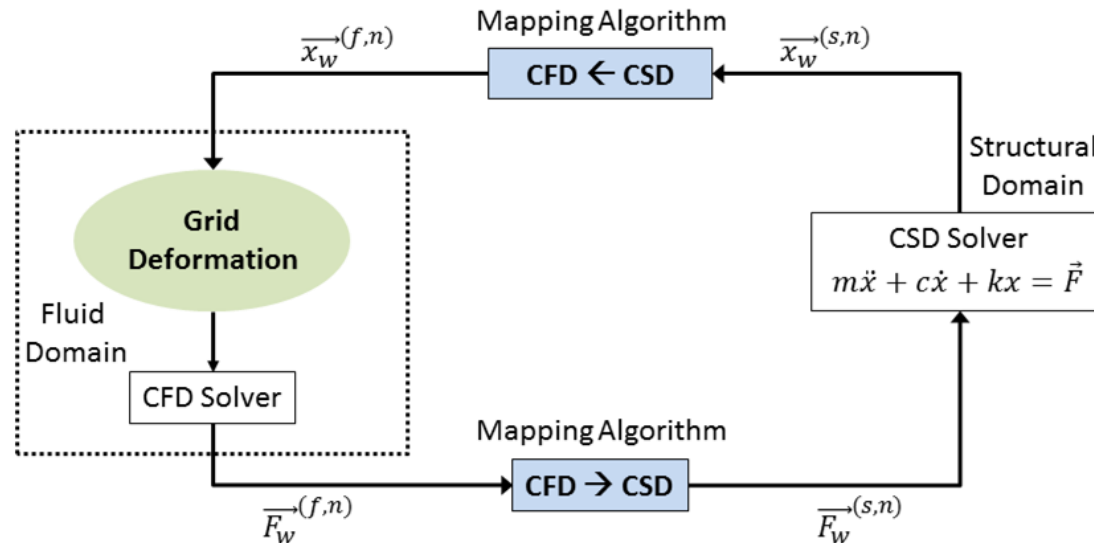


Cell Volume Fraction
0.1 1.0

Coupling Approach

When to couple/exchange information?

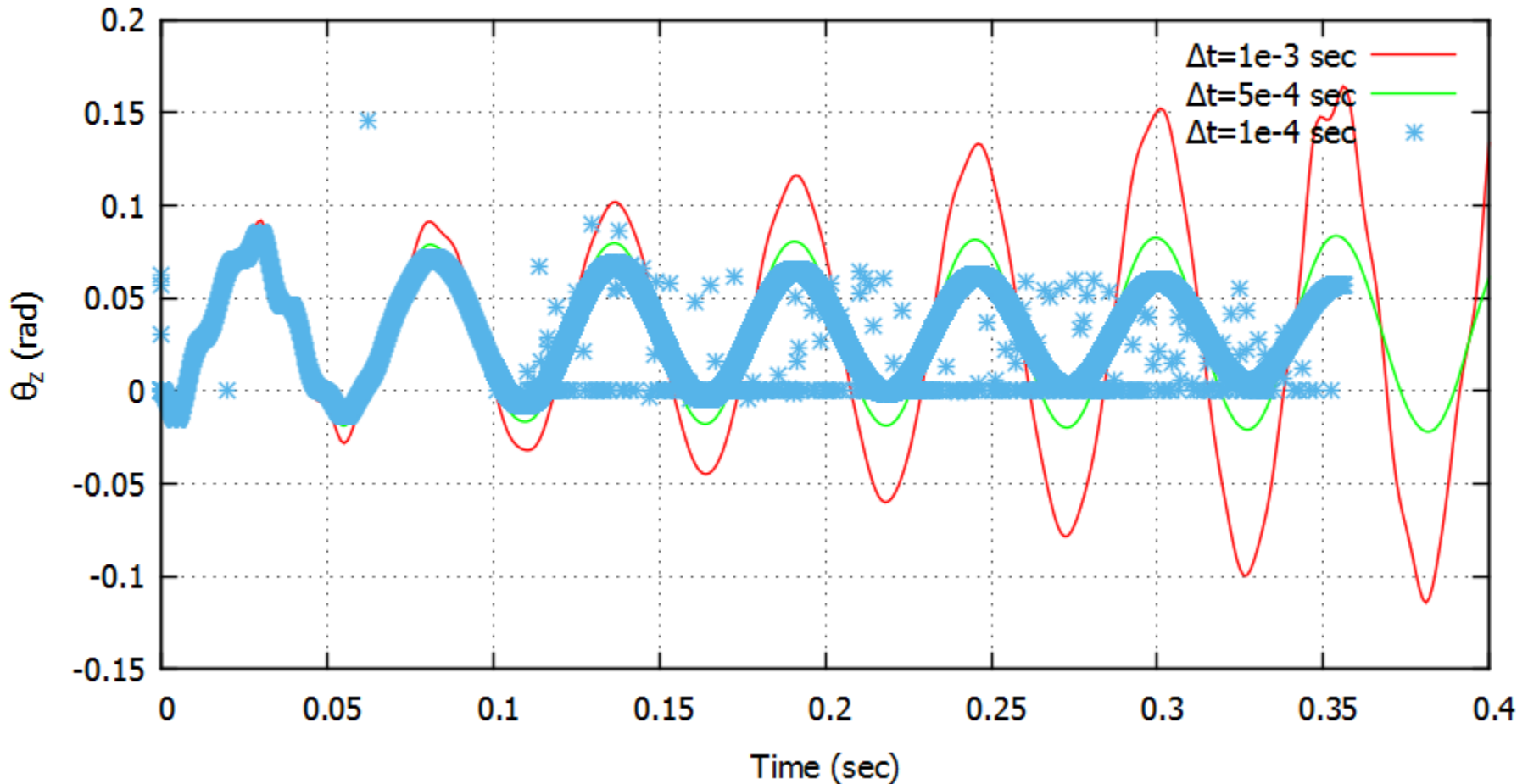
- Weak/loose coupling: Information exchange at end of each solver time step \rightarrow coupled solution is temporally 1st order



- Strong/tight coupling: Exchange information within time step at sub-iteration level \rightarrow coupled solution is temporally 2nd order

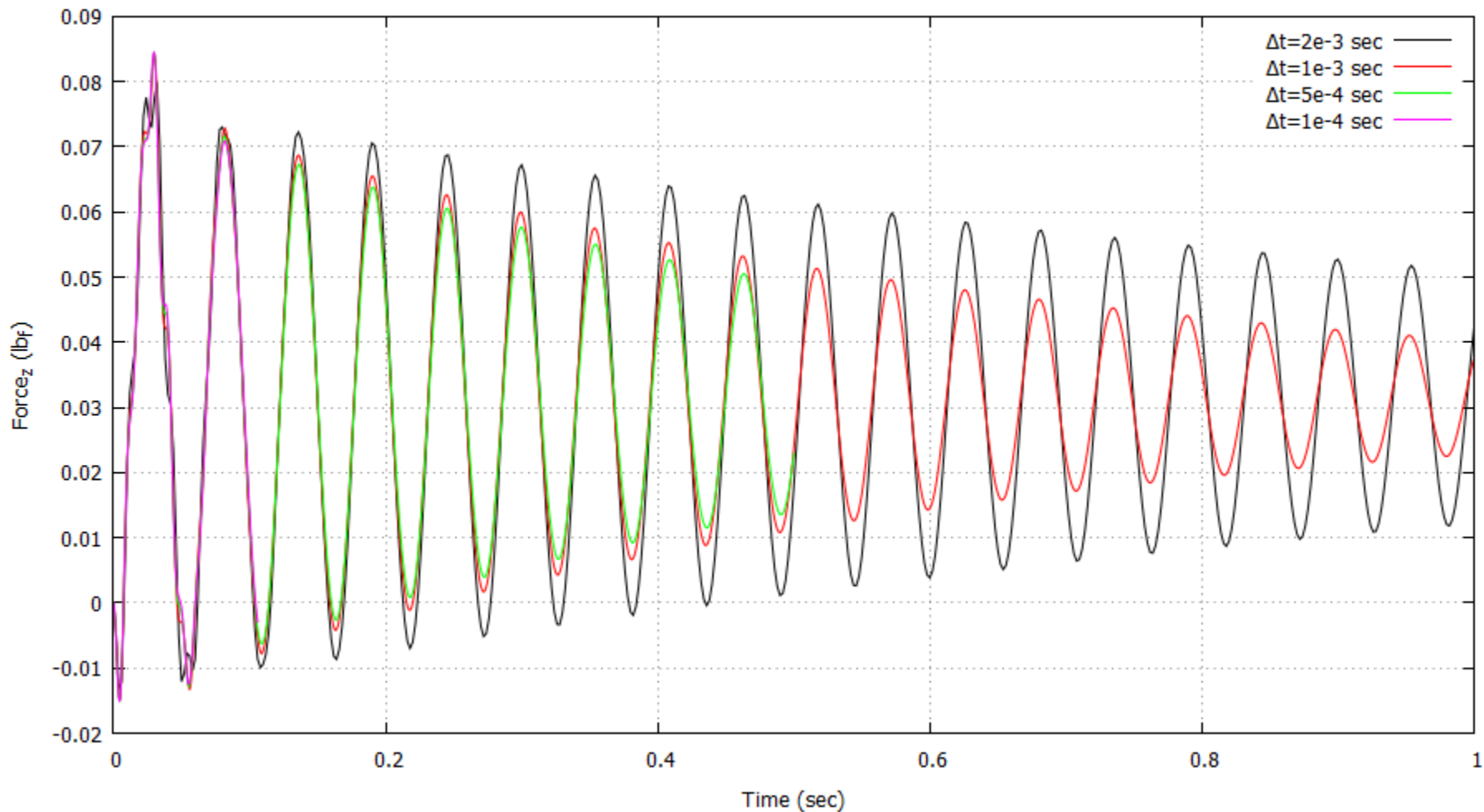
Coupling Scheme: First Order

First Order Coupling Time Step Study
NACA 64A010 Airfoil, Mach=0.7, $q=121505$ kPa, $\alpha=3^\circ$



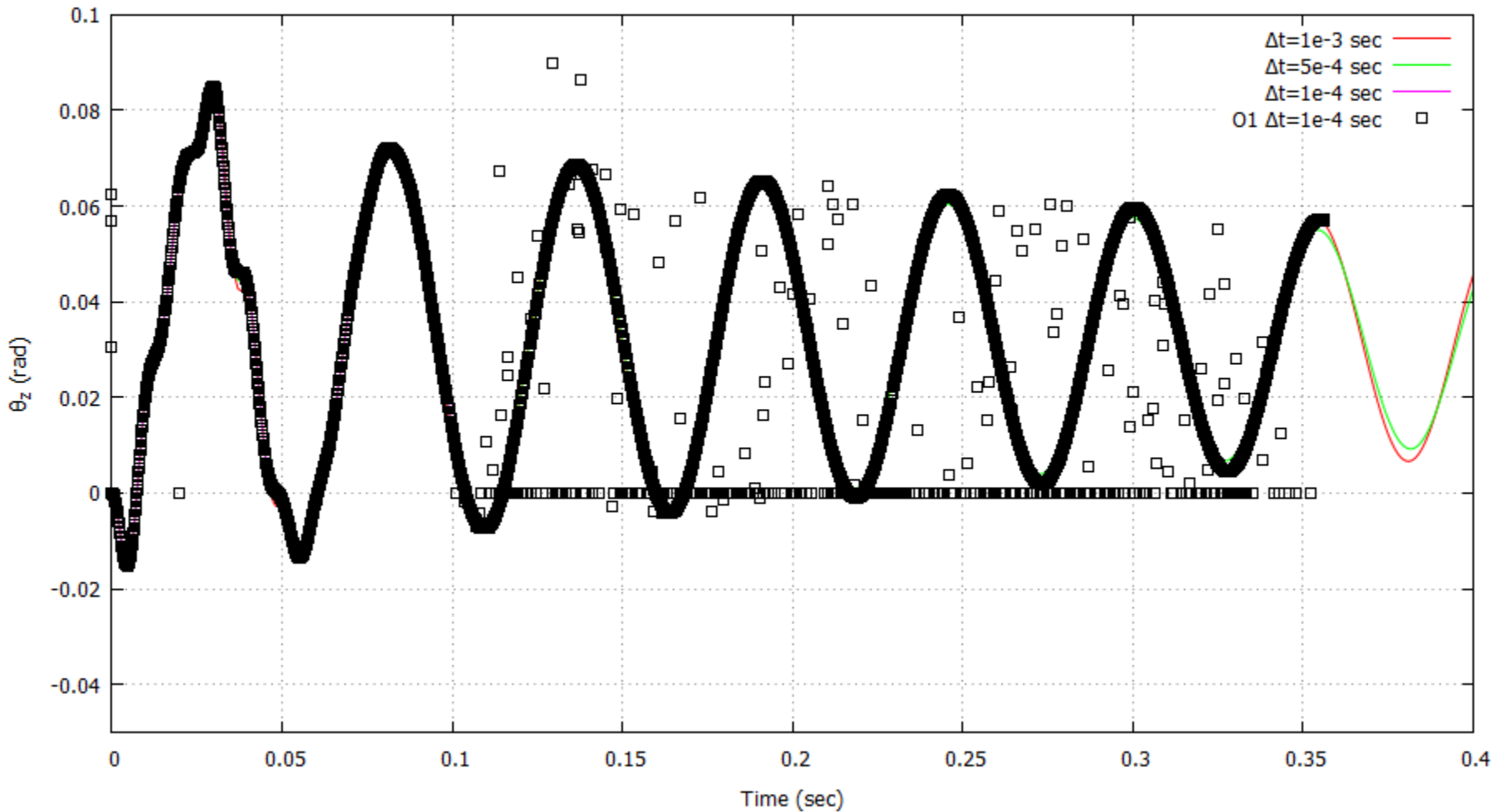
Coupling Scheme: Second Order

Second Order Coupling Time Step Study
NACA 64A010 Airfoil, Mach=0.7, $q=121505$ kPa, $\alpha=3^\circ$



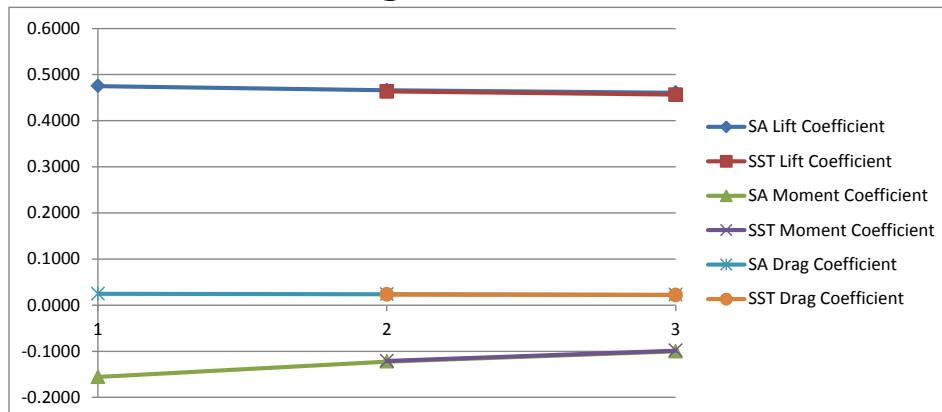
Coupling Scheme Comparison

Second Order Coupling Time Step Study
NACA 64A010 Airfoil, Mach=0.7, $q=121505$ kPa, $\alpha=3^\circ$



Case 1: Steady Results

- All grids were run steady-state before beginning oscillation and 60% Span coefficients calculated
- Minimal difference between turbulence models (SA used for dynamic runs)
- Lift and drag coefficients changed <5% between grids
- Moment coefficient changed ~36% from coarse to fine grid



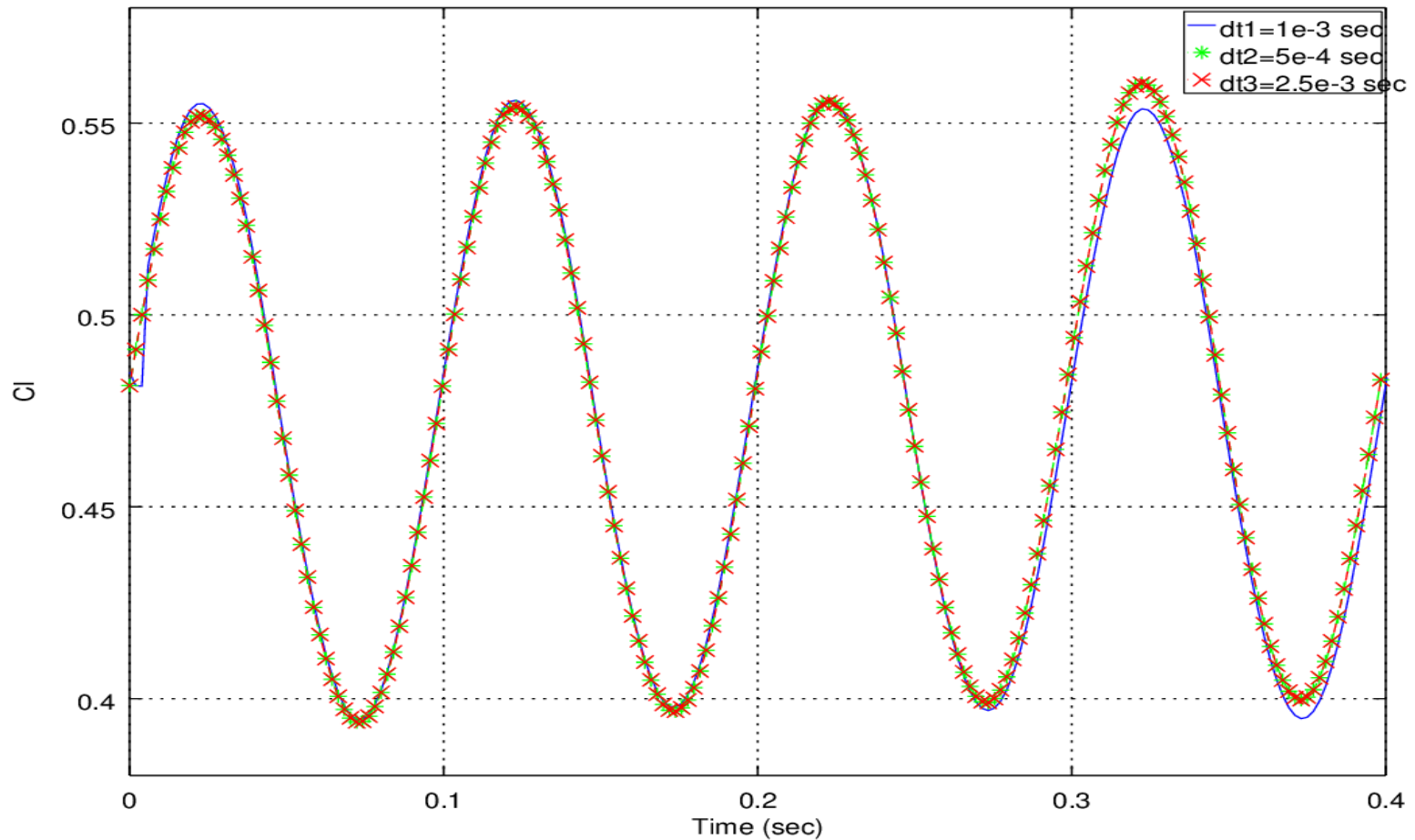
		Coarse		Med		Fine	
		SA	SST	SA	SST	SA	SST
C_L	Avg.	0.4750		0.4660	0.4635	0.4607	0.4565
	Std.	0.23%		0.30%	0.30%	0.06%	0.06%
C_D	Avg.	-0.1557		-0.1223	-0.1212	-0.1003	-0.0985
	Std.	0.11%		0.11%	0.11%	0.08%	0.08%
C_M	Avg.	0.0246		0.0236	0.0233	0.0224	0.0220
	Std.	0.34%		0.37%	0.37%	0.38%	0.39%

Case 1 Pertinent Unsteady Parameters

- Temporal resolution study
 - $\Delta t_1 = 1e-3 \text{ sec} \rightarrow 100 \text{ pts per cycle}$
 - $\Delta t_2 = 5e-4 \text{ sec} \rightarrow 200 \text{ pts per cycle}$
 - $\Delta t_3 = 2.5e-4 \text{ sec} \rightarrow 400 \text{ pts per cycle}$
 - Solution using Δt_2 and Δt_3 nearly identical
- Used 5 Newton sub-iterations
- Ran for 1 sec of physical time $\rightarrow 10$ cycles
- Grid was rigidly rotated, not deformed

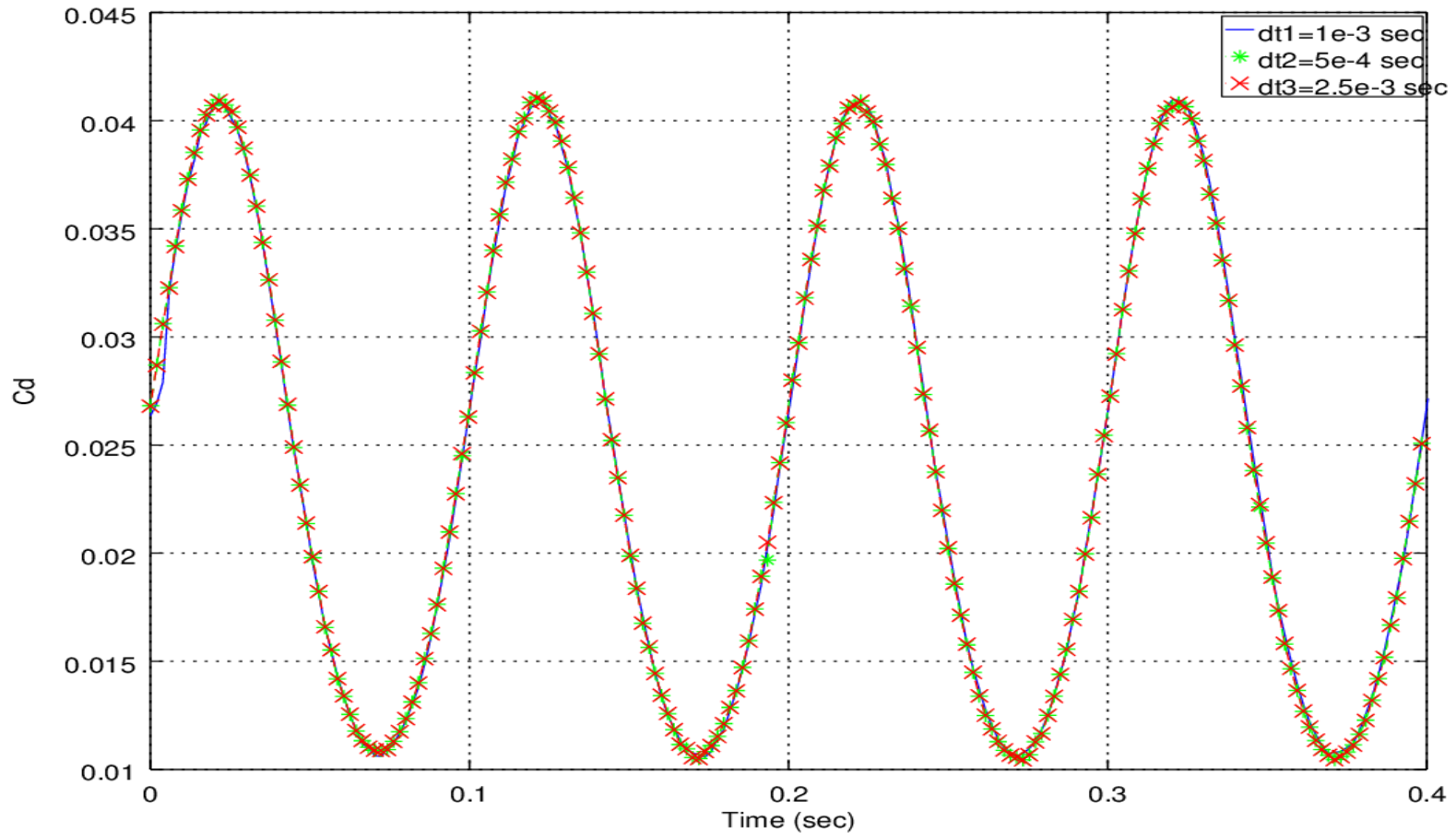
Case 1 Temporal Resolution Study

Coarse Grid: Lift Coefficient



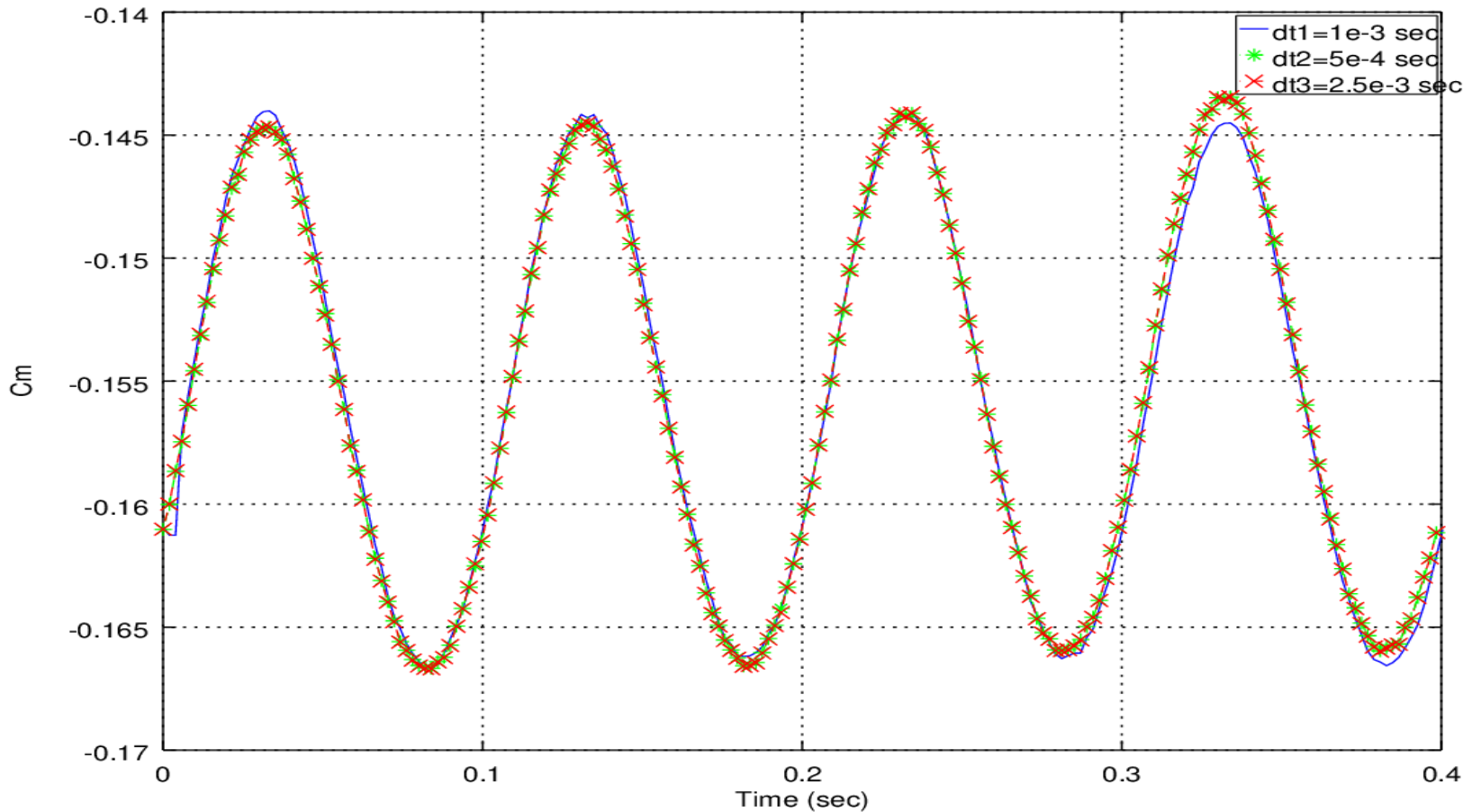
Case 1 Temporal Resolution Study

Coarse Grid: Drag Coefficient



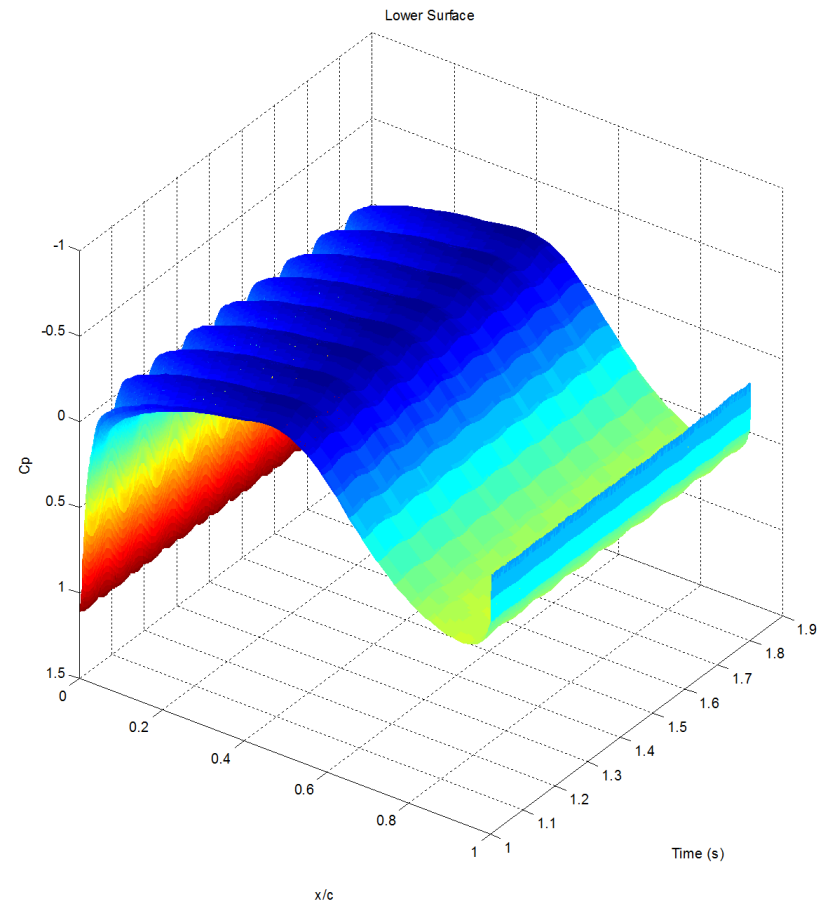
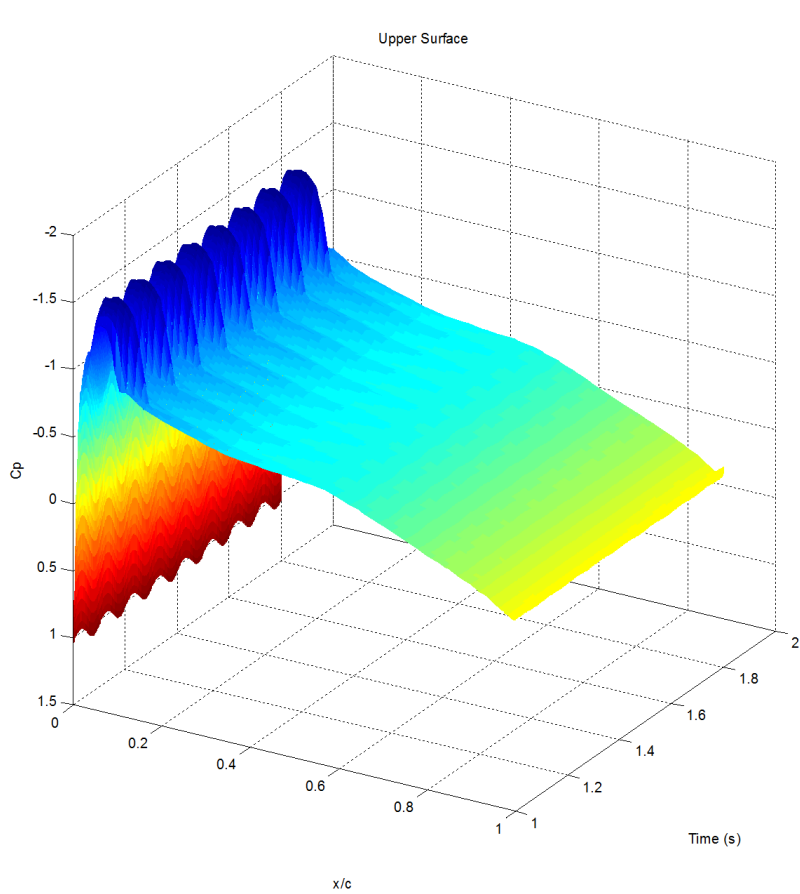
Case 1 Temporal Resolution Study

Coarse Grid: Pitching Moment Coefficient



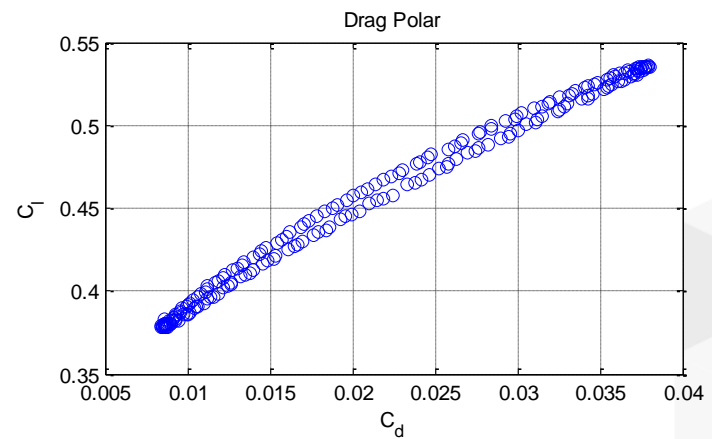
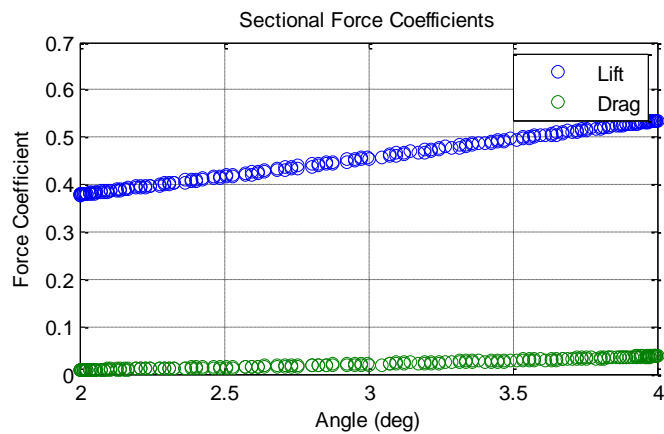
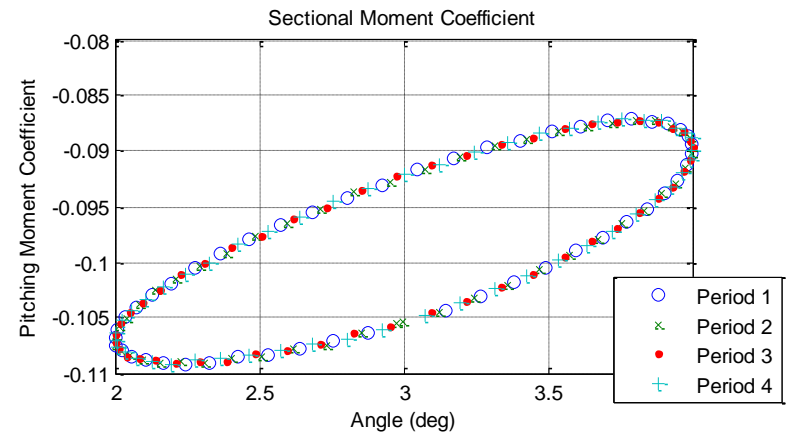
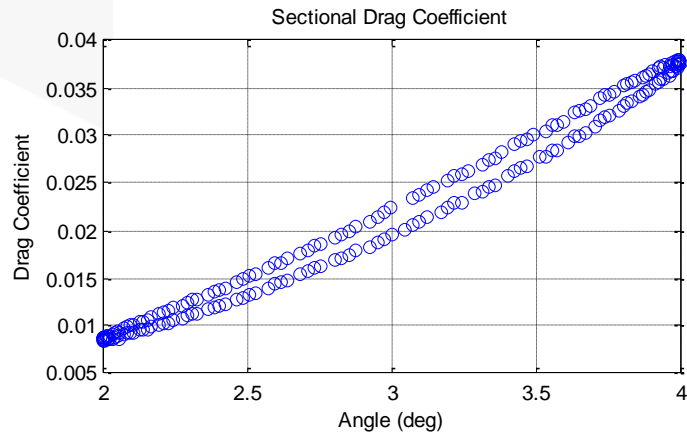
Case 1 Results

Fine Grid



Case 1: Coefficients vs Angle of Attack

Fine Grid, 60 % Span



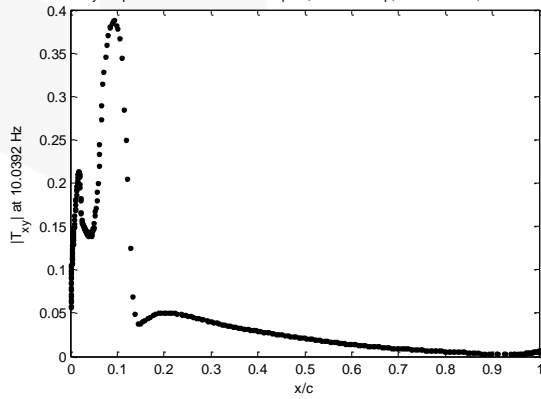
Case 1: FRFs

Fine Grid, 60 % Span, $dt_1=1e-3$

BSCW Analysis at Mach 0.7, 3° , Forced Oscillation at 10.0392 Hz

Input: θ ; Output: Cp upper surface, 60% span station

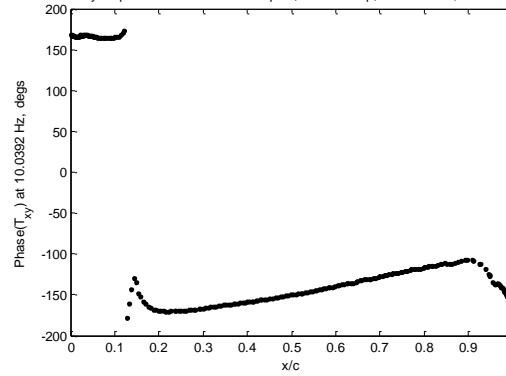
Fourier analysis parameters: nfft: 102 samples; 90% overlap; # blocks: 11, Window: rectwin



BSCW Analysis at Mach 0.7, 3° , Forced Oscillation at 10.0392 Hz

Input: θ ; Output: Cp upper surface, 60% span station

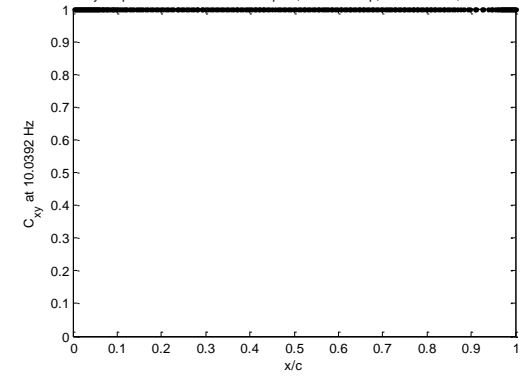
Fourier analysis parameters: nfft: 102 samples; 90% overlap; # blocks: 11, Window: rectwin



BSCW Analysis at Mach 0.7, 3° , Forced Oscillation at 10.0392 Hz

Input: θ ; Output: Cp upper surface, 60% span station

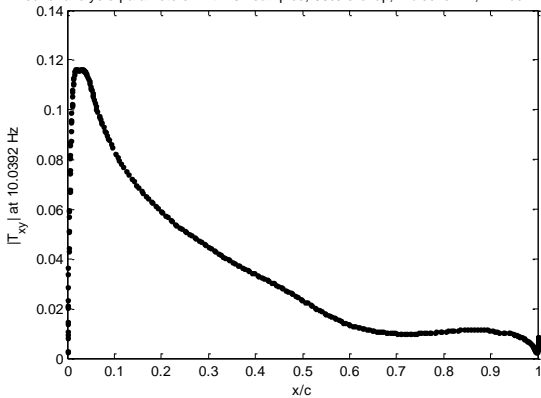
Fourier analysis parameters: nfft: 102 samples; 90% overlap; # blocks: 11, Window: rectwin



BSCW Analysis at Mach 0.7, 3° , Forced Oscillation at 10.0392 Hz

Input: θ ; Output: Cp lower surface, 60% span station

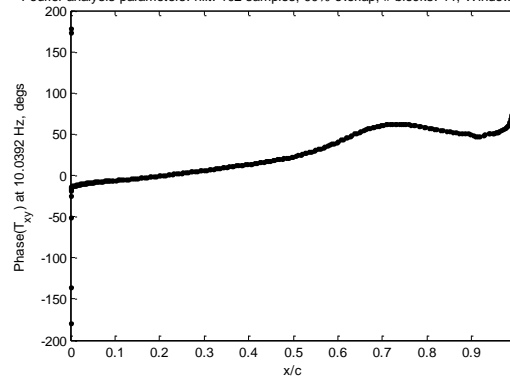
Fourier analysis parameters: nfft: 102 samples; 90% overlap; # blocks: 11, Window: rectwin



BSCW Analysis at Mach 0.7, 3° , Forced Oscillation at 10.0392 Hz

Input: θ ; Output: Cp lower surface, 60% span station

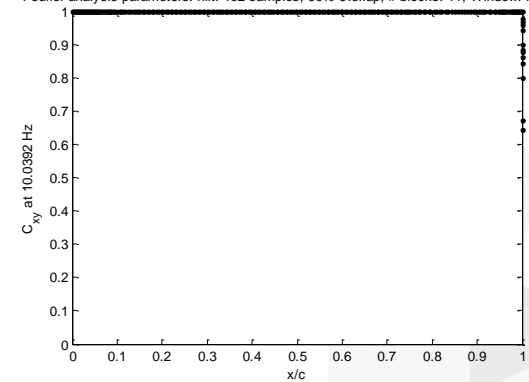
Fourier analysis parameters: nfft: 102 samples; 90% overlap; # blocks: 11, Window: rectwin



BSCW Analysis at Mach 0.7, 3° , Forced Oscillation at 10.0392 Hz

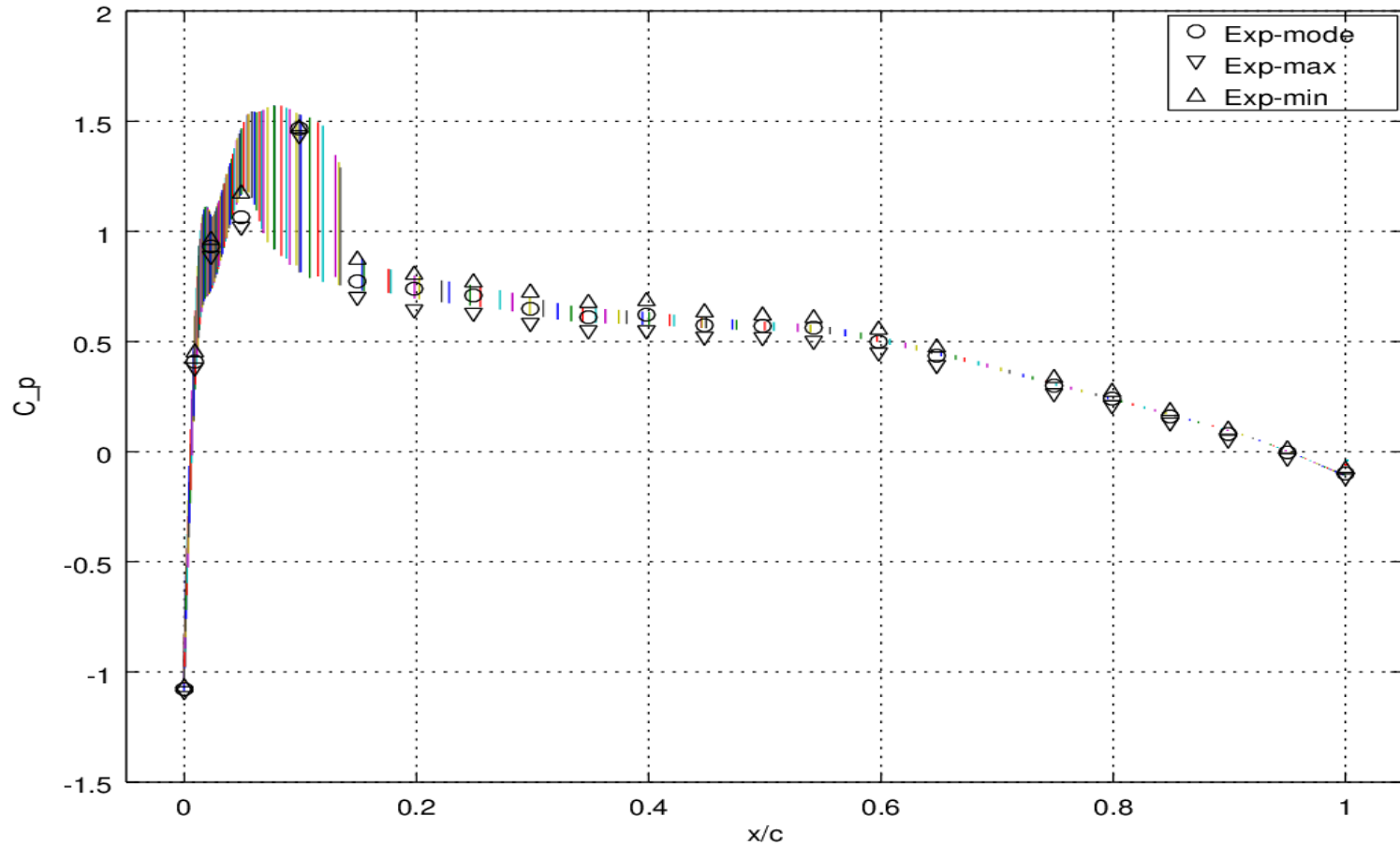
Input: θ ; Output: Cp lower surface, 60% span station

Fourier analysis parameters: nfft: 102 samples; 90% overlap; # blocks: 11, Window: rectwin



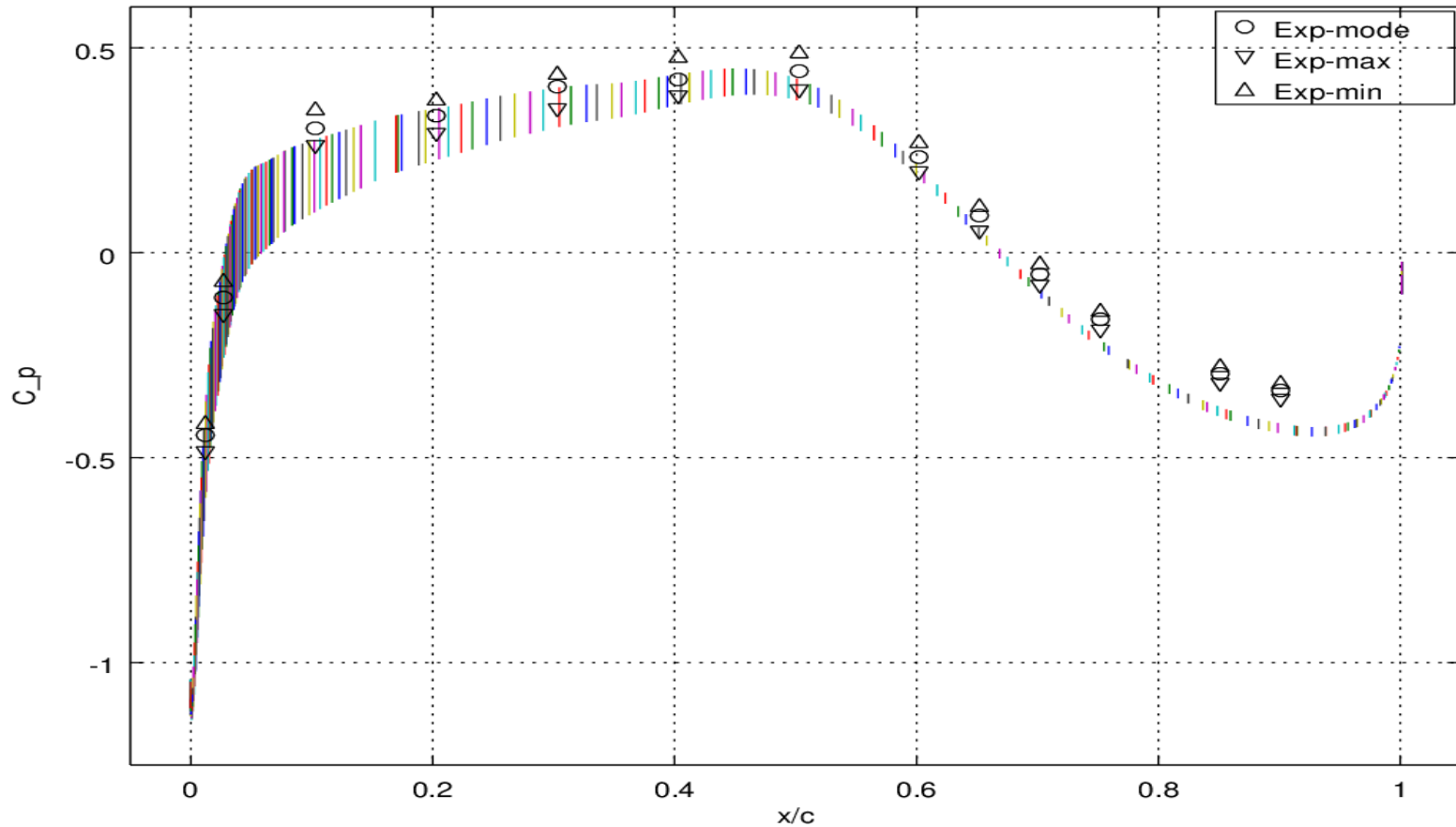
Unsteady Upper Surface Pressure

Medium Grid, 60% Span Location, $dt_2=5e-4$ sec



Unsteady Lower Surface Pressure

Medium Grid, 60% Span Location, $dt_2=5e-4$ sec



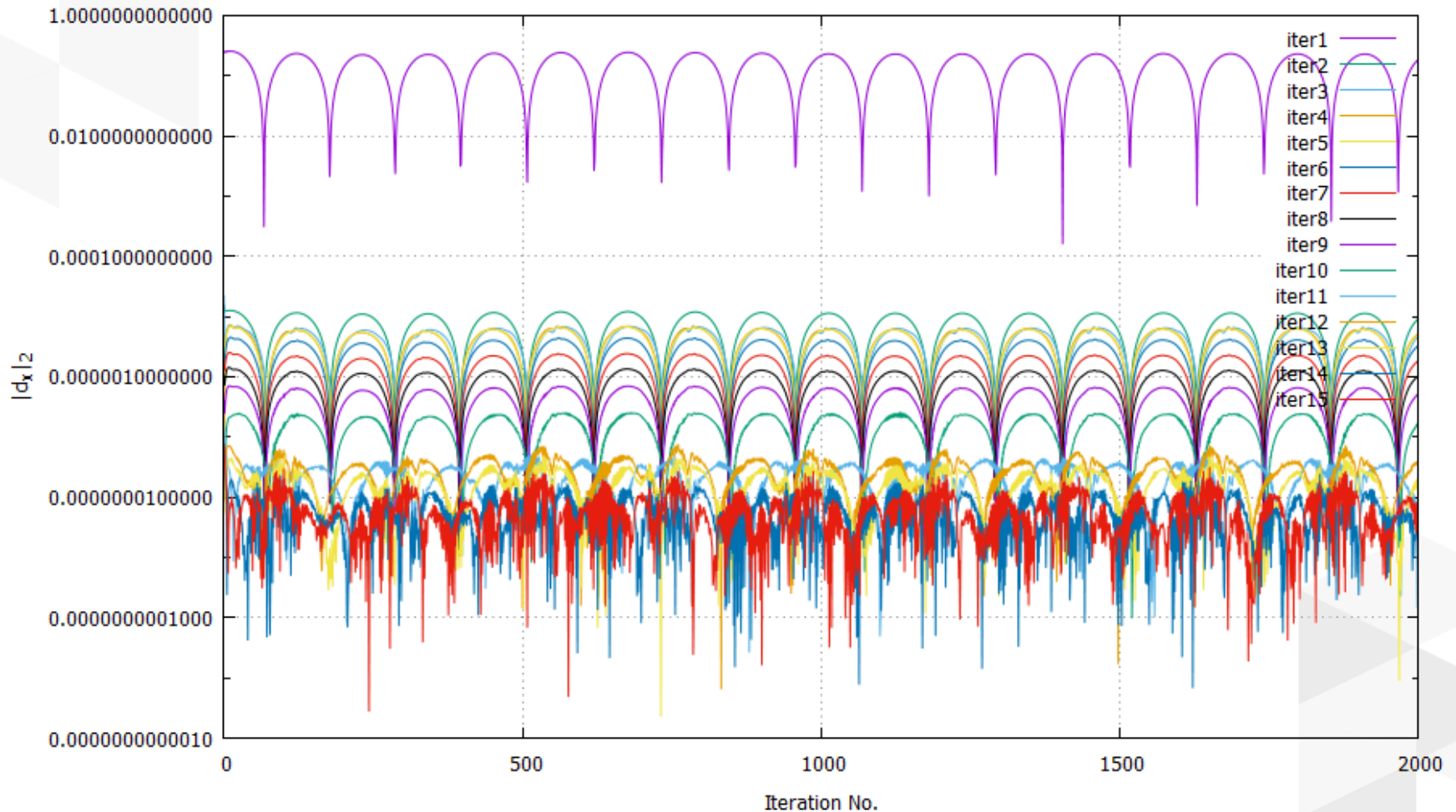
Case 2 Input Parameters

- Time step: $\Delta t = 1 \text{e-}3 \text{ sec}$
 - Approximately 220 pts per cycle (Strouhal number consideration)
 - Performed time step study on Case 1
 - $\Delta t = 5 \text{e-}4 \text{ sec}$ adequate (200 pts per cycle) and similar flow condition
 - Should perform temporal study for Case 2
 - Balance between accuracy and resources
- Used strong coupling with 15 sub-iterations
 - Displacement converge 4 orders of magnitude
 - Force converge 3-4 orders of magnitude
- Duration: 4 sec → ~18 periods
- Initial conditions: converged rigid solution and perturbation to rotational velocity
- Mesh deformed, not moved rigidly

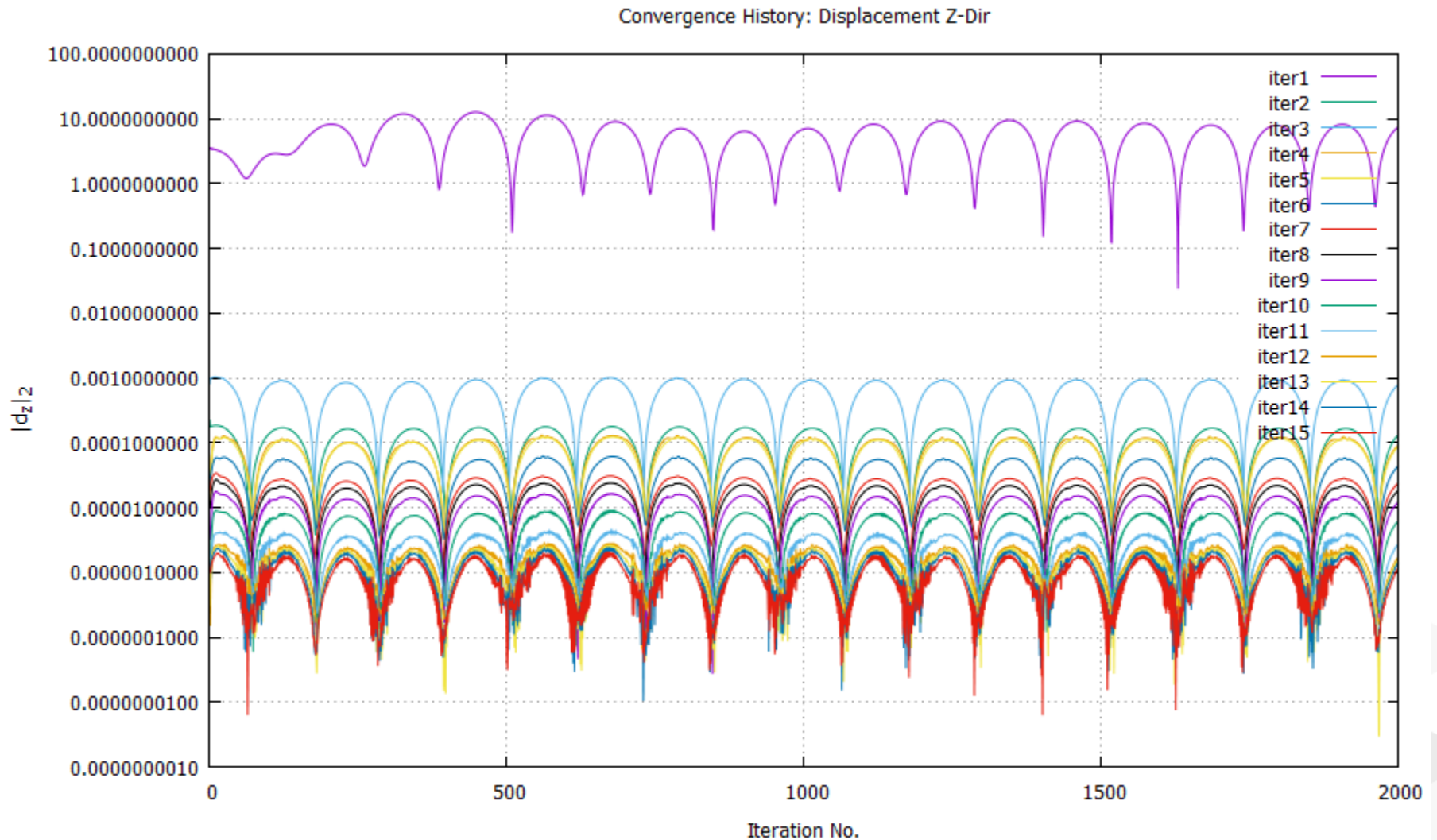
Sub-iteration Convergence History: dx

Case 2, Medium Grid, Flutter Condition

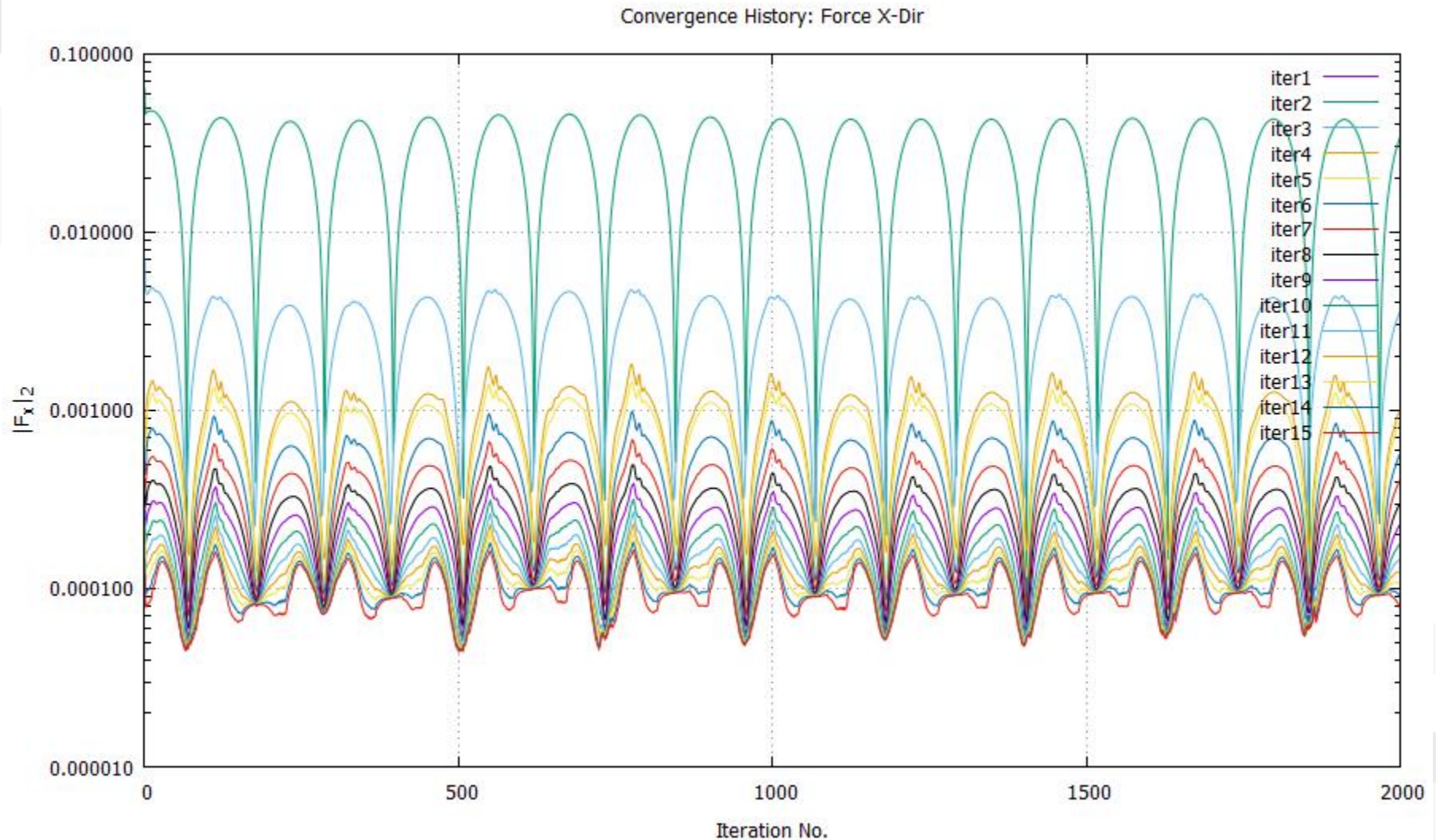
Convergence History: Displacement X-Dir



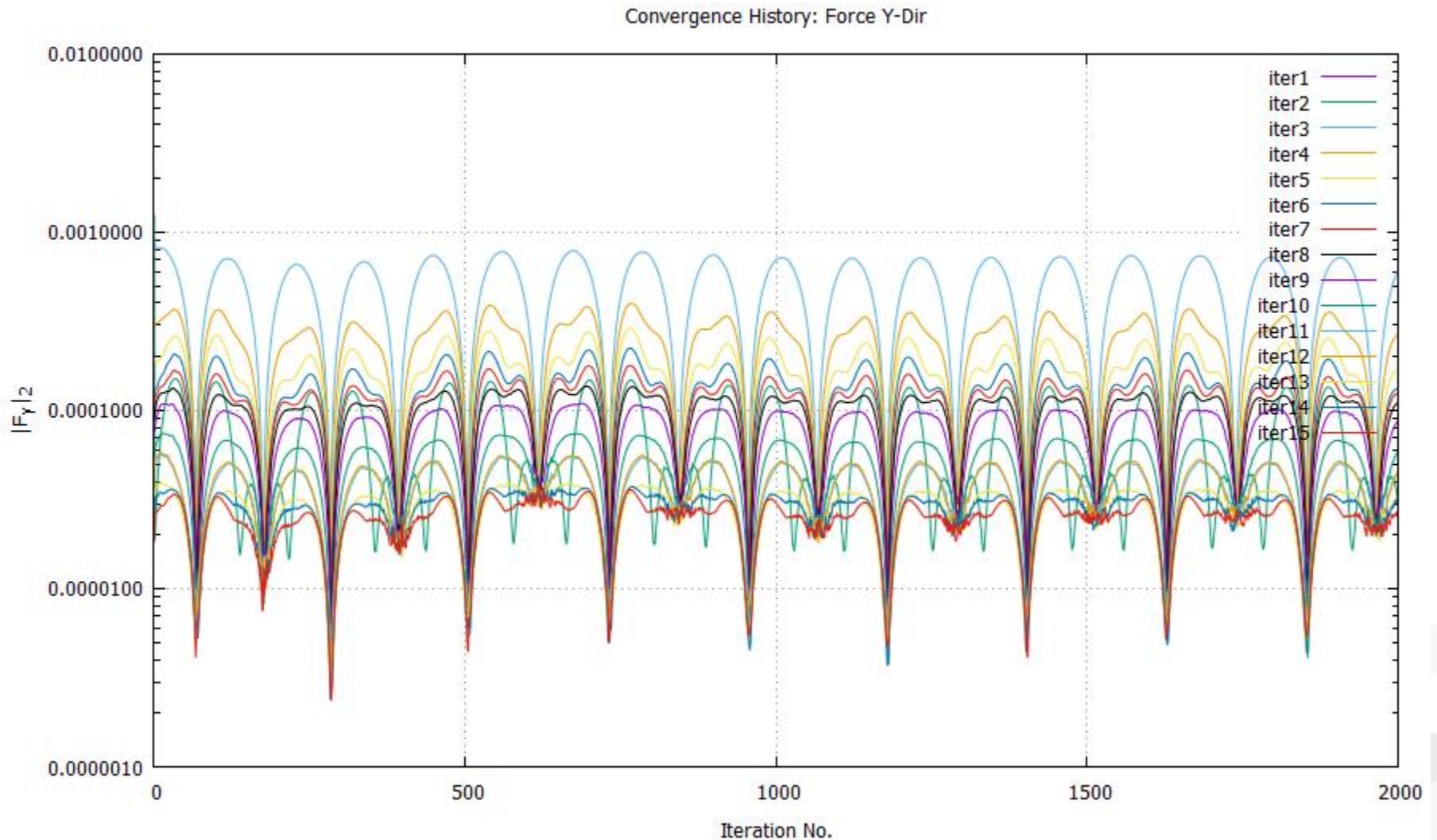
Sub-iteration Convergence History: dz



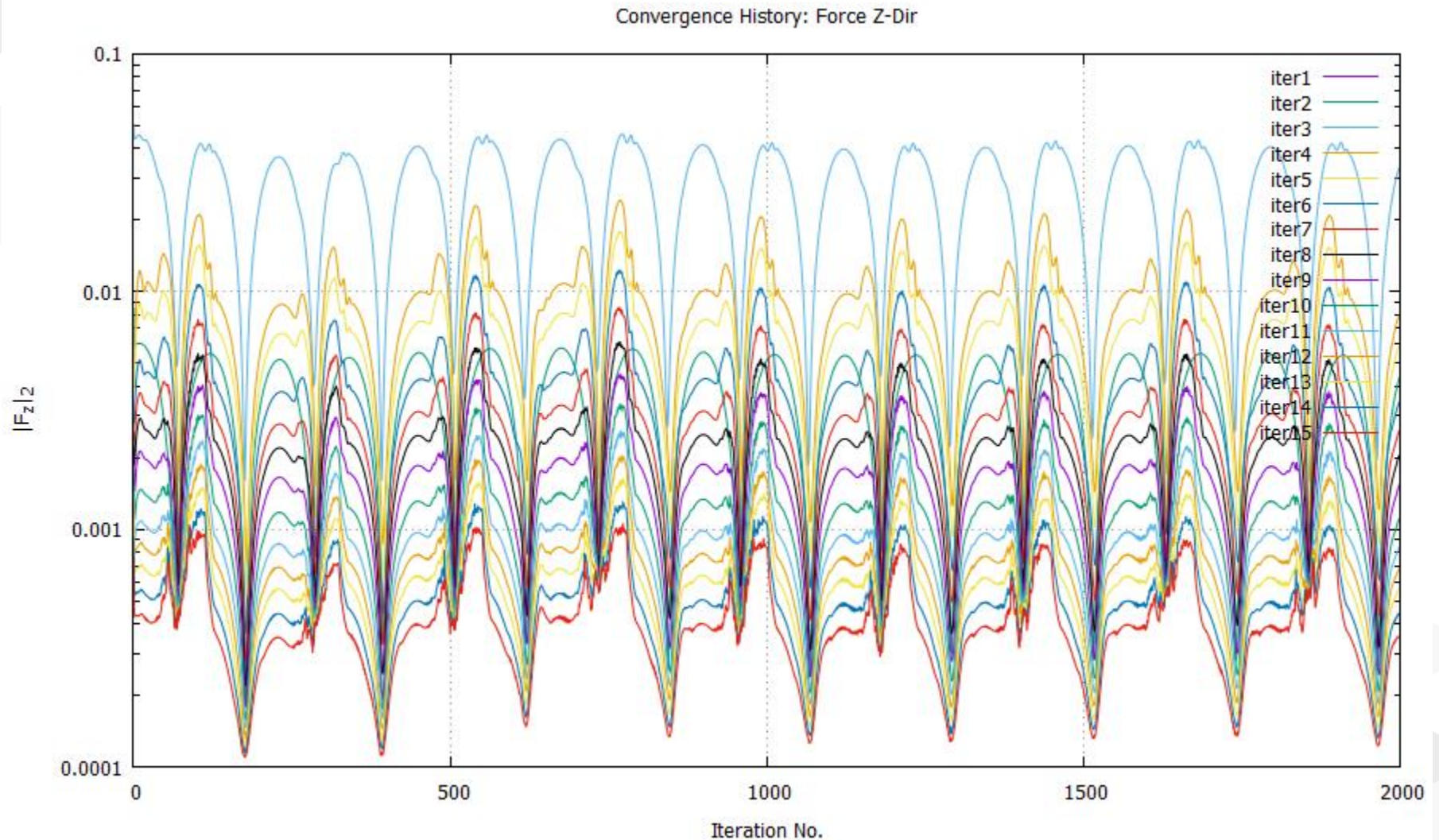
Sub-iteration Convergence History: Fx



Sub-iteration Convergence History: Fy



Sub-iteration Convergence History: Fz

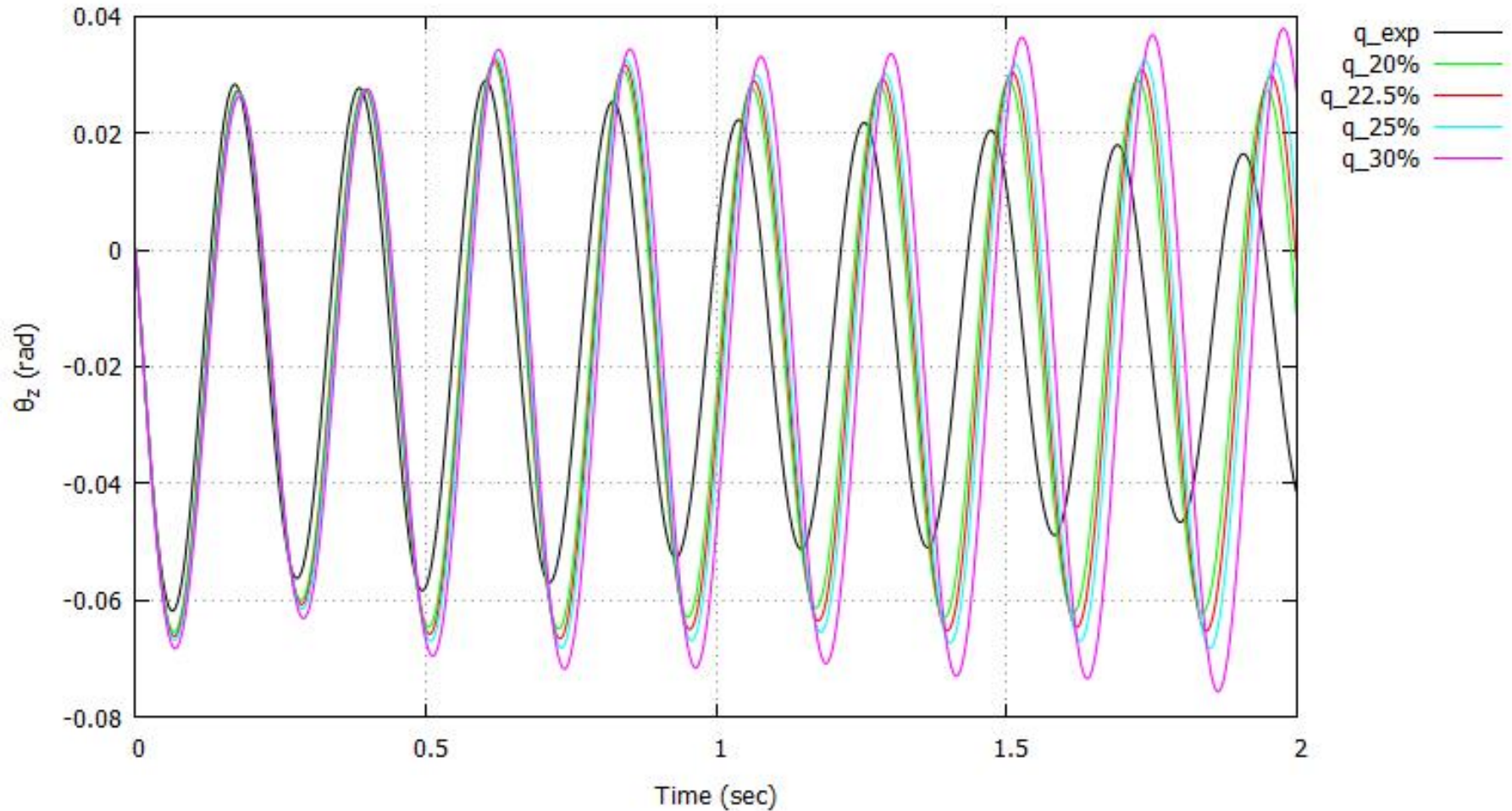


Case 2 Summary

	Experimental Condition F=4.3 Hz, Q=168.8 psf			Predicted Flutter Condition			
	Freq. (Hz)	% Error	Damping	Freq. (Hz)	% Error	Q (psf)	% Error
Coarse	4.63	7.67	0.83%	4.46	3.72	206.78	22.5
Medium	4.59	6.74	0.94%	4.46	3.72	202.56	20
Fine	4.57	6.28	0.91%	4.46	3.72	202.56	20

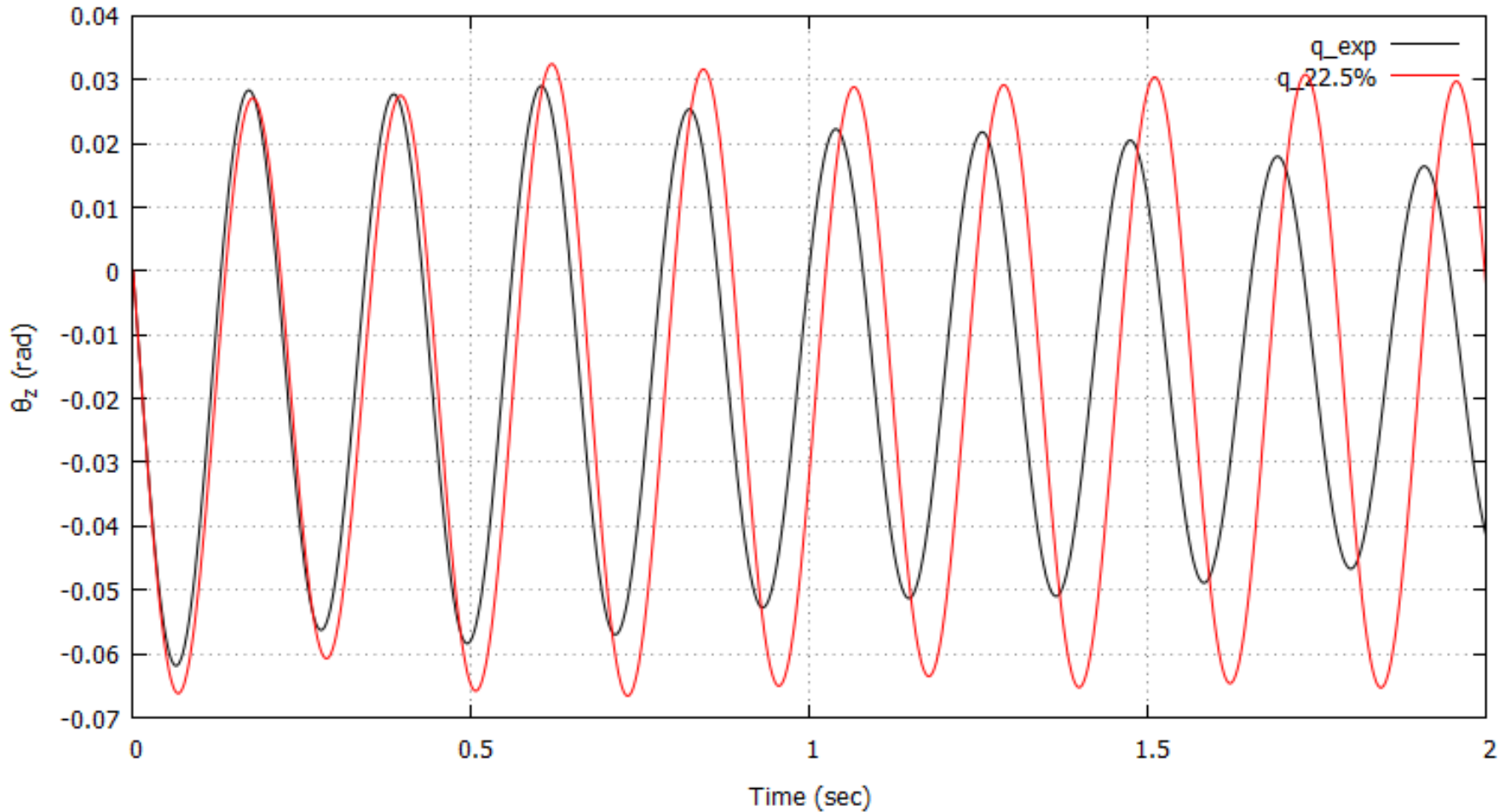
Case 2: Coarse Grid Pitch Response

Flutter Frequency = 4.45 Hz, $Q_f = +122.5\%$



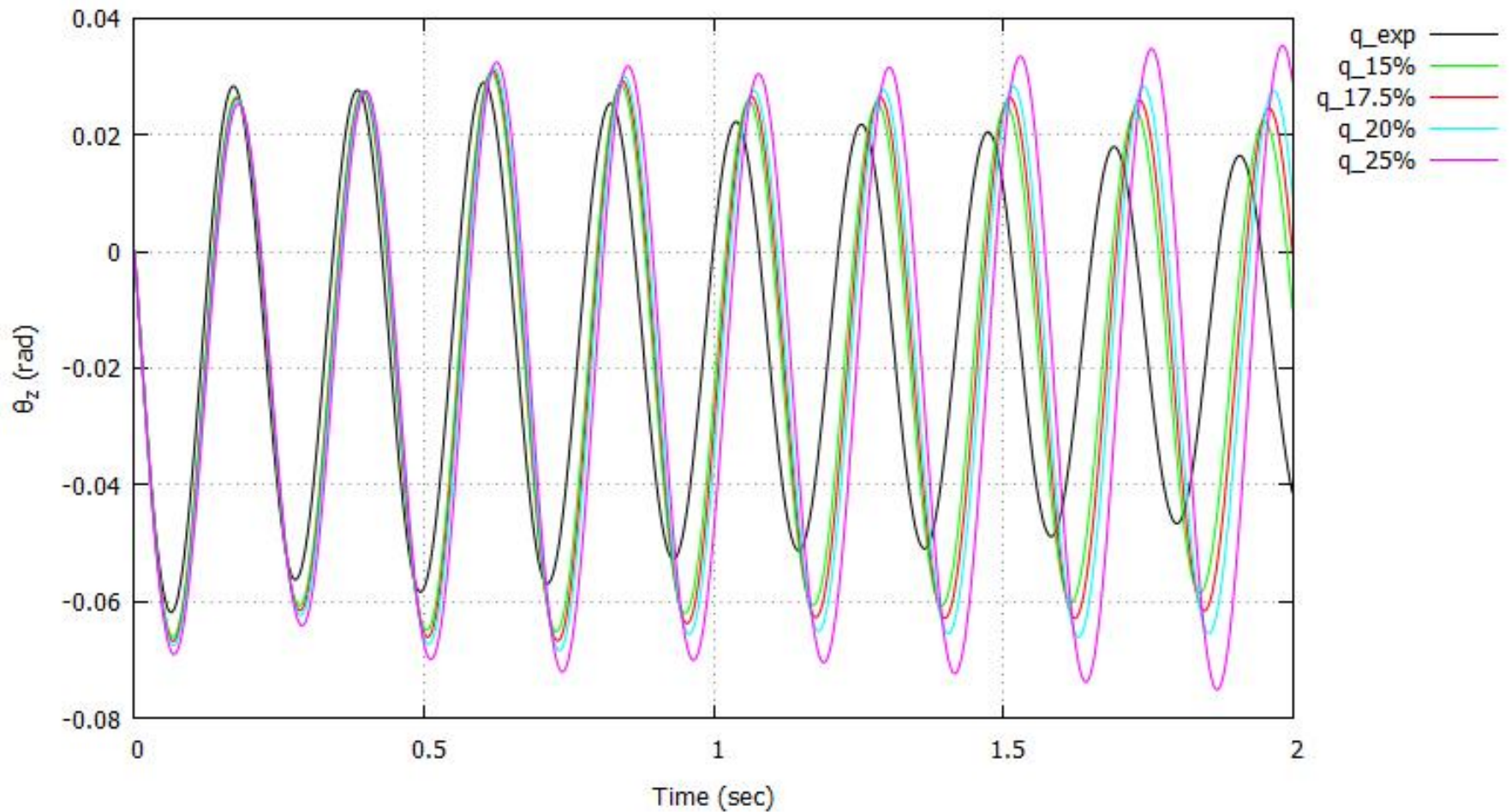
Case 2: Coarse Grid Pitch Response

Flutter Frequency = 4.45 Hz, $Q_f = +122.5\%$



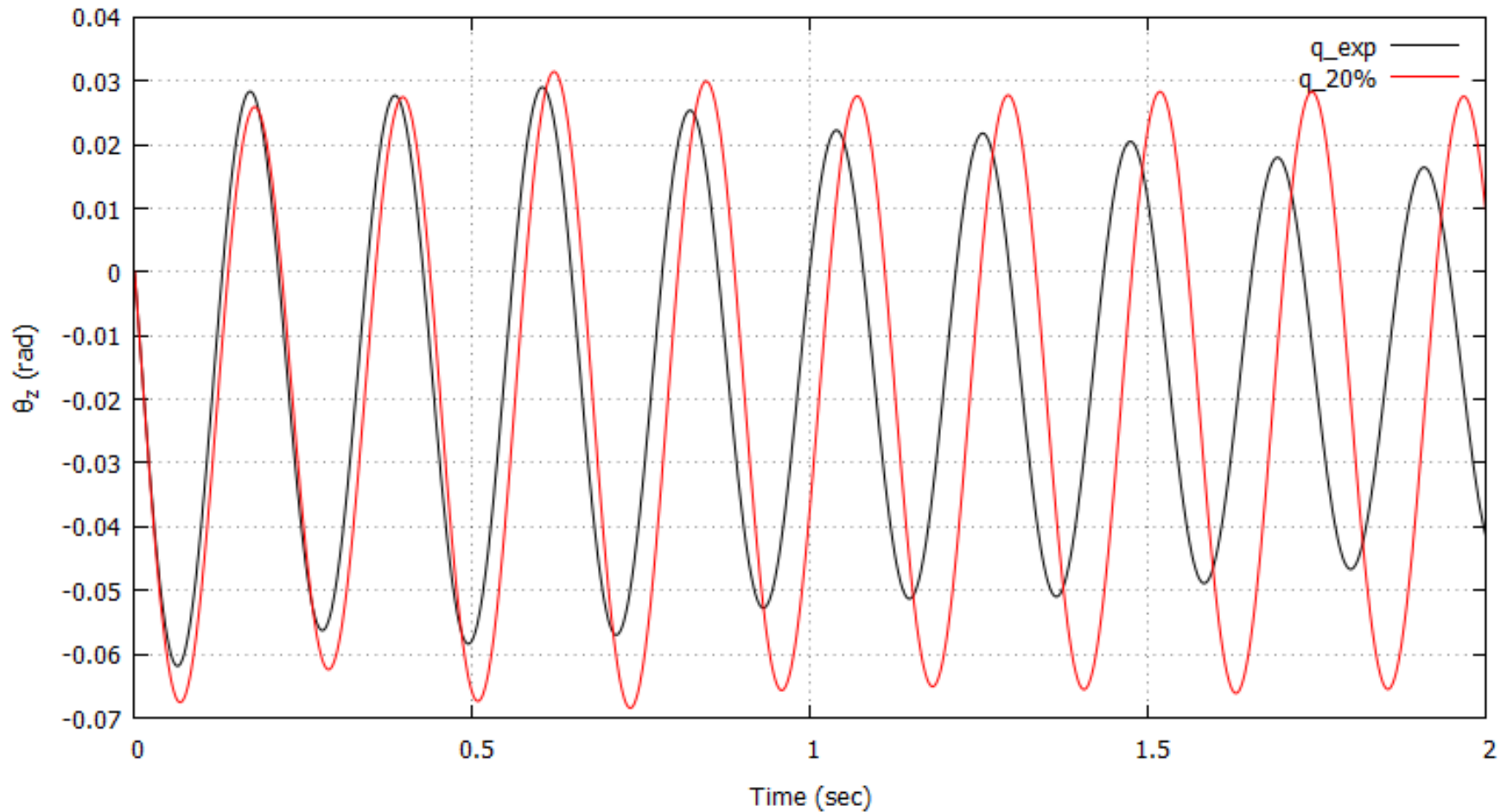
Case 2: Medium Grid Pitch Response

Flutter Frequency = 4.46 Hz, $Q_f = +120\%$



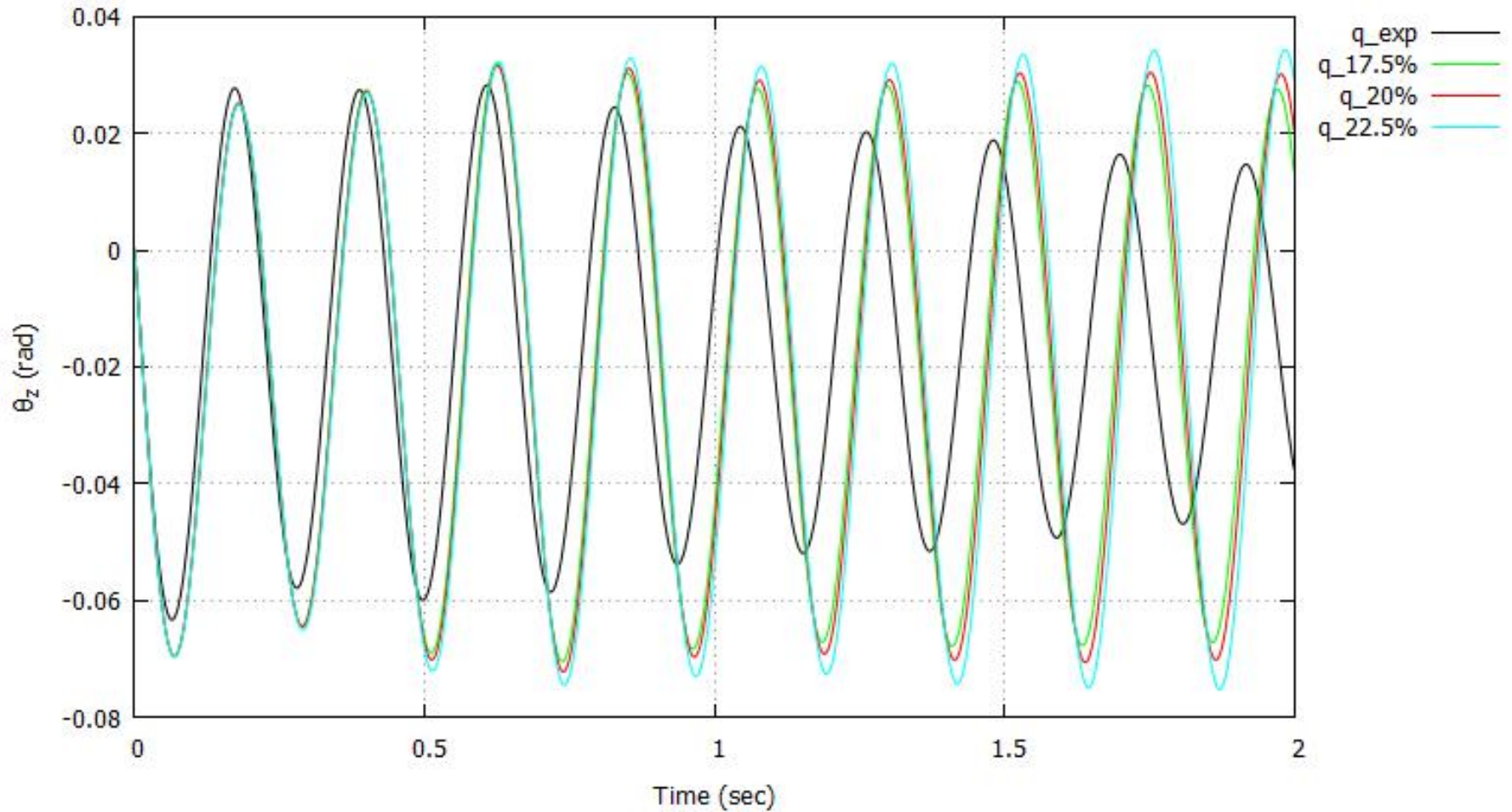
Case 2: Medium Grid Pitch Response

Flutter Frequency = 4.46 Hz, $Q_f = +120\%$



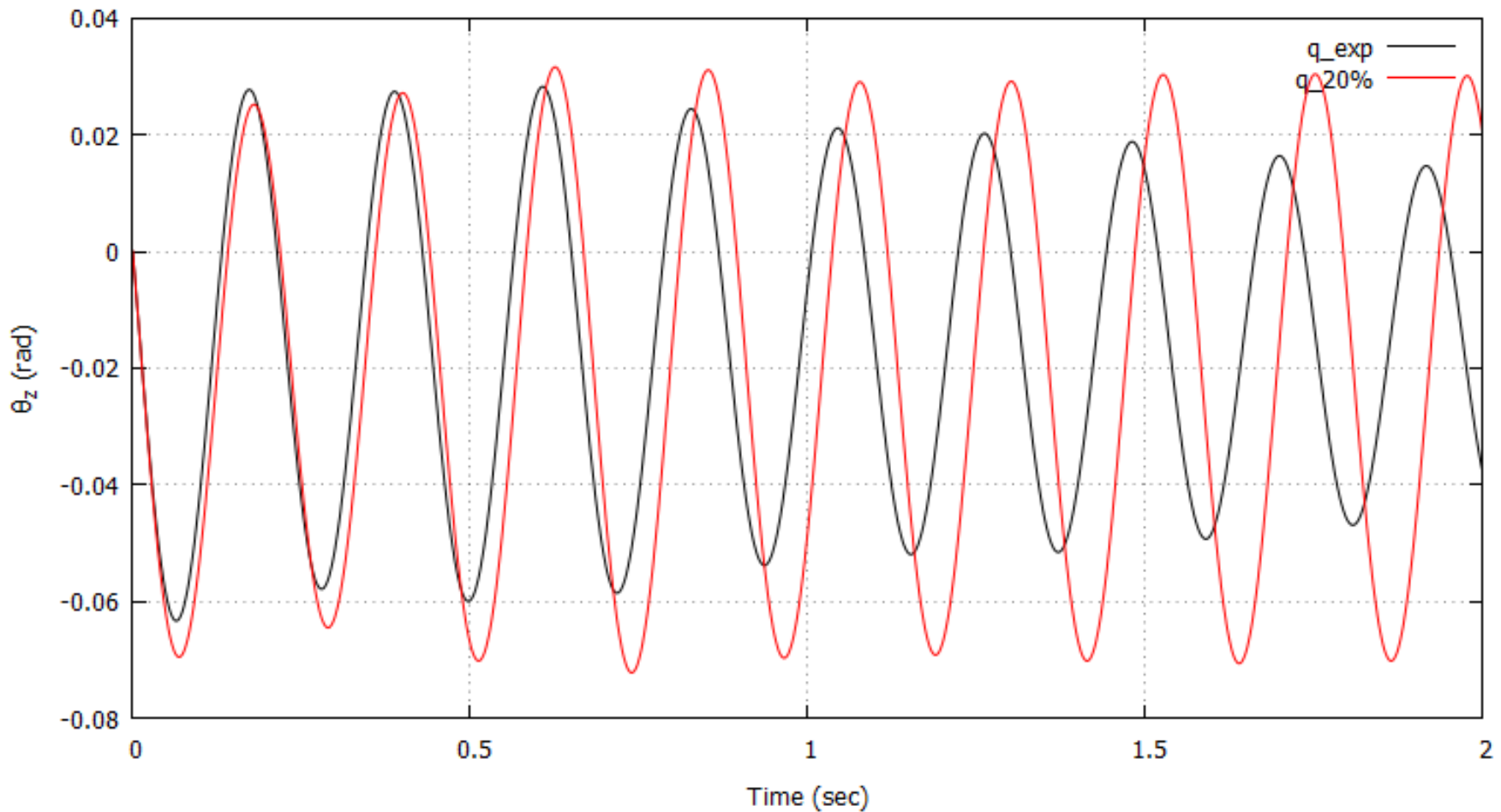
Case 2: Fine Grid Pitch Response

Flutter Frequency = 4.46 Hz, $Q_f = +120\%$



Case 2: Fine Grid Pitch Response

Flutter Frequency = 4.46 Hz, $Q_f = +120\%$

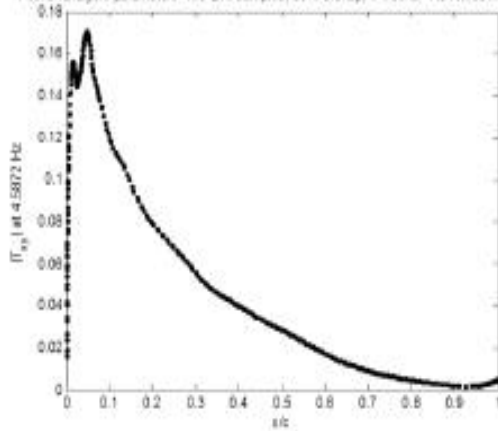


Case 2 FRF Data

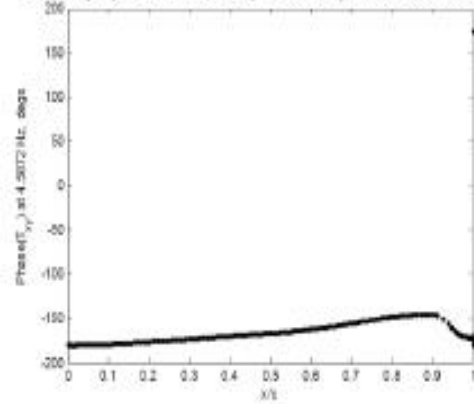
Fine Grid, 60% Span

Upper Surface

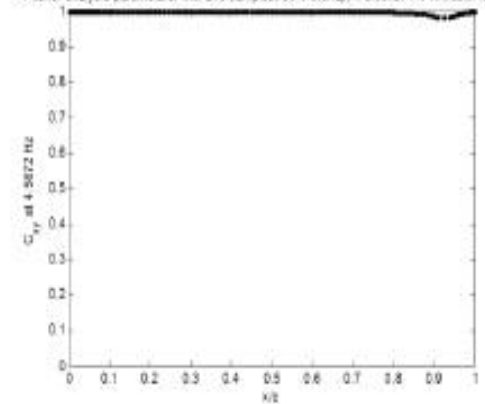
BBCW Analysis at Mach 0.74, 0°, Flutter at 4.5872 Hz
Input: ξ ; Output: C_p upper surface, 60% span station
Fourier analysis parameters: nfft: 216 samples, 90% overlap; # blocks: 14, Window: rectwin



BBCW Analysis at Mach 0.74, 0°, Flutter at 4.5872 Hz
Input: ξ ; Output: C_p upper surface, 60% span station
Fourier analysis parameters: nfft: 216 samples, 90% overlap; # blocks: 14, Window: rectwin

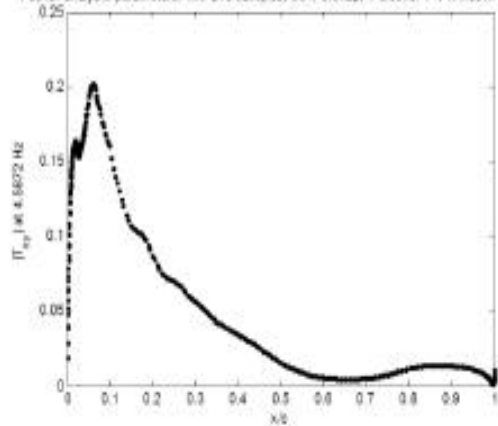


BBCW Analysis at Mach 0.74, 0°, Flutter at 4.5872 Hz
Input: ξ ; Output: C_p upper surface, 60% span station
Fourier analysis parameters: nfft: 216 samples, 90% overlap; # blocks: 14, Window: rectwin

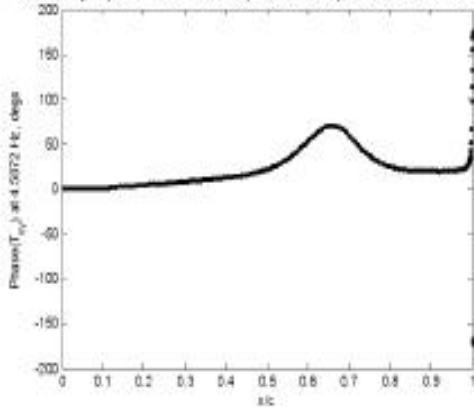


Lower Surface

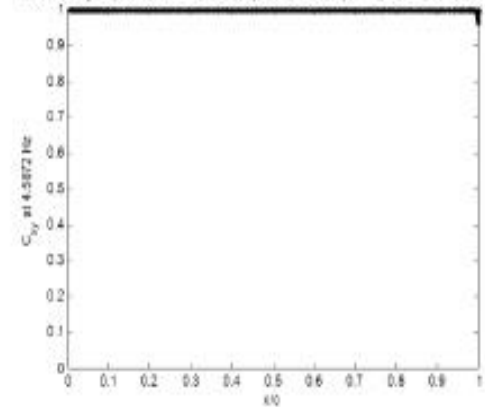
BBCW Analysis at Mach 0.74, 0°, Flutter at 4.5872 Hz
Input: ξ ; Output: C_p lower surface, 60% span station
Fourier analysis parameters: nfft: 216 samples, 90% overlap; # blocks: 14, Window: rectwin



BBCW Analysis at Mach 0.74, 0°, Flutter at 4.5872 Hz
Input: ξ ; Output: C_p lower surface, 60% span station
Fourier analysis parameters: nfft: 216 samples, 90% overlap; # blocks: 14, Window: rectwin



BBCW Analysis at Mach 0.74, 0°, Flutter at 4.5872 Hz
Input: ξ ; Output: C_p lower surface, 60% span station
Fourier analysis parameters: nfft: 216 samples, 90% overlap; # blocks: 14, Window: rectwin

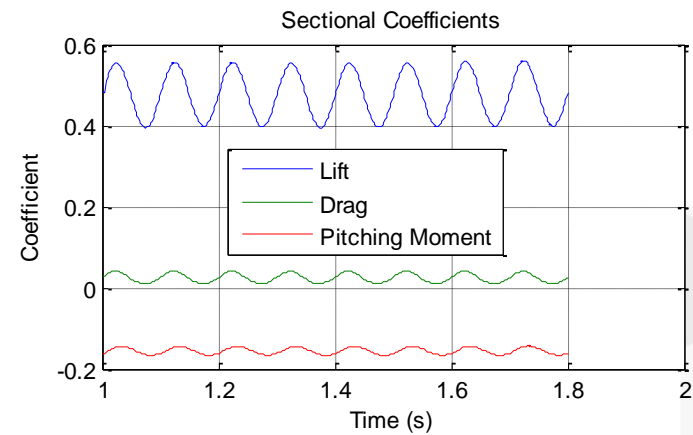
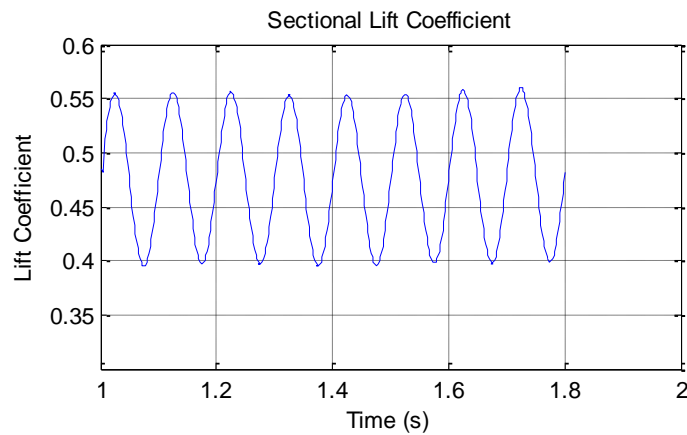
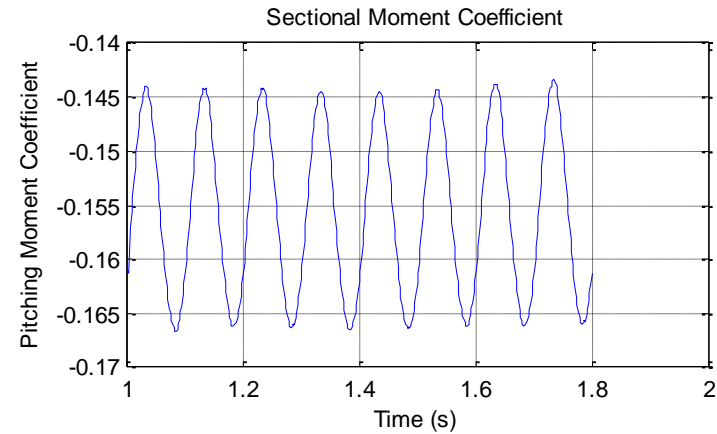
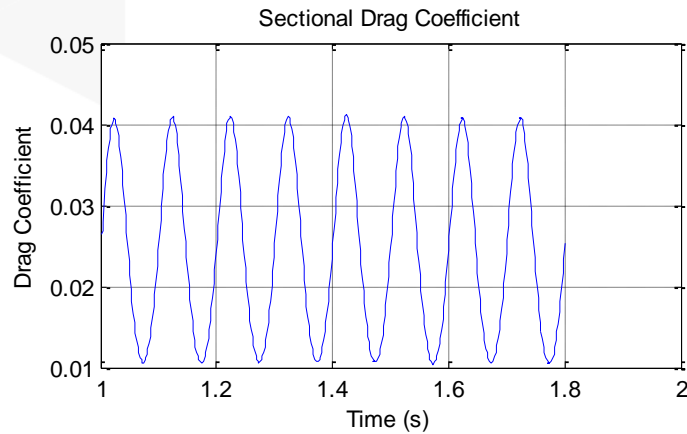


- Case 1: Unsteady pressure within experimental bounds
- Case 2: Flutter predictions estimate flutter at higher dynamic pressure (~20% higher)
 - Still investigating why
 - Generate own grid to resolve near wing region
 - Repeat without limiter
 - Need to conduct temporal study for Case 2
 - Need to complete steady/unsteady comparisons to experiment
- Coupling example: Strong coupling allows for larger time step than weak coupling

Questions?

Case 1: Coefficient Time Histories

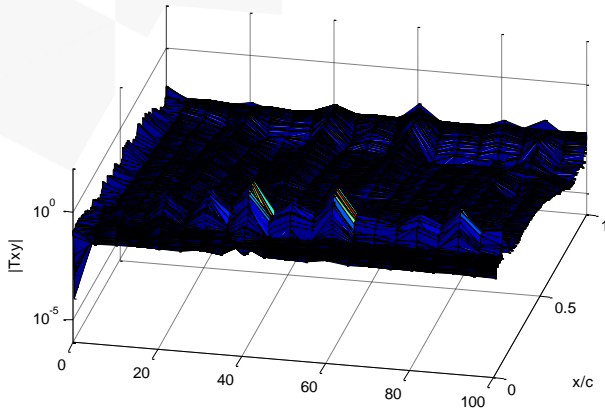
Fine Grid, 60 % Span



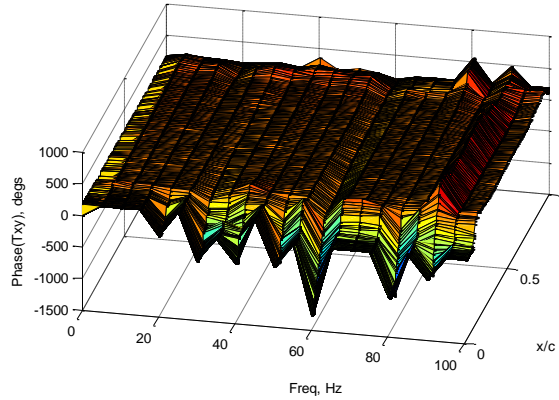
Case 1: FRFs

Fine Grid, 60 % Span

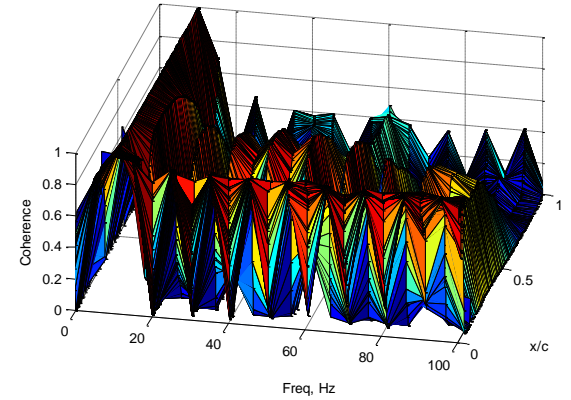
BSCW Analysis at Mach 0.7, 3° , Forced Oscillation at 10.0392 Hz
 Input: θ ; Output: Cp upper surface, 60% span station
 Fourier analysis parameters: nfft: 102 samples; 90% overlap; # blocks: 11, Window: rectwin



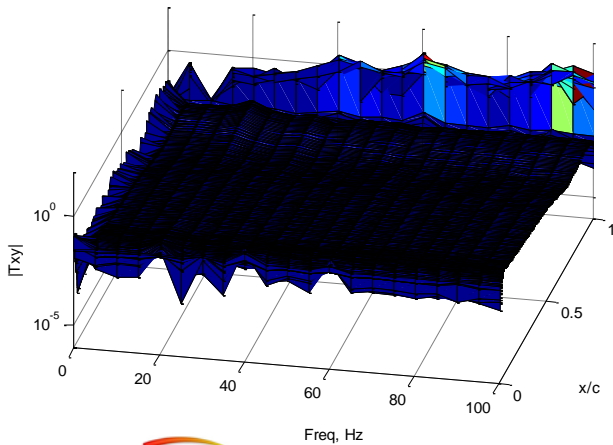
BSCW Analysis at Mach 0.7, 3° , Forced Oscillation at 10.0392 Hz
 Input: θ ; Output: Cp upper surface, 60% span station
 Fourier analysis parameters: nfft: 102 samples; 90% overlap; # blocks: 11, Window: rectwin



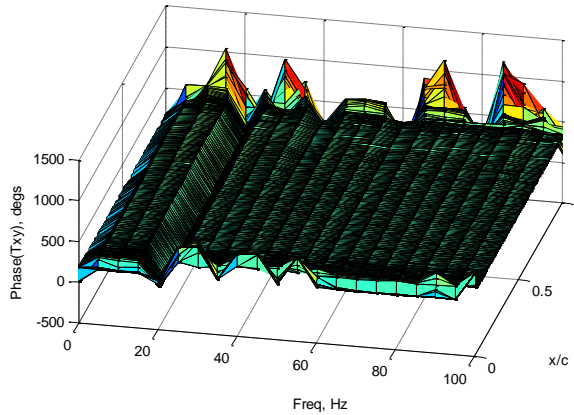
BSCW Analysis at Mach 0.7, 3° , Forced Oscillation at 10.0392 Hz
 Input: θ ; Output: Cp upper surface, 60% span station
 Fourier analysis parameters: nfft: 102 samples; 90% overlap; # blocks: 11, Window: rectwin



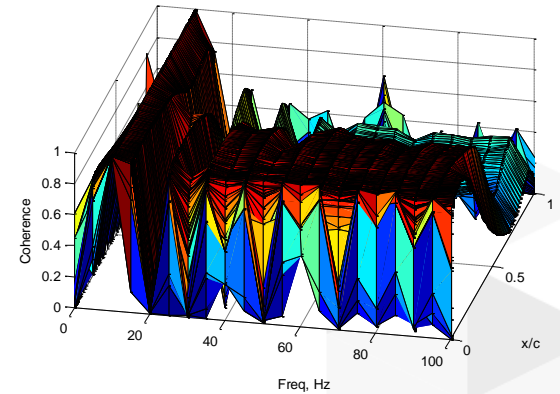
BSCW Analysis at Mach 0.7, 3° , Forced Oscillation at 10.0392 Hz
 Input: θ ; Output: Cp lower surface, 60% span station
 Fourier analysis parameters: nfft: 102 samples; 90% overlap; # blocks: 11, Window: rectwin



BSCW Analysis at Mach 0.7, 3° , Forced Oscillation at 10.0392 Hz
 Input: θ ; Output: Cp lower surface, 60% span station
 Fourier analysis parameters: nfft: 102 samples; 90% overlap; # blocks: 11, Window: rectwin



BSCW Analysis at Mach 0.7, 3° , Forced Oscillation at 10.0392 Hz
 Input: θ ; Output: Cp lower surface, 60% span station
 Fourier analysis parameters: nfft: 102 samples; 90% overlap; # blocks: 11, Window: rectwin



➤ Equations of motion

$$m\ddot{h} + S_\alpha \ddot{\alpha} + K_h = -L$$

$$S_\alpha \ddot{h} + I_\alpha \ddot{\alpha} + K_\alpha = M_{ea}$$

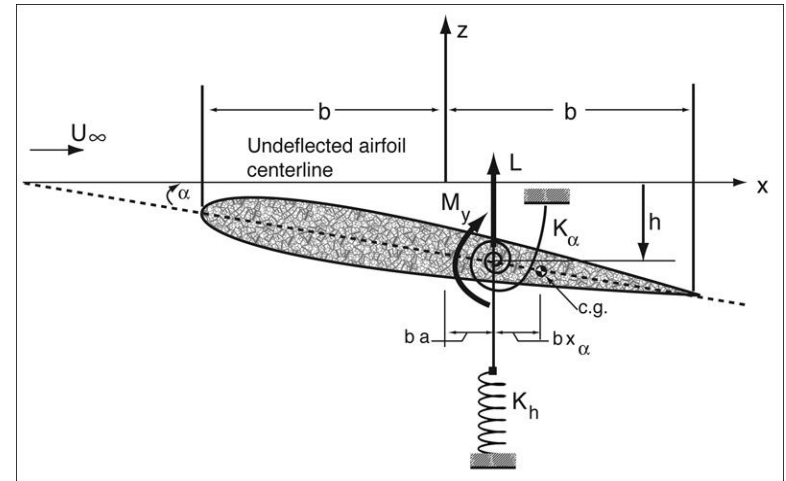
$$[M] = \begin{bmatrix} 1 & x_\alpha \\ x_\alpha & r_\alpha^2 \end{bmatrix} \quad [K] = \begin{bmatrix} \left(\frac{\omega_h}{\omega_\alpha}\right)^2 & 0 \\ 0 & r_\alpha^2 \end{bmatrix}$$

$$\mu = \frac{m}{\pi \rho b^2} = 60$$

$$a = -2.0$$

$$r_\alpha = \sqrt{\frac{I_\alpha}{mb^2}} = \sqrt{3.48} \quad x_\alpha = \frac{S_\alpha}{mb} = 1.8$$

$$\omega_h = \omega_\alpha = 100 \text{ rad/sec}$$



Exhibits a dramatic reduction in the flutter speed in the transonic region

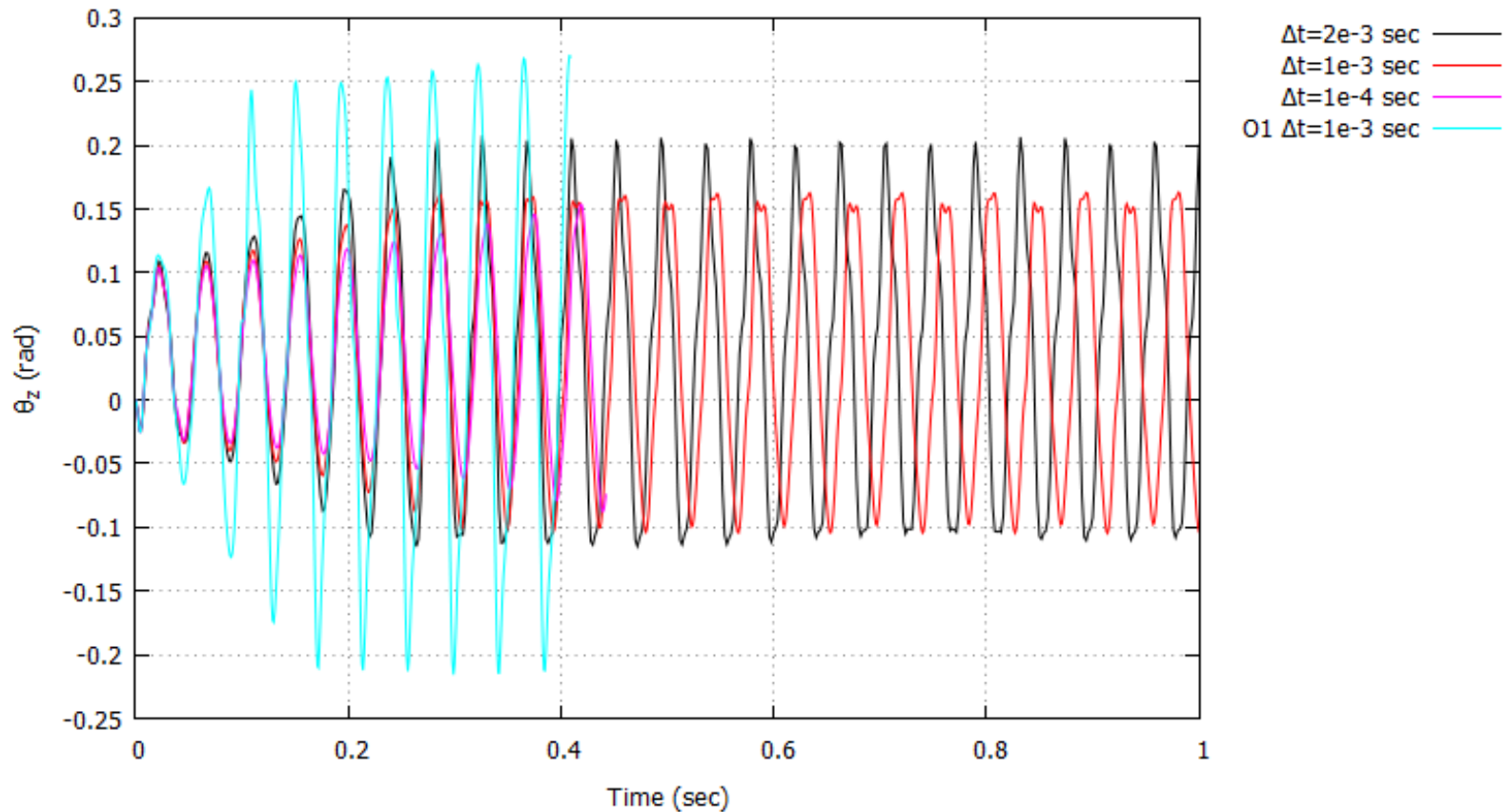
Pertinent Questions for FSI Simulations

- What is appropriate time step?
- When/how frequently to couple/exchange information?
 - How many sub-iterations are required?
- How to perturb the system?
 - Gust
 - Initial rotational velocity
 - Apply impulse force/moment to structure
 - Magnitude
 - Duration

Coupling Scheme Comparison

Neutrally Stable Condition

Second Order Coupling Time Step Study
NACA 64A010 Airfoil, Mach=0.7, $q=206,719$ kPa, $\alpha=3^\circ$



Case 1: Unsteady Pressure Slices at 60% span

Predicted shock location is forward of experiment

